



**AT&T Labs-Research**

# **Adaptive Learning: From Supervised to Active Learning of Statistical Models for Natural Language and Speech Processing**

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# Outline

## ◆ Learning Dimension:

- Passive vs. Active Learning
- Supervised vs Unsupervised Learning
- Combining Active and Unsupervised Learning

## ◆ Application Dimension:

- Classification (Text categorization, Part of Speech Tagging, Call Classification,...)
- Automatic Speech Recognition
- Syntactic Parsing

# Learning

## ◆ Describe (natural) phenomenon

- *Apple falling off the tree (XVII century)*
- *NASDAQ (XX century)*

## ◆ Data collection (**Experiment**)

- **Experiments vs Measurements**

“Do you like candidate X?”

“Do you like candidate X or rather Y?”

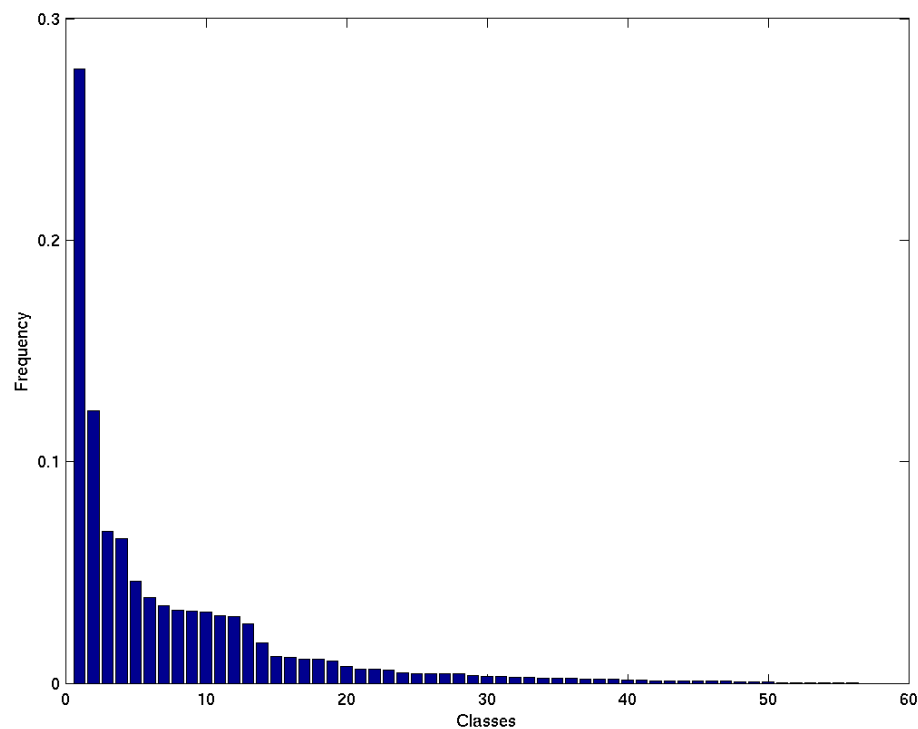
## ◆ Modeling data (**Prediction**)

- *What if I jump off a tree?*
- *Is candidate Y going to win the election?*

# Passive Learning

## ◆ Typical Class Distribution

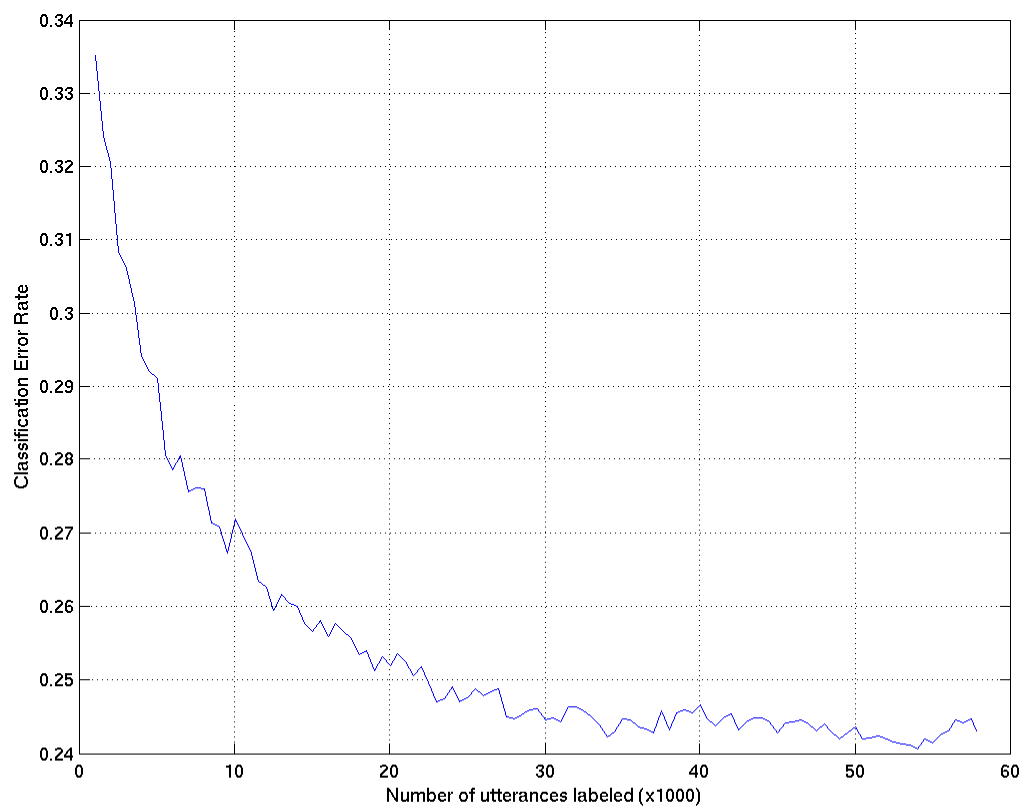
- Zipf's Law: *Frequency  $\times$  Rank = Constant*
- *Sample infrequent examples (tail of the distribution)*



# Passive Learning

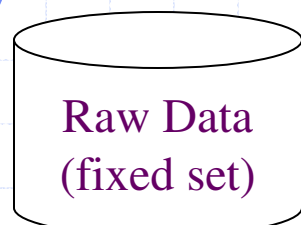
## ◆ Typical Learning Curve

- “no data like more data”



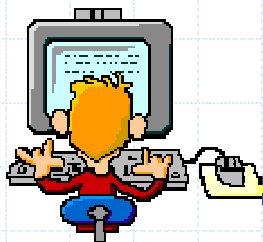
# Supervised Learning

(the nineties)

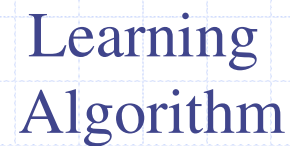
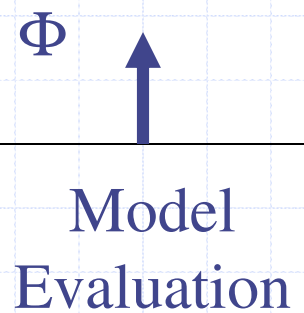


Speech Utterances (ASR)  
Raw Transcriptions (NLU)

ATIS (0.5  $10^6$  words)  
WSJ (25  $10^6$  words)  
SWBS (3  $10^6$  words)



delay

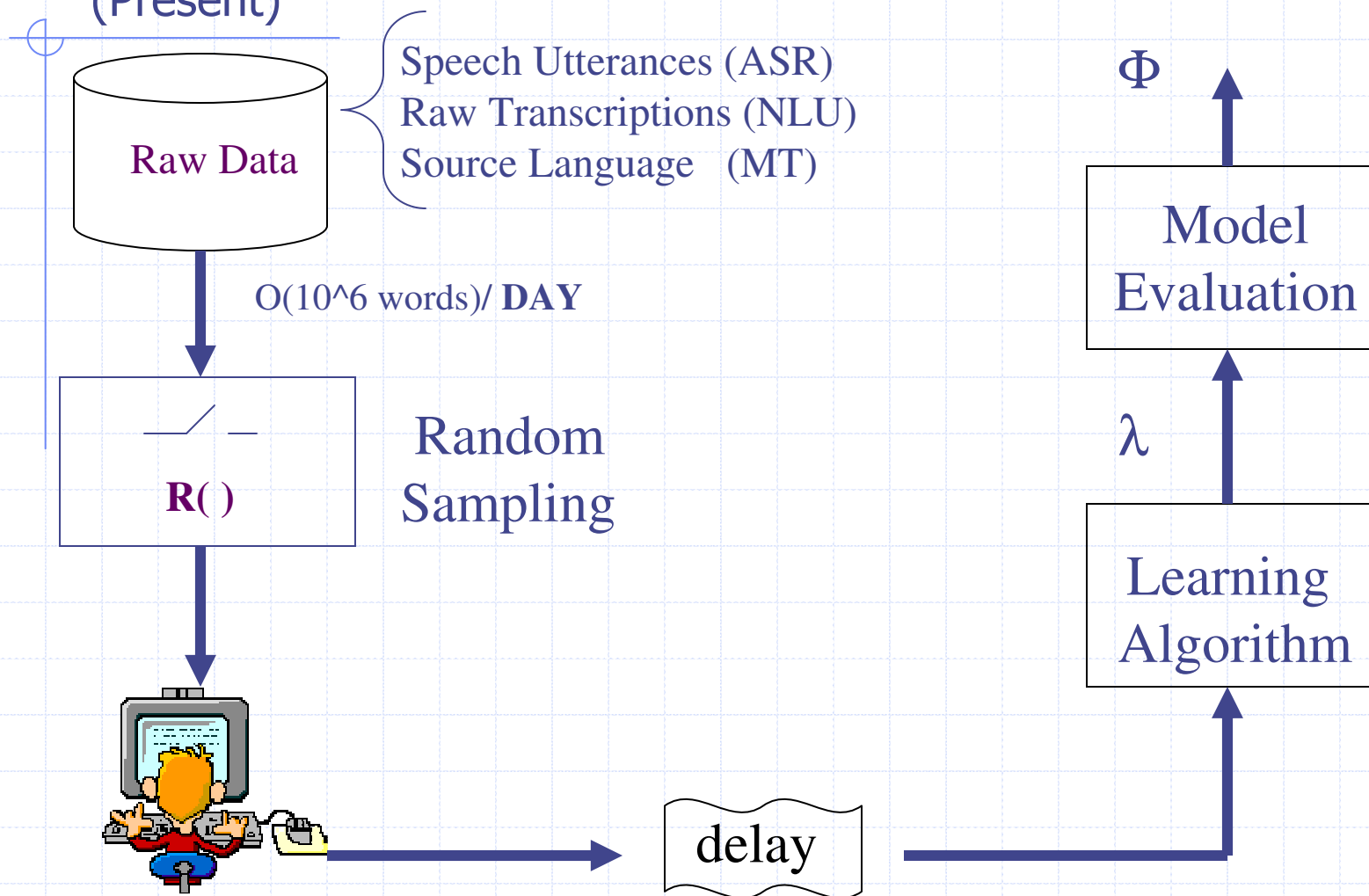


$\Phi$

$\lambda$

# Supervised Learning

(Present)





# Data Driven Learning

- ◆ The Eighties: (almost) no data, prior knowledge
- ◆ The Nineties: Data Driven Models
  - DARPA projects (ATIS, WSJ)
  - “no data like more data”
- ◆ Third Millenium
  - Terabytes of Data (*“Data Divide between University and Private Research”*)
- ◆ Supervised Learning (*learning from examples*)
  - Small data set
  - Human intervention (labeling or annotation)
  - Delayed Response

# Maximum Likelihood (1)

- ◆ The General setting
- ◆ Data Samples (Measurements) i.i.d.
  - $X = \{x_1, \dots, x_N\}$
- ◆ Underlying probability law  $p(X)$  with parameters  $\theta$
  
- ◆  $P(X | \theta) = \prod_k p(x_k | \theta)$ 
  - (log) Likelihood function

# Maximum Likelihood (2)

## ◆ Example: Binary random variable

$$X = \{x_1, x_1 \cdots, x_N\}$$

Training set of data samples

$$L(X, \theta) = P(X | \theta)$$

Likelihood Function

$$\log L(X, \theta) = \log(p^{N_1} (1-p)^{N_2}) = N_1 \log p + N_2 \log(1-p)$$

$$\frac{d \log L(X, \theta)}{d \theta} = 0$$

Likelihood Maximization

$$p = \frac{N_1}{N_1 + N_2}$$

# Maximum Likelihood (3)

## ◆ Example: Language Modeling

$$\begin{aligned} P(W) &= P(w_1 w_2 \cdots w_N) \\ &= \prod_i P(w_i | w_1 \cdots w_{i-1}) \\ &= \prod_i P(w_i | w_{i-n+1} \cdots w_{i-1}) \end{aligned}$$

## Example: Language Modeling

### Data Sparseness Problem

- Large Vocabulary ( $|V| \sim 50K$ )
- Generalization
  - ◆ I would like {a, to, the, this,..}
- Zipf's Law (frequency of n-gram  $\propto 1/n$ )

### Maximum Likelihood (ML) Probability

$$P(w_i | w_{i-n+1}, \dots, w_{i-1}) = \# w_1 w_2 \dots w_i / \# w_1 w_2 \dots w_{i-1}$$

### Discounted ML Probability

$$\hat{P}(w_i | w_{i-n+1}, \dots, w_{i-1}) = \alpha(w_1 w_2 \dots w_i) P(w_i | w_{i-n+1}, \dots, w_{i-1})$$

# Discriminative Training

- ◆ The goal of ASR is to minimize the probability of error. This does not necessarily imply maximizing  $P(X | \Phi)$ .
- ◆ Discriminative Training methods are applied to maximize a function that provides better discrimination between classes.
- ◆ Automatic Speech Recognition
- ◆ Text Classification

# Adaptive Learning

## ◆ Describe (natural) phenomenon

- NASDAQ (Measurements over a month in April)
- $X = X_1, X_2, X_3, \dots, X_N$
- What if a war is going on?
- $X = X_1(t), X_2(t), X_3(t), \dots, X_N(t)$
- Time dependent statistics
  - ◆ Stationary (e.g. seasonal effects)
  - ◆ Bursty (e.g. unforeseen events)

## ◆ Adaptive Learning

- Prediction is based on **current estimates (input) and adapts (output)**.
- **State** of the system

# Adaptive Learning

## ◆ Definition

- Adapt fast to changes in feature statistics
- Learn new events
- Minimize supervision

◆ Instead of assuming a fixed and given training data as in the passive learning, the data is dynamic and determined by the learner itself.



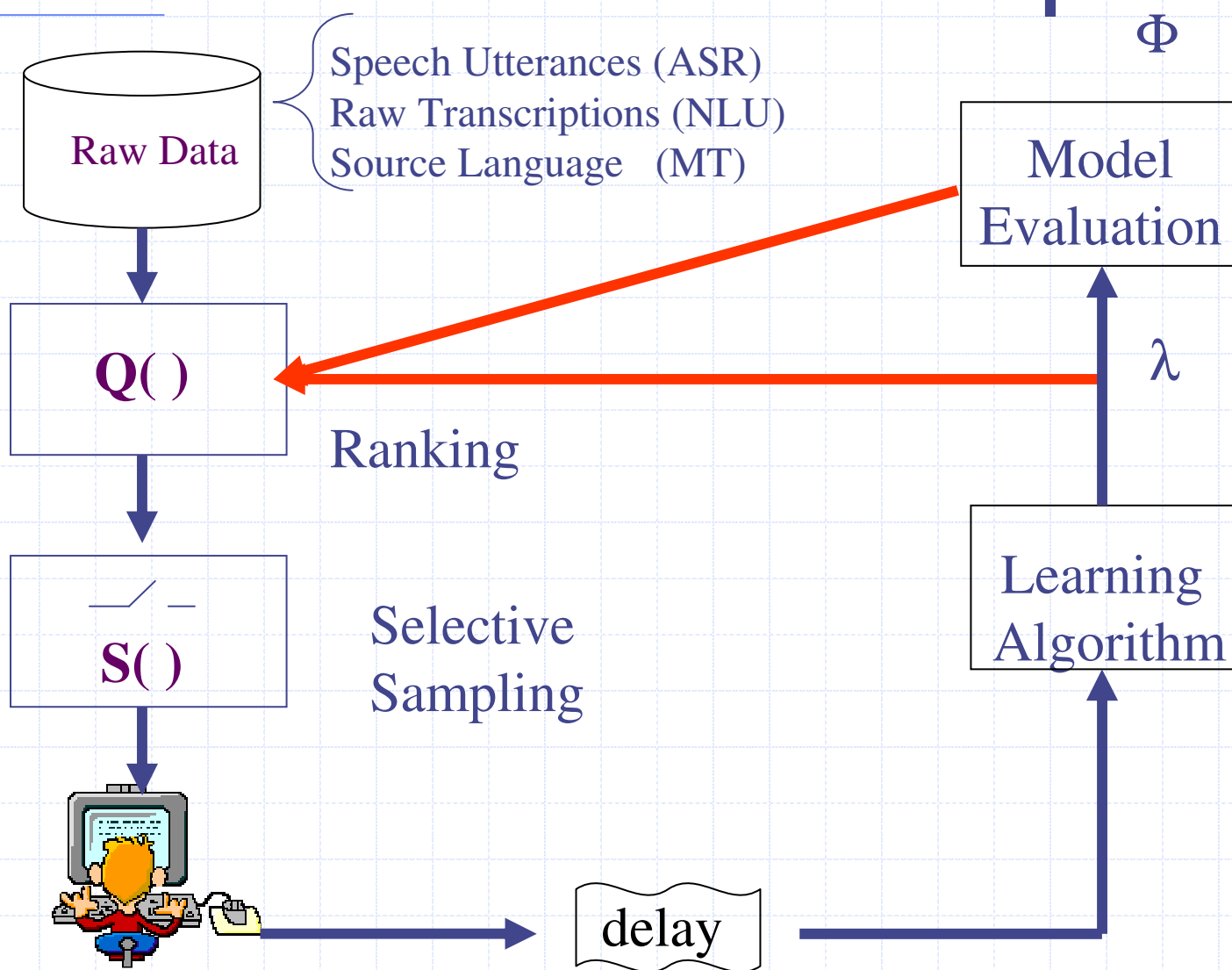
# Adaptive Learning

- ◆ Methods for adaptive learning:
  - Active learning
  - Unsupervised learning
  - Combining active and unsupervised learning

# Outline

- ◆ Algorithm Dimension:
  - Passive vs. Adaptive Learning
  - **Active Learning**
    - ◆ Certainty-based
    - ◆ Committee-based
  - Unsupervised Learning
  - Combining Active and Unsupervised Learning

# Active Learning



# Active Learning

(static)

- ◆ Sample space  $T$  is very large and finite (size  $N$ )

*Select  $K_{min}$  examples from  $T$  to label such that  $\Delta\Phi$  is maximized on a random test set*

- ◆ The number of combinations of  $k$  examples is very large ( $N!/k!(N-k)!$ )
- ◆ The number of permutations of  $k$  examples is very large ( $k!$ )

# Active Learning

(dynamic)

- ◆ Sample space  $T$  is very large (size  $N$ )
- ◆ At time  $t$  there are  $K(t)$  samples available

At time  $t$ , for a given  $K(t)$  in  $T$ ,

*Compute  $K_{min}$  examples from  $K(t)$  to label*  
such that  $\Delta\Phi$  is maximized on a random  
test set

- ◆ Compute  $\rightarrow$  Select from a given  $T$
- ◆  $t = \infty$

# Ranking Sample Space (1)

◆  $T = \{u_i\}$

- Set of all examples

◆  $Q(u_i) = j$

- Compute confidence scores for each example
  - ◆ Probability that example  $u_i$  is correctly labeled by the current model  $\lambda$
- Sort

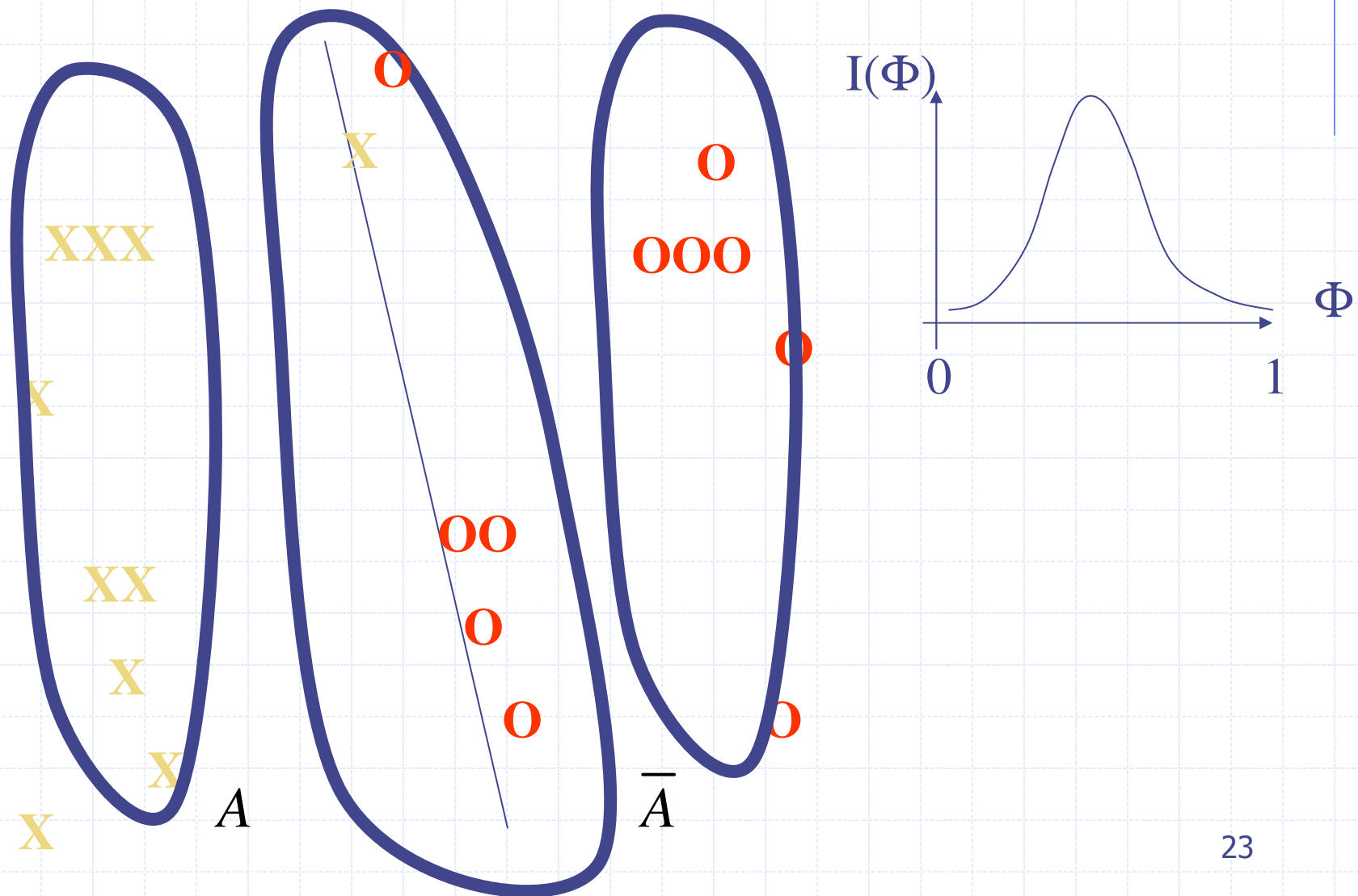
◆ **Selective Sampling  $S()$**

- $S(T) = (1, \dots, K_{\min})$

◆ Label  $S(T)$

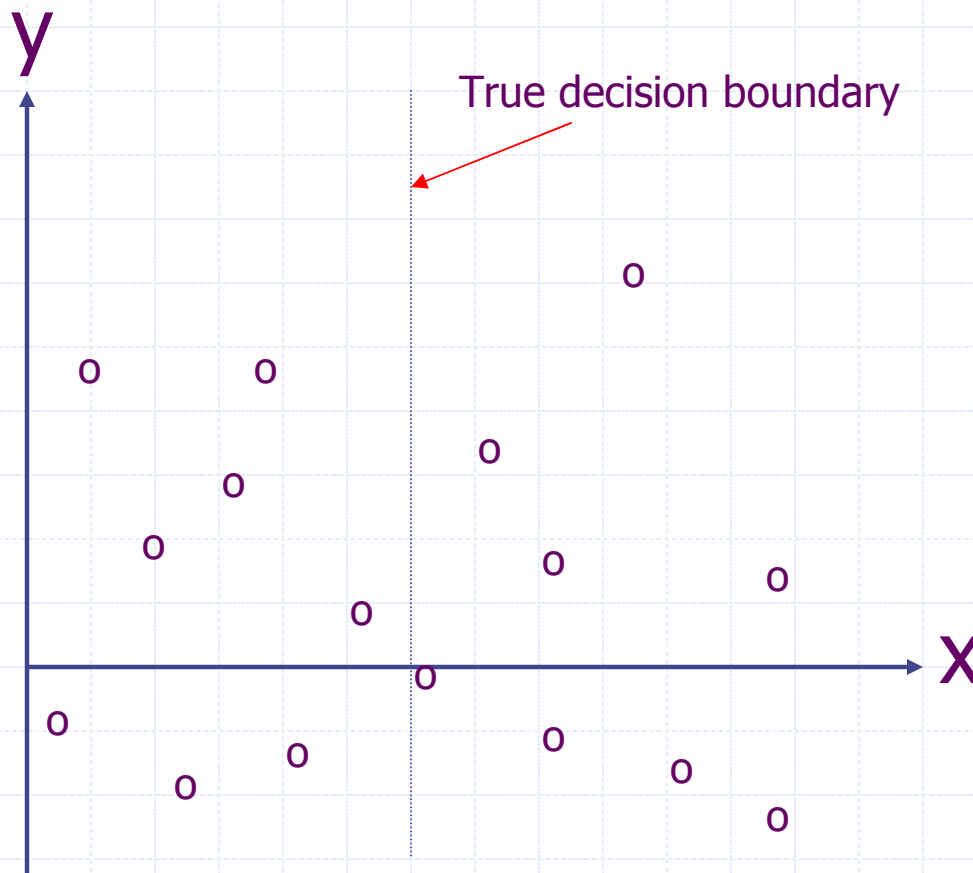
# Ranking Sample Space (2)

(classification case)



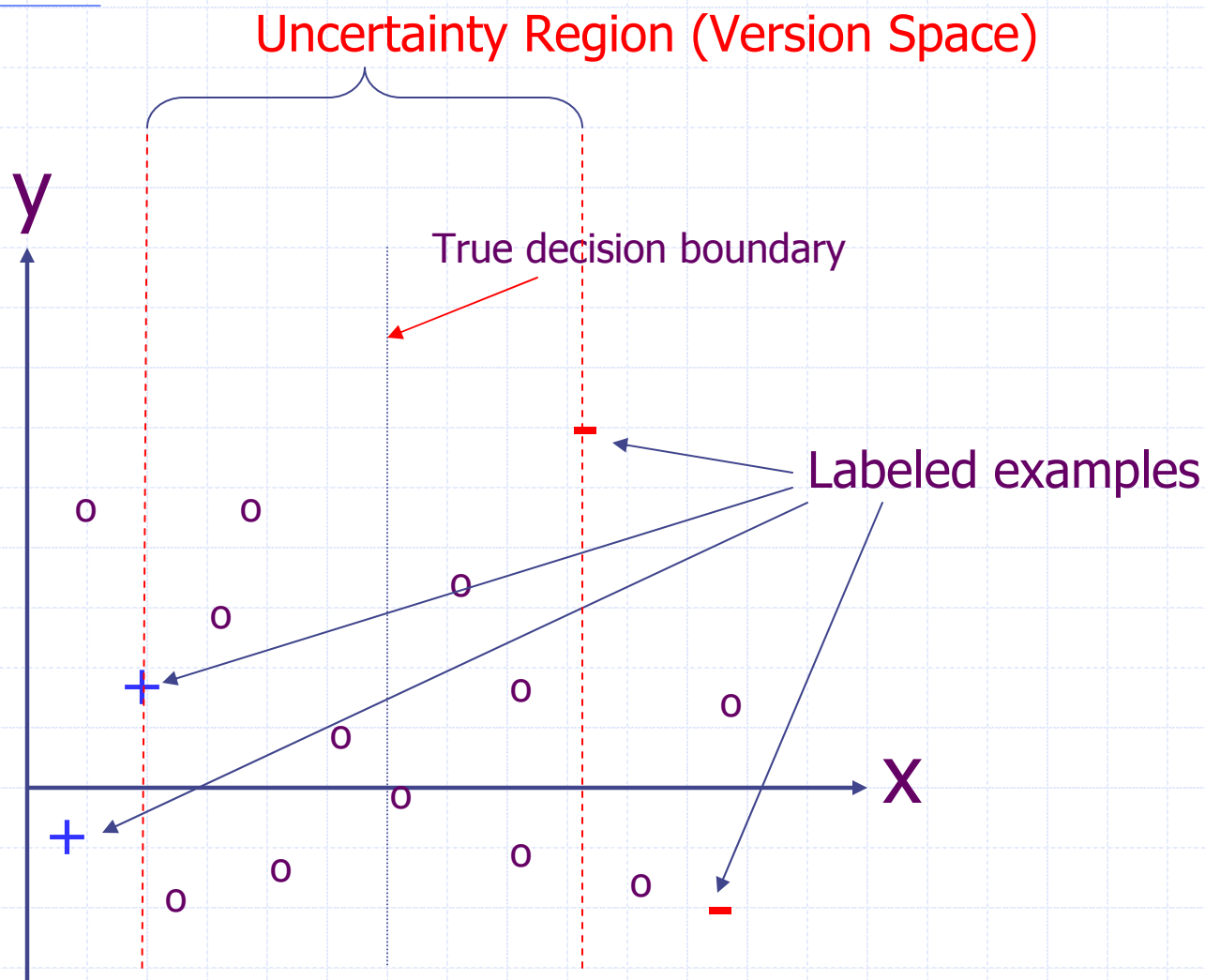
# A Simple Binary Classification Example

TASK: Locating a boundary on the unit line (x-axis) interval.

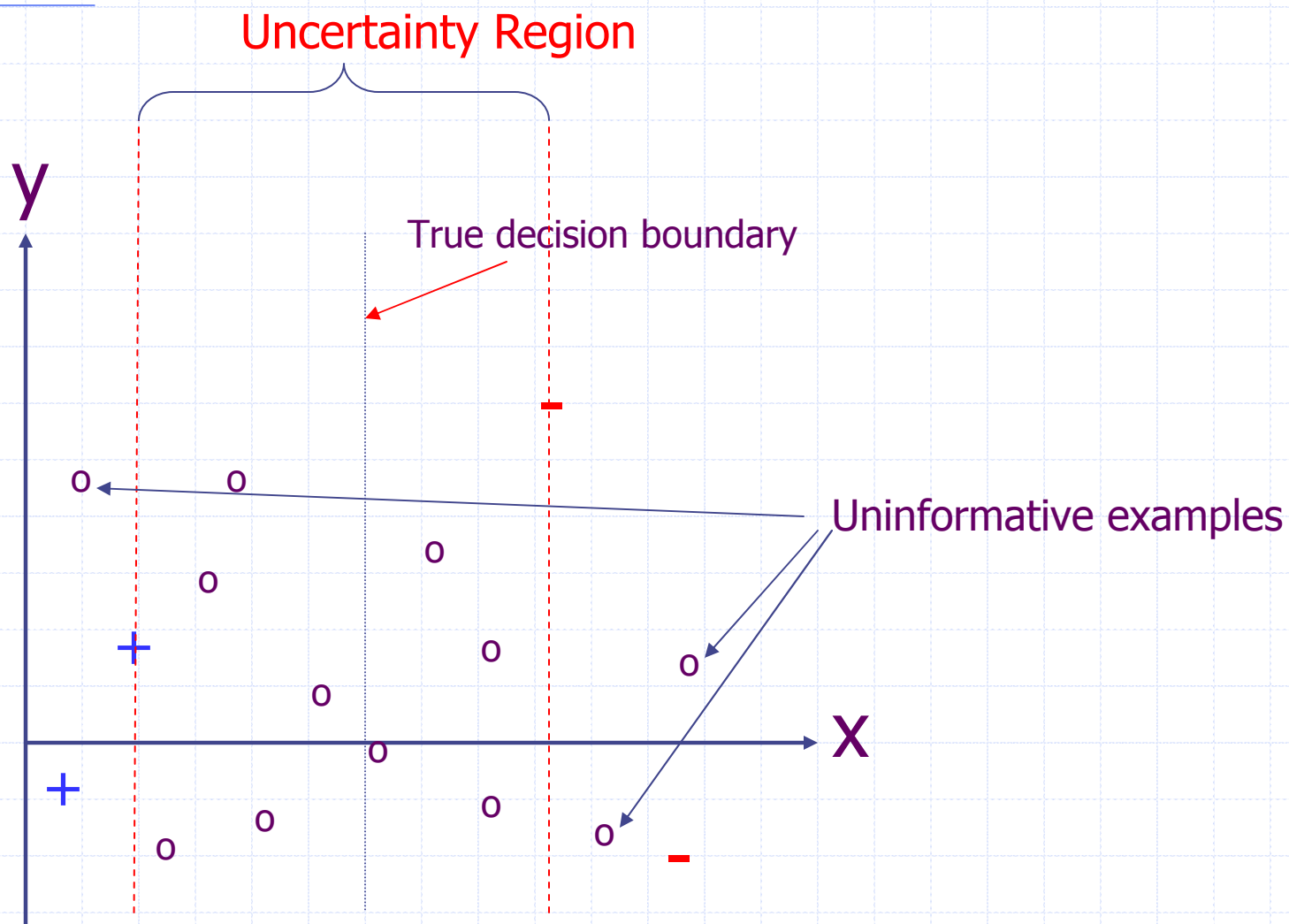




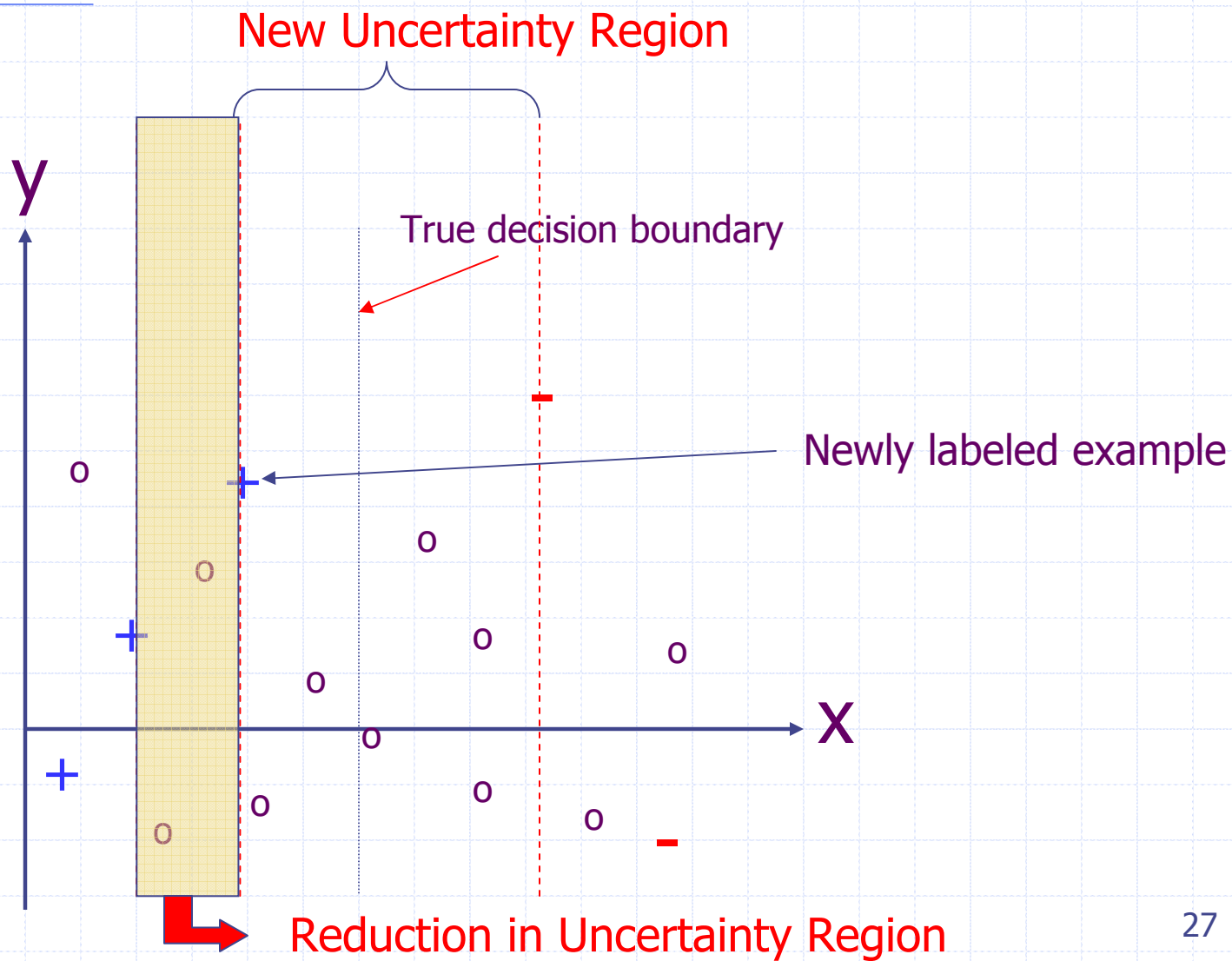
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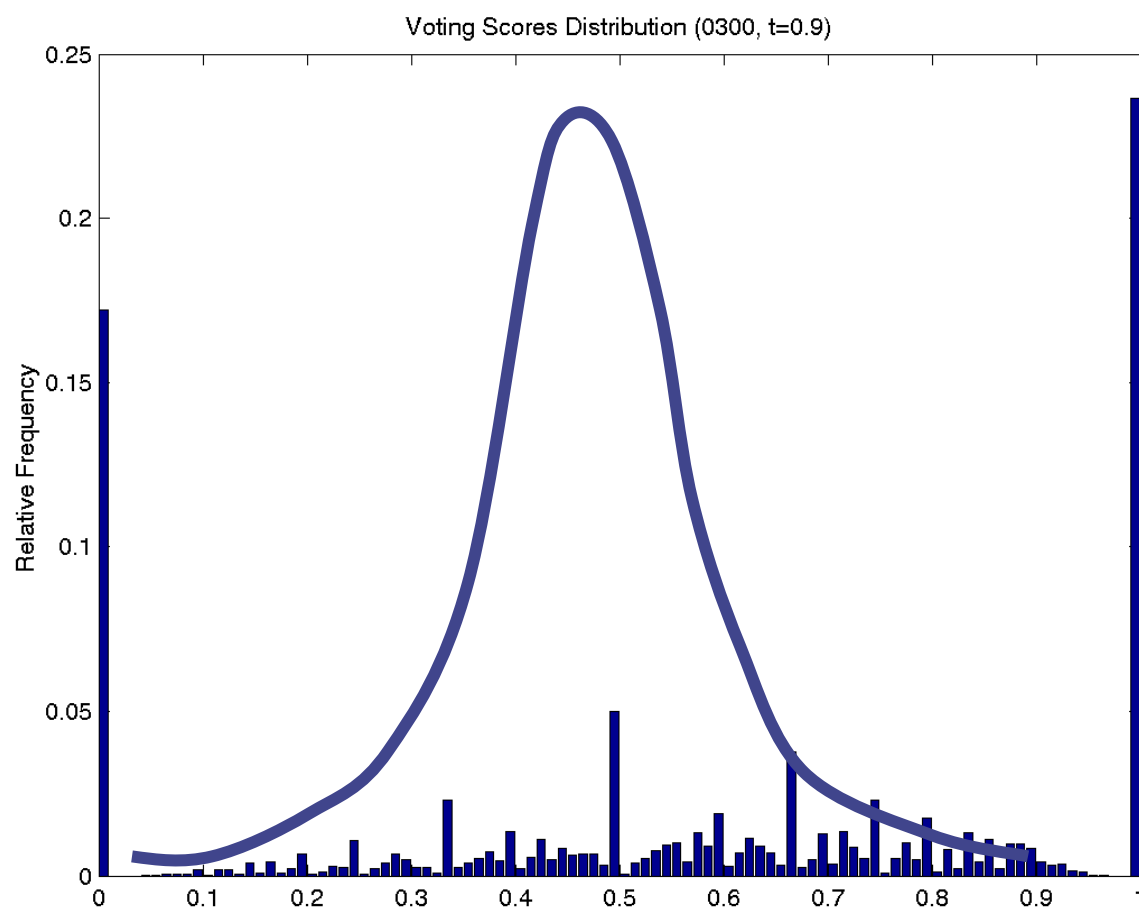
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# A Simple Binary Classification Example



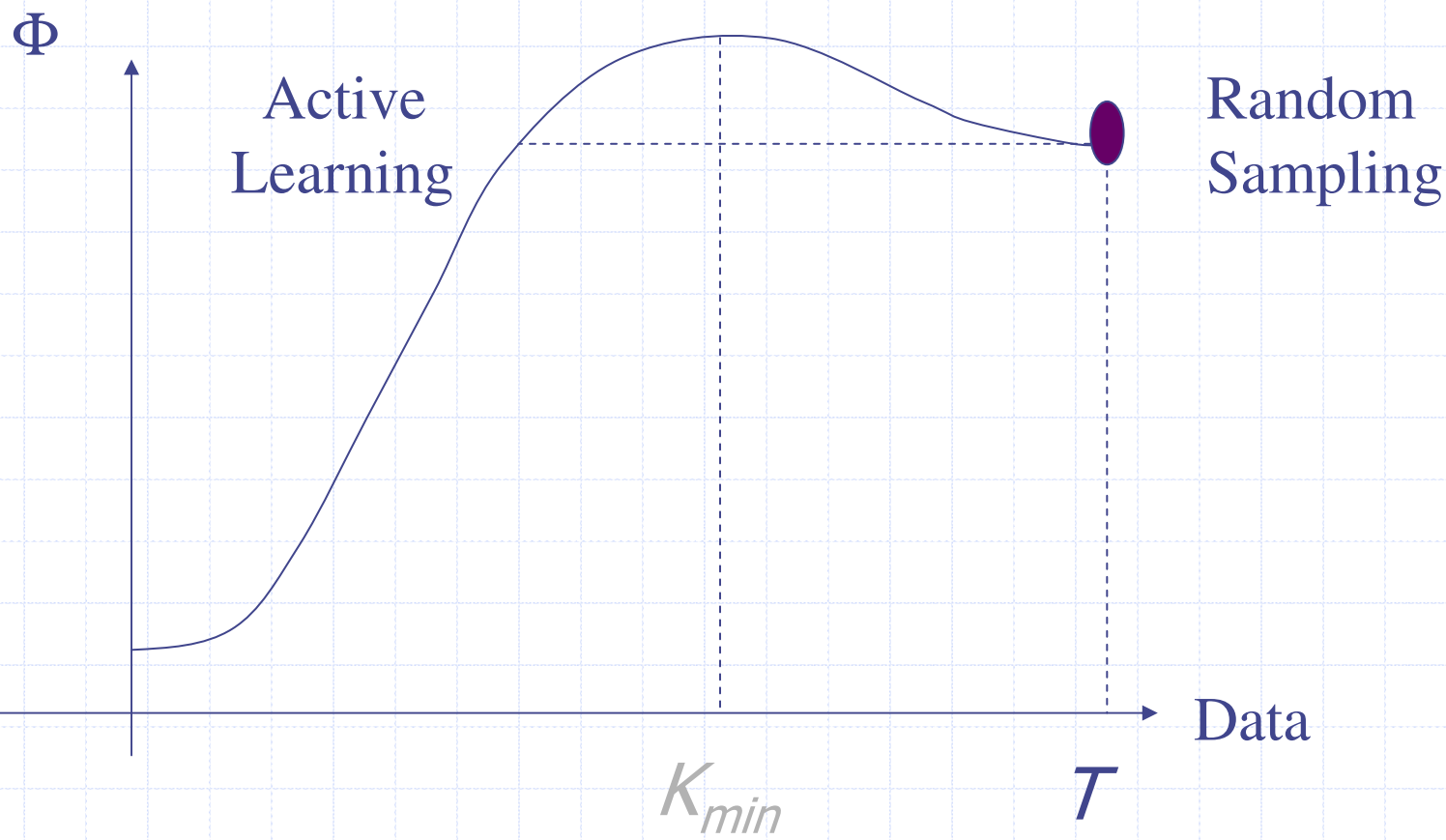
# *Informativeness* of Speech Samples



# Selecting $K_{min}$

("less is more")

- Active Learning as optimization problem



# Applications

- ◆ Classification Tasks:
  - Text Categorization
  - Call Classification
  - Part of Speech Tagging
  - Word Segmentation
  - Information Extraction
- ◆ Automatic Speech Recognition
- ◆ Syntactic/Semantic Parsing
- ◆ Machine Translation

# Outline

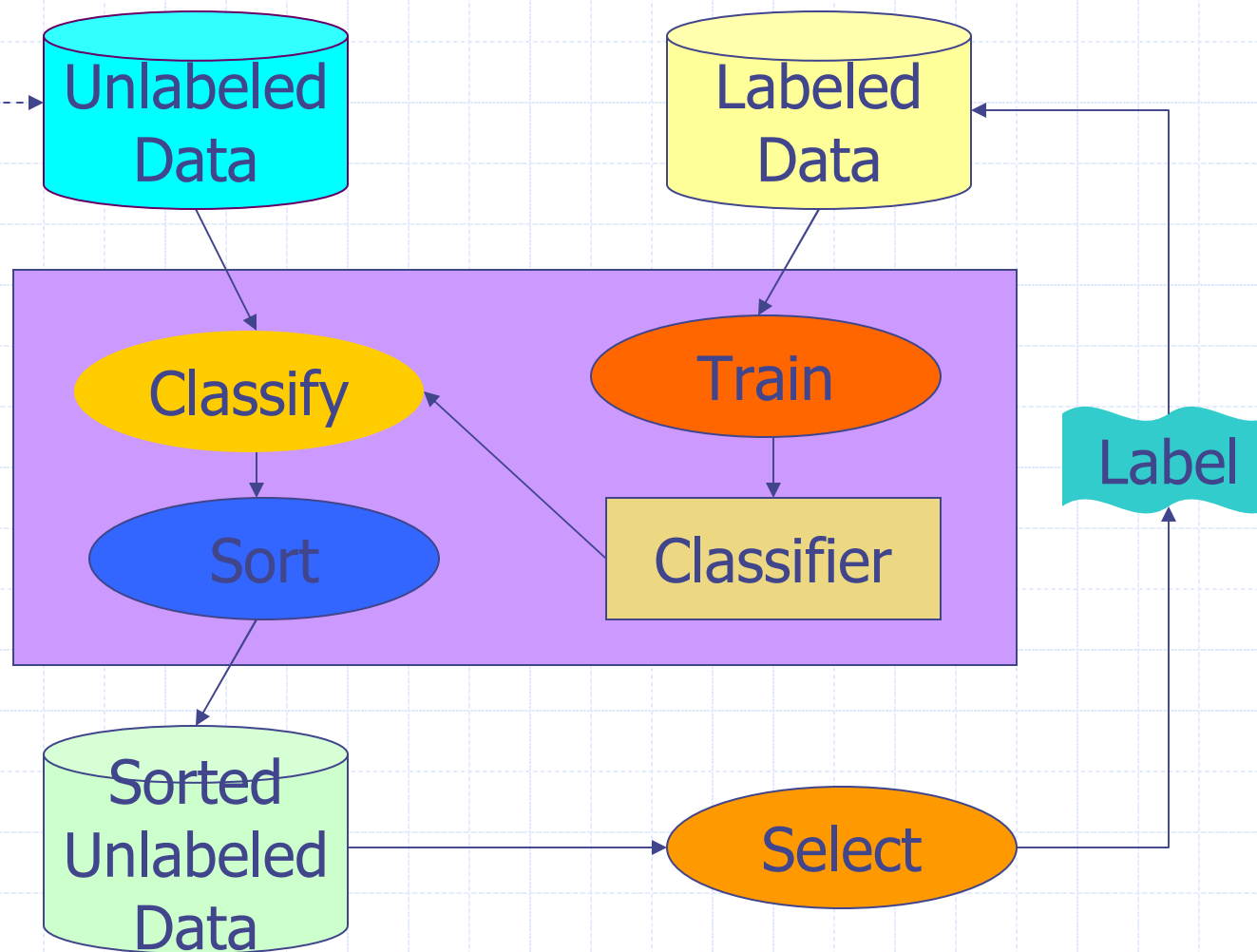
- ◆ Algorithm Dimension:
  - Passive vs. Adaptive Learning
  - Active Learning
    - ◆ Certainty-based
    - ◆ Committee-based
  - Unsupervised Learning
  - Combining Active and Unsupervised Learning

# Certainty-based Active Learning for Classification

- ◆ Train a base classifier (SVM, Boostexter, etc.)
- ◆ While (labelers/data available) do
  - Classify the pool of unlabeled data
  - Sort them according to their informativeness,  $I(\Phi)$
  - Select the top  $k$  of them
  - Label and add the selected ones to the training data
  - Re-train the classifier
  - Update the pool



# Certainty-Based Active Learning for SLU



# Classification

- ◆ *Definition:* The task of assigning objects to 2 or more classes.
- ◆ *Example Task / Unit*
  - Part-of-Speech Tagging:
    - ◆ Word (e.g. going/VBG)
  - Topic Classification (Text Categorization):
    - ◆ Document
  - Call-type Classification:
    - ◆ Utterance Transcription (often ASR output)

# Classification Methods

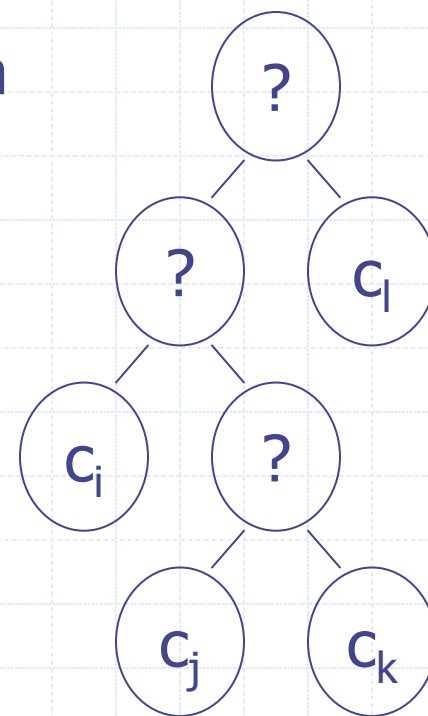
- ◆ Rule-based approaches
  - Mostly an expert writing rules for the application based on world/app knowledge
- ◆ Machine Learning approaches
  - Employing one of the machine learning algorithms (decision tree, naïve bayes, boosting, SVM, etc.) using the application data
- ◆ Hybrid approaches
  - Combining rules with data
  - Learning (probabilities of) rules from data

# Decision Trees

- ◆ Classify an object starting from the top node, testing its question, branching to the appropriate node, repeat until it is a leaf.
- ◆ Training is based on splitting criterion:
  - Typically *information gain*, which computes the reduction in uncertainty.

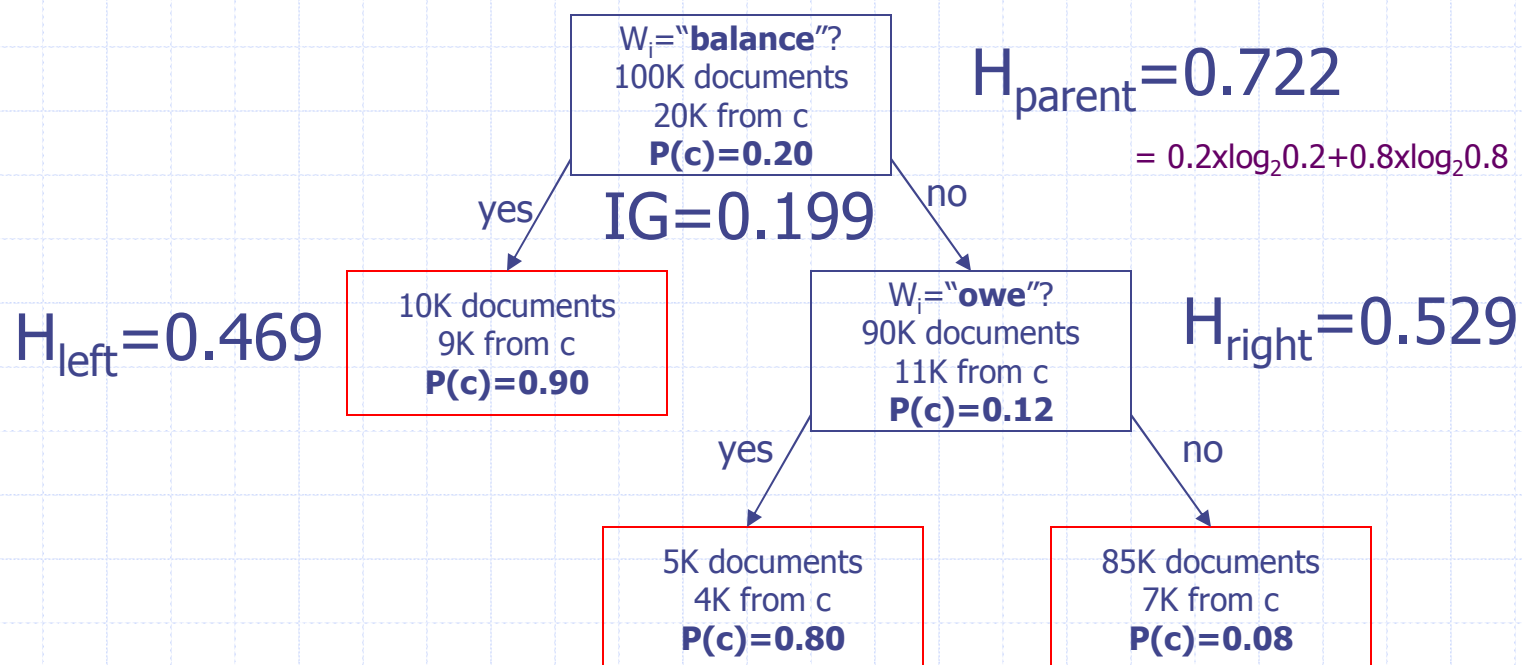
$$G(a) = H(t) - (p_L \times H(t_L) + p_R H(t_R))$$

where  $a$  is the feature, the split is to be decided,  $t_{(R|L)}$  is the distribution of the (right|left) node.



# An Example Decision Tree

- Text categorization using a binary classifier with unigram features, deciding whether the class is  $c$  (Tellme(Balance)), or not



# Naïve Bayes

◆ Using the Bayes rule:

$$\hat{c} = \arg \max_{c_i} P(c_i | o) = \arg \max_{c_i} \frac{P(o | c_i) \times P(c_i)}{P(o)} = \arg \max_{c_i} P(o | c_i) \times P(c_i)$$

where  $o$  is the object to be classified.

◆ Assuming conditional independence:

$$P(o | c_i) = P(a_1, \dots, a_n | c_j) = \prod_j P(a_j | c_i)$$

where  $a_j$  is a feature for the object  $o$ .

# An Example Naïve Bayes Classifier

- ◆ Text categorization using unigram features (*bag-of-words*)

$$\arg \max_c P(c | sent) = \arg \max_c P(sent | c) \times P(c)$$

- ◆ Sentence: "balance request"

$$P(sent | c) = P(word_1, \dots, word_n | c) = \prod_j P(word_j | c)$$

$$score_{c,sent} = P("request" | c) \times P("balance" | c) \times P(c)$$

$$P(c | sent) = \frac{score_{c,sent}}{\sum_i score_{c_i,sent}}$$

# Boosting

- ◆ Given the data  $(x_1, y_1), \dots, (x_m, y_m)$  where  $x_i \in X, y_i \in Y$
- ◆ Initialize the distribution  $D_1(i) = 1/m$
- ◆ For each iteration  $t=1, \dots, T$  do
  - Train a base learner,  $h_t$  using distribution  $D_t$ .
  - Update

$$D_{t+1}(i) = \frac{D_t(i) \times e^{-\alpha_t \times y_i \times h_t(x_i)}}{Z_t}$$

where  $Z_t$  is a normalization factor and  $\alpha_t$  is the weight of the base learner, computed using the error rate of that learner.

- ◆ The output of the final classifier is defined as:

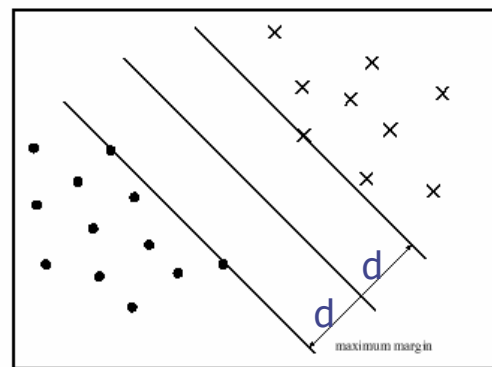
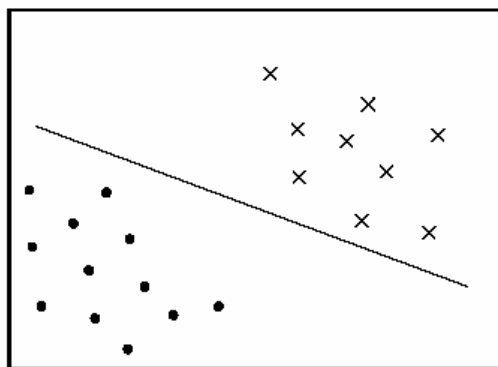
$$f(x) = \sum_{t=1}^T \alpha_t \times h_t(x)$$

$$H(x) = \text{sign}(f(x))$$



# Support Vector Machines

- ◆ Given a set of examples belonging to two different classes, the Support Vector Machine (SVM) tries to separate them with the maximum margin (Vapnik).



# Evaluation Metrics

$$\text{Accuracy} = \frac{\text{\#correctly\_classified}}{\text{\#examples}}$$

$$\text{Classification Error Rate (CER)} = 1 - \text{Accuracy}$$

- ◆ Assuming thresholding using the scores

	decision is correct	decision is incorrect
Score $\geq$ Threshold (accept)	a	b
Score $<$ Threshold (reject)	c	d

$$\text{Recall} = \frac{a}{a+c} = \frac{\text{\#correct and accepted}}{\text{\#correct}}$$

$$\text{Precision} = \frac{a}{a+b} = \frac{\text{\#correct and accepted}}{\text{\#accepted}}$$

$$\text{F-Measure} = \frac{\text{Recall} \times \text{Precision}}{\alpha \times \text{Recall} + (1 - \alpha) \times \text{Precision}}$$

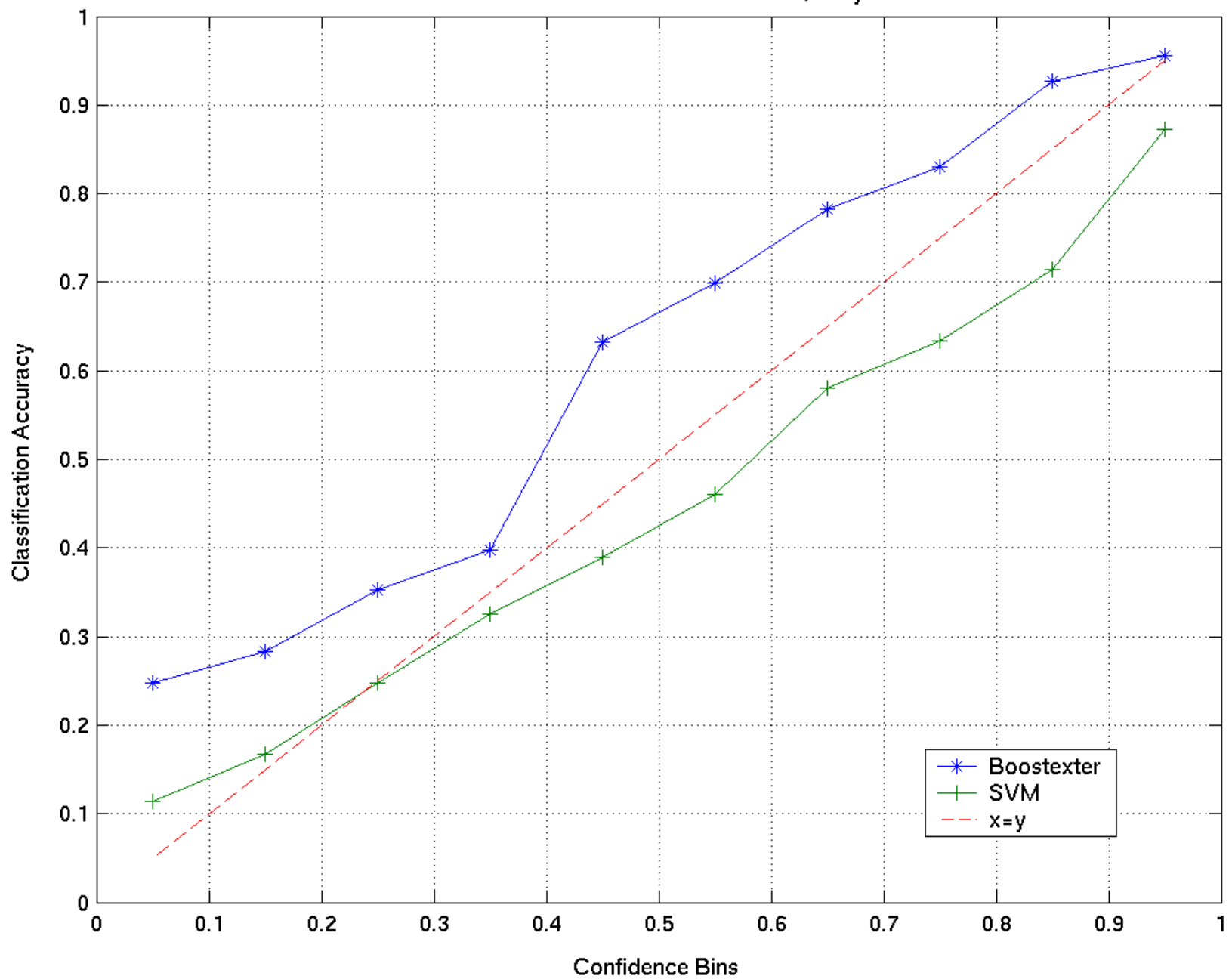
$$\text{False-Rejection} = \frac{c}{c+d} = \frac{\text{\#correct and rejected}}{\text{\#rejected}}$$

$$\text{False-Acceptance} = \frac{b}{a+b} = \frac{\text{\#wrong and accepted}}{\text{\#accepted}}$$

# Error Modeling

- ◆ Needs an informativeness measure to sort the candidate unlabeled utterances
- ◆ Use confidence scores output by the learners.
- ◆ e.g. for the Naïve Bayes classifier, it is nothing but  $P(c_i | o)$
- ◆ Alternative usages:
  - Confidence of the top scoring class (e.g.  $\max_i P(c_i | o)$ )
  - Difference in the confidences of top two scoring classes
  - $KL(P(C|X) || P(C))$

Boostexter and SVM Confidence Quality



# Selected Bibliography for Certainty-Based Active Learning

- ◆ Lewis and Catlett, ICML'94 (*Text Categorization*)
- ◆ Cohn et al., ML'94 (*Text Categorization*)
- ◆ Thompson et al., ICML'99 (*Parsing and Info. Ext.*)
- ◆ Schohn and Cohn, ICML'00 (*Text Categorization*)
- ◆ Hwa, EMNLP/VLC'00 (*Parsing*)
- ◆ Hakkani-Tür et al., ICASSP'02 (*ASR*)
- ◆ Tang et al., ACL'02 (*Parsing*)
- ◆ Sassano, ACL'02 (*Japanese Word Segmentation*)
- ◆ Tur et al., ICASSP'03 (*Call Classification*)

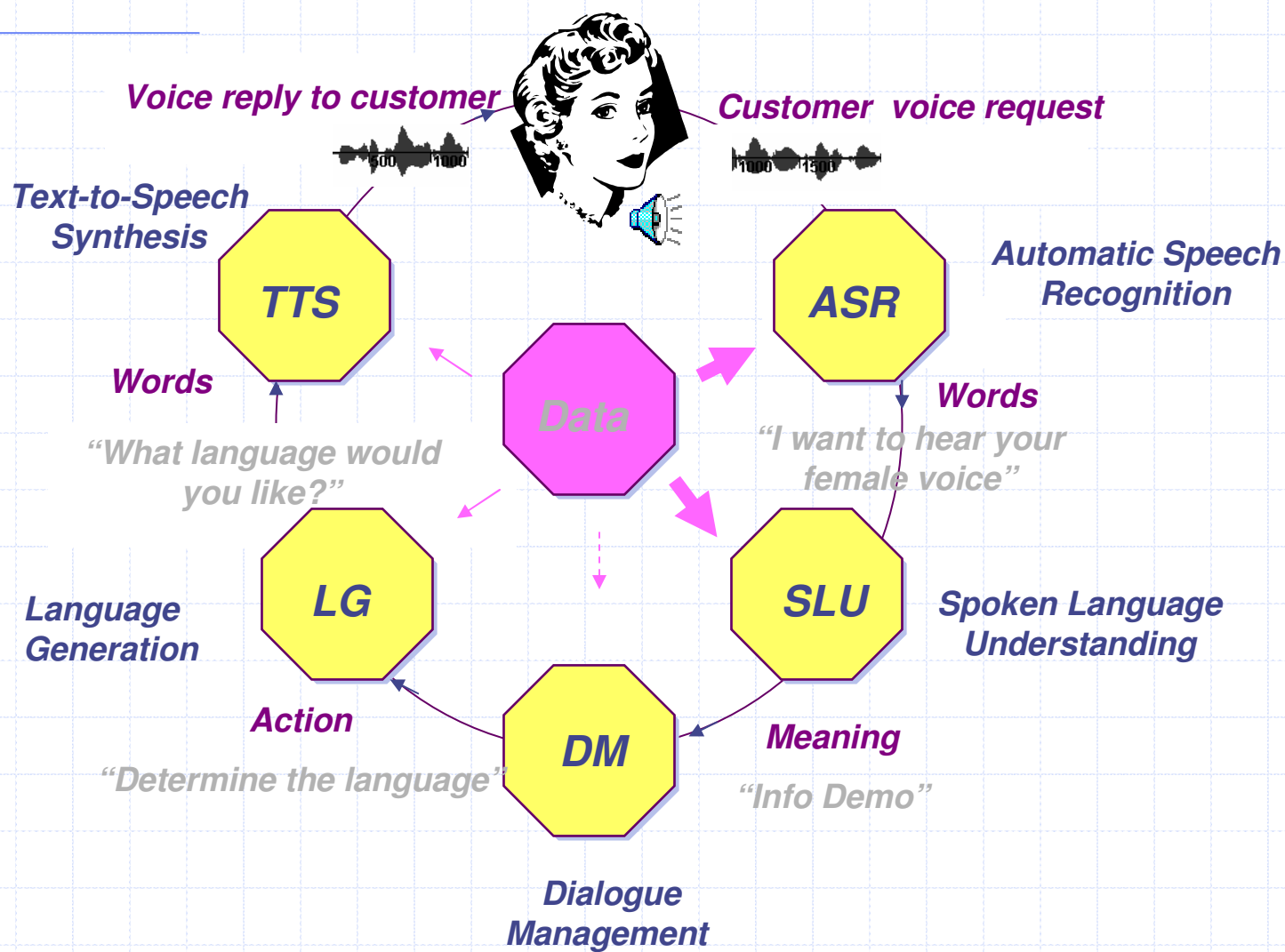
# Text Categorization

- ◆ *Lewis and Catlett ICML'94*
- ◆ AP articles, 10 classes
- ◆ Classifier: Decision Trees
- ◆ Used a simple probabilistic classifier for sample selection
- ◆ Reduced the amount of human-labeled data needed by a factor of 10.

# Parsing

- ◆ (Hwa, EMNLP/VLC, 2000)
- ◆ Criterion: Tree Entropy (TE)
  - Parse the sentence,  $s$ 
    - ◆ i.e. get multiple parse trees,  $v \in V$ , with confidences,  $p(v)$
  - Compute  $TE(s) = -\sum_{v \in V} p(v) \log p(v)$
  - Pick the sentences with high TE values
- ◆ Decreased the amount of training data needed to achieve the same performance by 36%

# Human-Machine Spoken Dialog



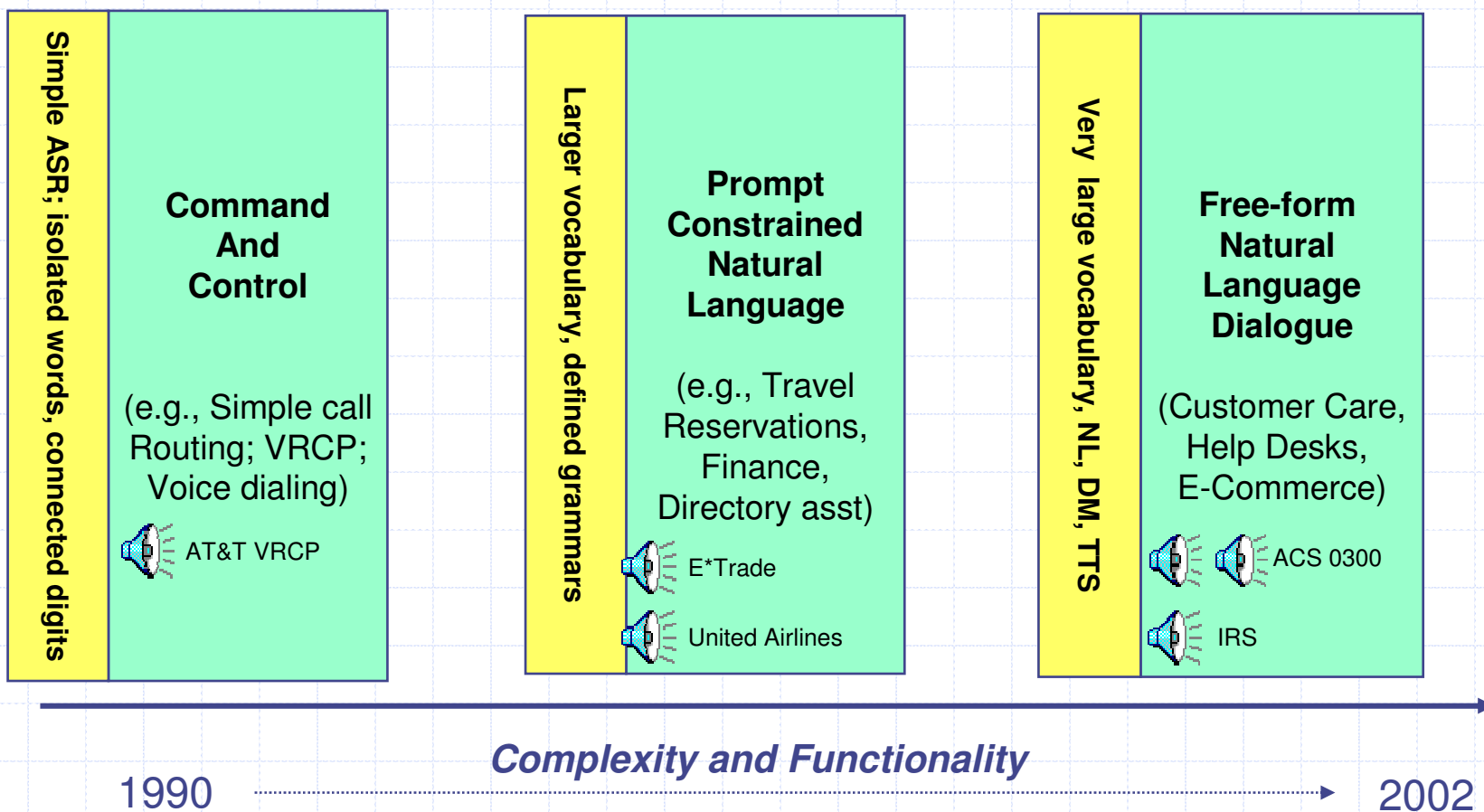


# Conversational Speech

- ◆ How May I Help You?
- ◆ hello [ uh ] [ .clrt ] excuse me I I would like I don't understand my **bill** I
- ◆ Okay. What is your question?
- ◆ what is my what
- ◆ I'm sorry, I didn't understand that. How may I help you?
- ◆ well [ eh ] I don't understand certain **items** on my **bill** like [uh] [ .lps ] it says **summary toll calls** [ .clrt ] excuse me 87 cents now I get listed for **toll calls** th- [ eh ] there's [ uh ] [ um ] [ .lps ] there's a whole list of [uh ] **toll calls** that I made why do they put this one separately...



# Voice-Enabled Services Complexity

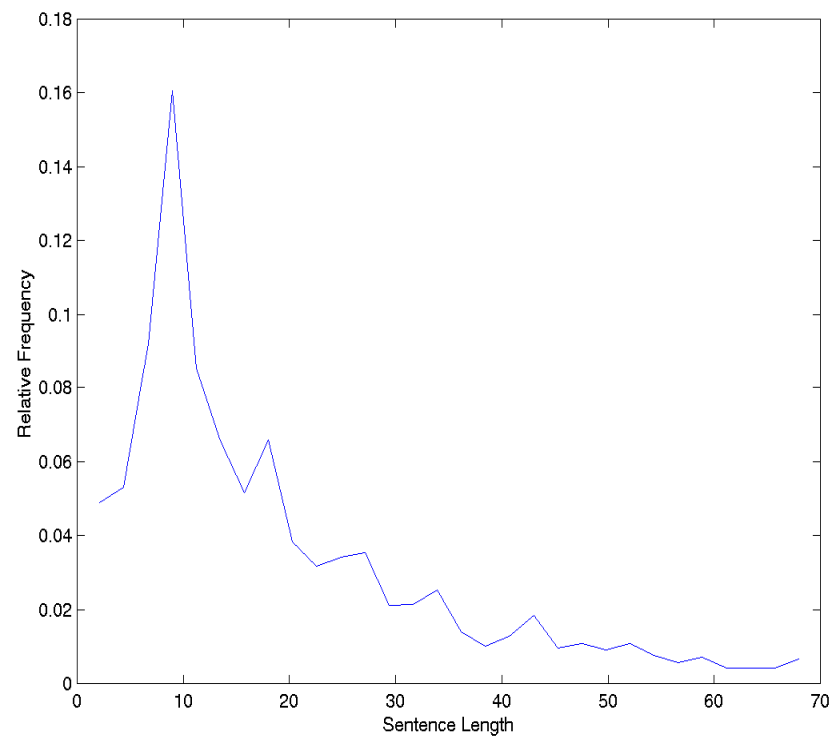
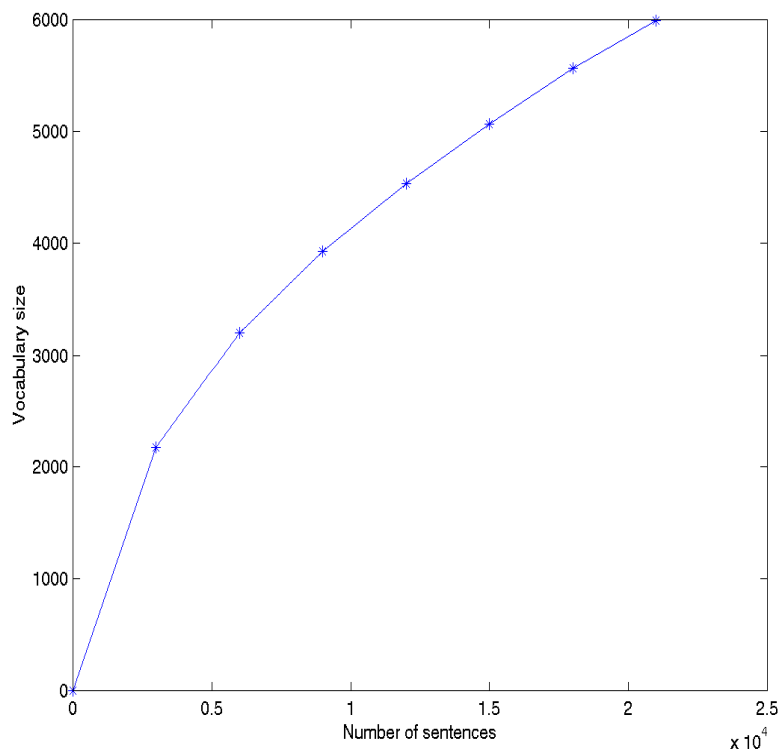


# Data Driven Learning

(Speech and Language)

- ◆ **Input:** Speech Utterance  $u_i$
- ◆ Automatic Speech Recognition
  - Gaussian Mixture Modeling (HMMs)
  - N-gram estimations ( $P(w_i | w_{i-n+1}, \dots, w_{i-1})$ )
- ◆ Semantic Associations
  - $T = \{w_i, c_j\}$
  - Feature Extraction ( $\#(f_k, c_i)$ )
    - ◆ (Salient) N-grams  $\rightarrow$  Bayes, Boosting, SVM Classifiers)
- ◆ **Output:** Model  $\lambda$ 
  - Speech recognition:  $\lambda_{ASR} : u \rightarrow w$
  - Semantic Associations:  $\lambda_{NL} : w \rightarrow c$

# Corpus Statistics

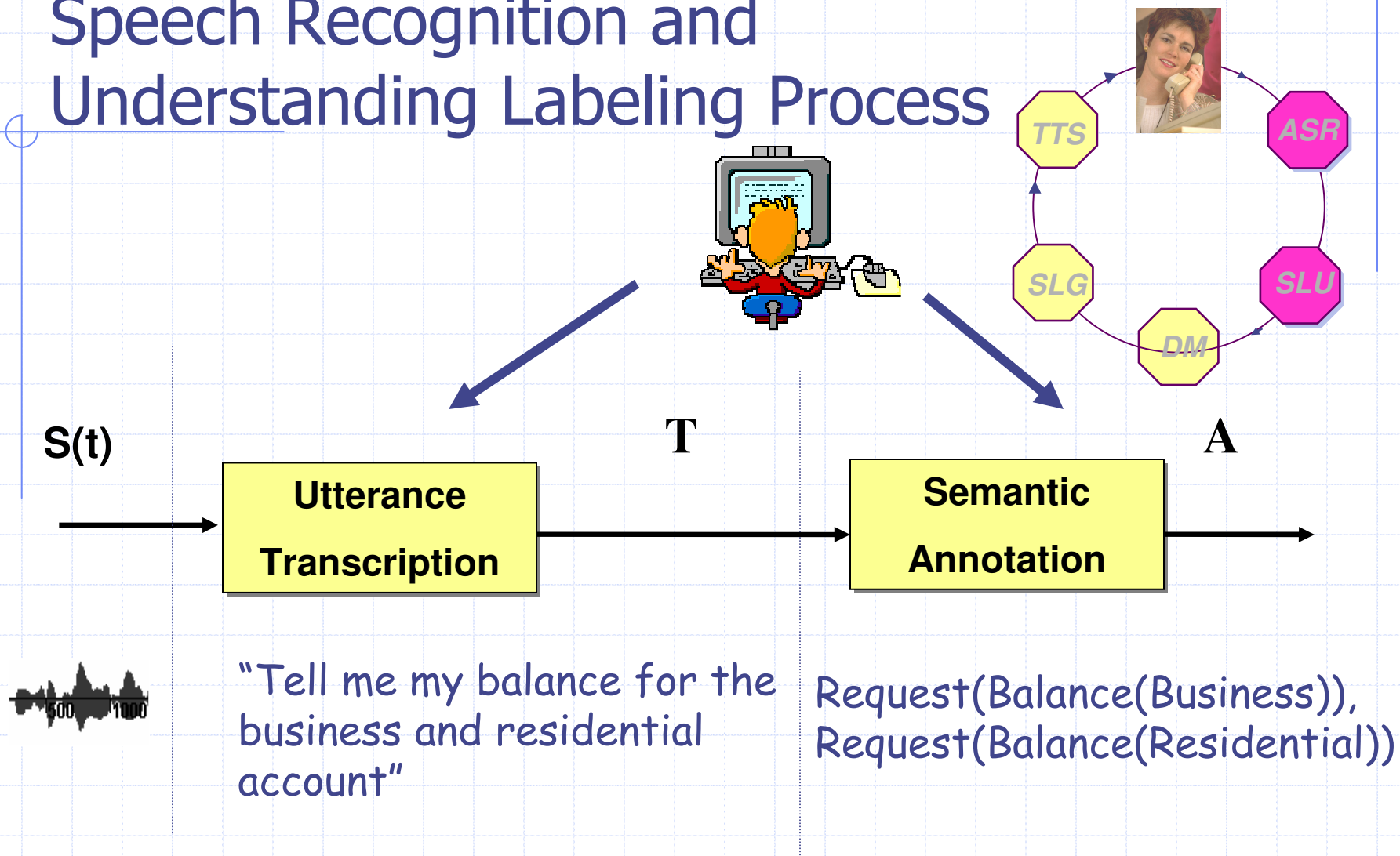


# Ways to say "question about my bill"

105 question about my bill	6 problem with my billing
63 question on my bill	6 information about my bill
57 calling about my bill	6 calling about my A T and T bill
43 talk to somebody about my bill	5 talk to someone about my phone bill
41 talk to someone about my bill	5 talk to someone about a bill
32 questions about my bill	5 talk to somebody about my billing
30 problem with my bill	5 talk to somebody about a bill
23 speak to someone about my bill	5 speak to someone in the billing
22 calling about a bill	5 speak to someone about a bill
20 calling about my phone bill	5 questions on my billing
16 questions on my bill	5 question on the bill
16 question about a bill	5 question on a bill
15 talk about my bill	5 question my bill
11 question about my phone bill	5 calling in regards to my bill
11 question about my billing	5 calling about the bill
11 discuss my bill	4 talk to someone about my telephone bill
10 speak with someone about my bill	4 talk to somebody about my account
10 calling about my billing	4 talk to billing
9 problem with my phone bill	4 speak with someone in billing
9 calling about my telephone bill	4 question about my telephone bill
8 speak to someone in billing	4 information on my bill
8 question about the bill	4 calling regarding my statement
7 speak to somebody about my bill	.....
7 speak to a billing	1 talk to someo- to someone about my moms telephone bill
7 question on my phone bill	1 question about the new A T and T billing
7 calling regarding my bill	1 calling for Bertha Fitz***** about a b- statement
7 calling concerning my bill	
6 talk to somebody in billing	
6 questions about my billing	
6 question on my billing	

Total 1083 variations in 1912 matches

# Speech Recognition and Understanding Labeling Process



## Basic Formulation of ASR

Given an acoustic observation sequence  $\mathbf{X} = X_1, X_2, \dots, X_n$  and a specified word sequence  $\hat{\mathbf{W}} = w_1 w_2 \dots w_m$ , then

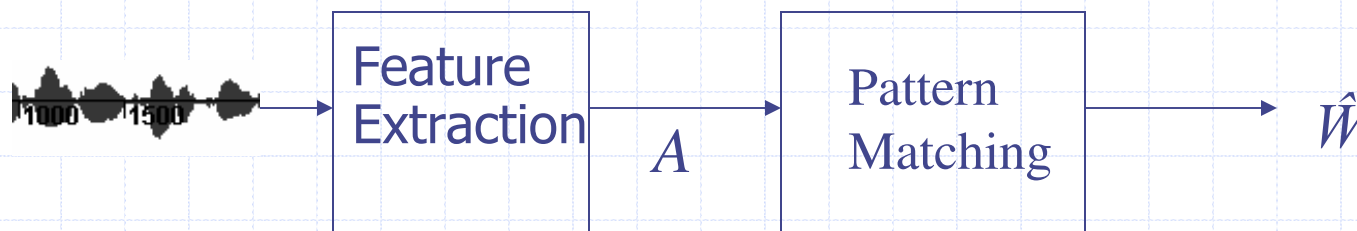
$$\hat{\mathbf{W}} = \arg \max_{\mathbf{w}} P(\mathbf{W} | \mathbf{X}) = \arg \max_{\mathbf{w}} \frac{P(\mathbf{W})P(\mathbf{X} | \mathbf{W})}{P(\mathbf{X})} = \arg \max_{\mathbf{w}} P(\mathbf{W})P(\mathbf{X} | \mathbf{W})$$

$P(\mathbf{X} | \mathbf{W})$  is the acoustic model

$P(\mathbf{W})$  is the language model

# ASR - Overview

Given the acoustic observation sequence  $A = a_1, a_2, \dots, a_m$   
 what is the most probable word sequence  $W = w_1, w_2, \dots, w_n$ ?

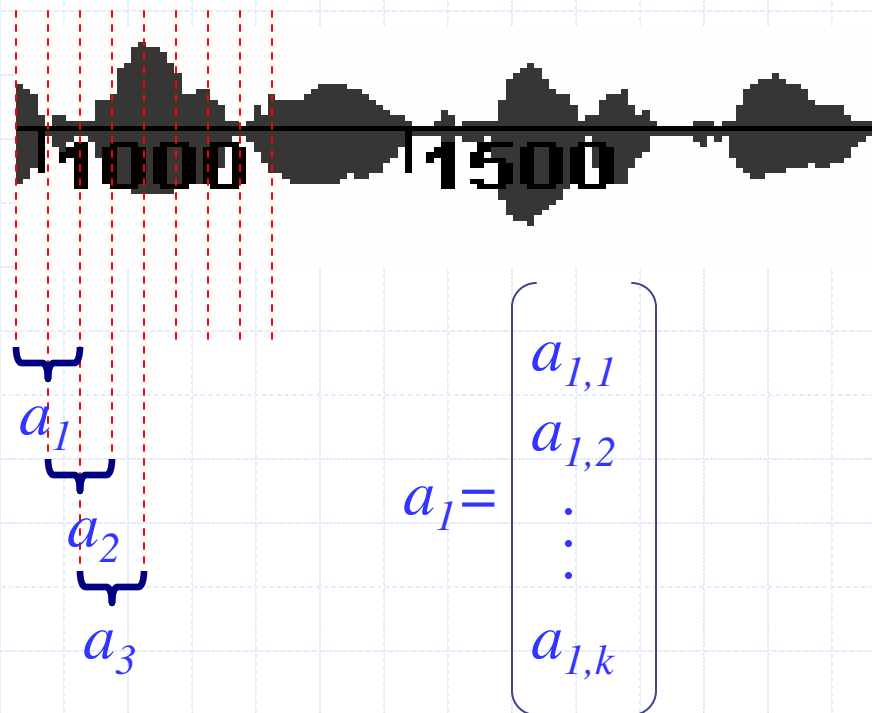


$$\begin{aligned}
 \hat{W} &= \arg \max_w P(W | A) &= \arg \max_w \frac{P(A | W) P(W)}{P(A)} \\
 & &= \arg \max_w \underbrace{P(A | W)}_{\text{Acoustic Model}} \underbrace{P(W)}_{\text{Language Model}}
 \end{aligned}$$



# Feature Extraction

- Extract features from the speech signal that are relevant for recognition.

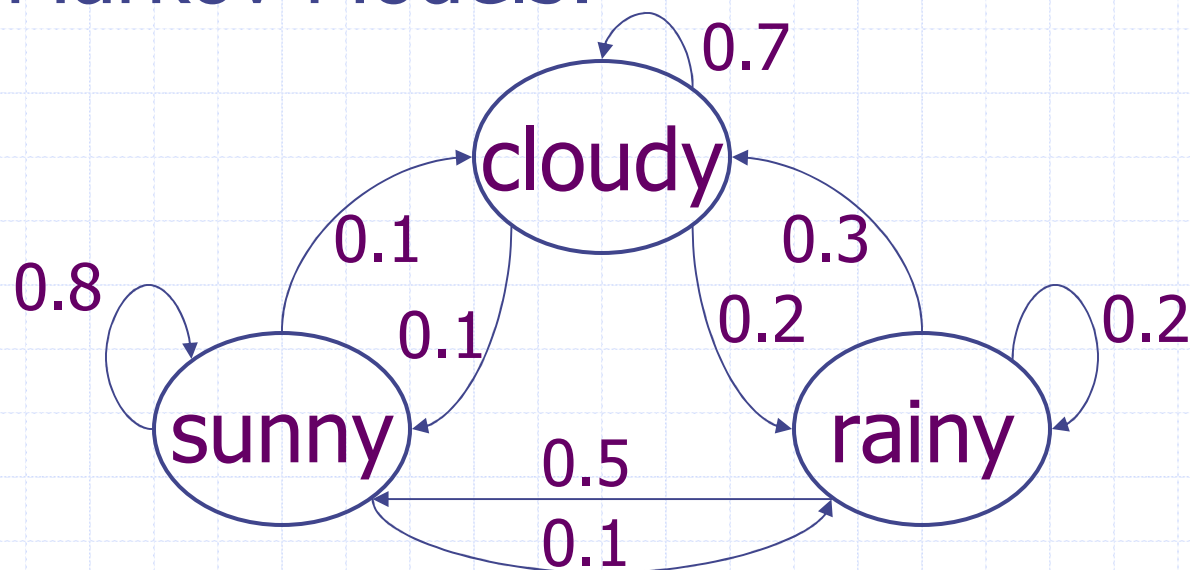


# Acoustic Modeling

- ◆  $P(A/W)$
- ◆ To extract sub-word units from the acoustic features.
- ◆ State-of-the-art systems are based on the use of Hidden Markov Models (HMMs).
- ◆ For an extensive discussion of HMMs, see Rabiner 1989.

# A Very Brief Introduction to HMMs

## ◆ Markov Models:

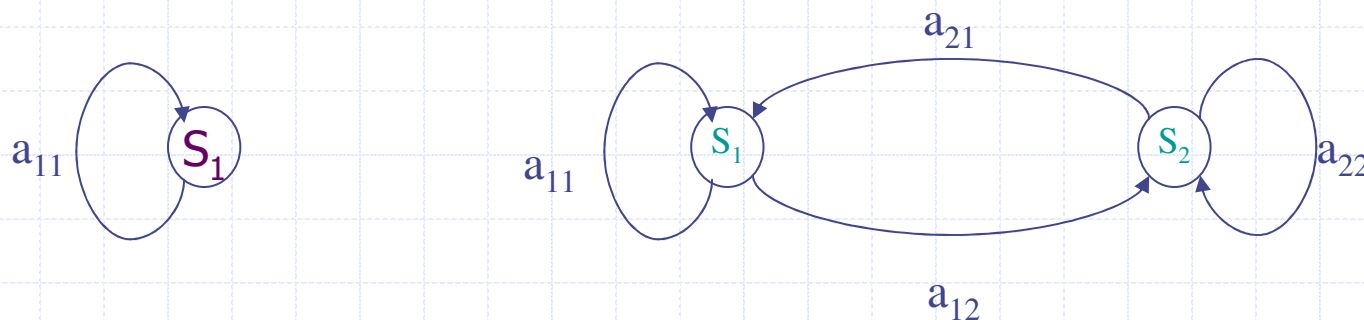


◆  $\Pi(\text{cloudy})=0.2$

◆  $O=\text{cloudy cloudy rainy sunny}$

◆  $P(O|\text{model})=0.2 \times 0.7 \times 0.2 \times 0.5=0.014$

# Hidden Markov Models



- ◆ Observations are probabilistic functions of the states.
- ◆ Additional Elements:
  - $B = \{b_i(o_j)\}$ , the observation symbol probabilities, for observing  $o_j$  at state  $i$ .
  - e.g.:  $b_1(\text{sunny}) = 0.3$

# Observation Evaluation

- ◆ What is the probability of the observation sequence,  $O$ , given the model parameters?

## 1. Initialization:

$$\alpha_1(i) = \pi_i b_i(o_1), \quad 1 \leq i \leq N$$

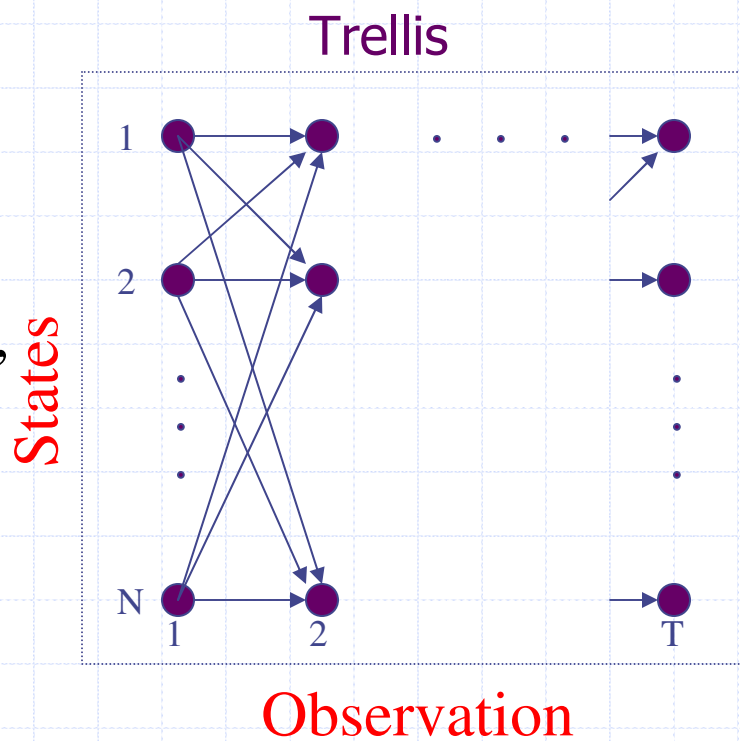
## 2. Induction:

$$\alpha_{t+1}(j) = \left( \sum_{i=1}^N \alpha_t(i) a_{ij} \right) b_j(o_{t+1}),$$

$$1 \leq t \leq T-1, \quad 1 \leq j \leq N$$

## 3. Termination:

$$P(O | \Phi) = \sum_{i=1}^N \alpha_T(i)$$



# Other HMM Problems

- ◆ **The Viterbi Algorithm:** What is the most probable state sequence, given the observation sequence,  $O$ , and model parameters  $\Phi=(A,B,\Pi)$ ?
- ◆ **The Baum-Welch Algorithm:** How do we adjust the model parameters  $\Phi=(A,B,\Pi)$ , to maximize  $P(O/\Phi)$ ,  $O=o_1, \dots, o_T$ ?

# Language Modeling

- Probability of word sequences.
- $W =$  “I wanna fly to Boston”

$$\begin{aligned}P(W) &= P(I) \times P(\text{wanna} | I) \times \dots \times P(\text{Boston} | I, \text{wanna}, \text{fly}, \text{to}) \\ &= P(I) \times P(\text{wanna} | I) \times \dots \times P(\text{Boston} | \text{to})\end{aligned}$$

- Maximum likelihood estimates

$$P(\text{Boston}) = \frac{C(\text{Boston})}{N} \quad P(\text{Boston} | \text{to}) = \frac{C(\text{to}, \text{Boston})}{C(\text{Boston})}$$

- $C(w_i, \dots, w_j)$  is the number of times word sequence  $w_i, \dots, w_j$  occurs in the training text.

# Smoothing

- ◆ What about the word sequence:  
 $W = \text{“I wanna fly to Geneva”}$   
if  $C(\text{to, Geneva}) = 0$ , as it never occurred in the training set?
- ◆ Aim: To assign a non-zero probability to previously unseen sequences.
- ◆ Robustness to unseen data.



# Smoothing - Approaches

## ◆ Add One

$$P_{smooth}(w_i) = \frac{C(w_i) + 1}{N + V} \quad P_{smooth}(w_i | w_{i-1}) = \frac{C(w_{i-1}, w_i) + 1}{C(w_{i-1}) + V}$$

## ◆ Interpolation

$$P_{smooth}(w_i | w_{i-1}) = \lambda \times P(w_i | w_{i-1}) + (1 - \lambda)P(w_i)$$

## ◆ Back-off

$$P_{smooth}(w_i | w_{i-1}) = \begin{cases} P(w_i | w_{i-1}), & \text{if } C(w_{i-1}, w_i) > 0 \\ \alpha \times P(w_i), & \text{otherwise} \end{cases}$$

# Adaptation

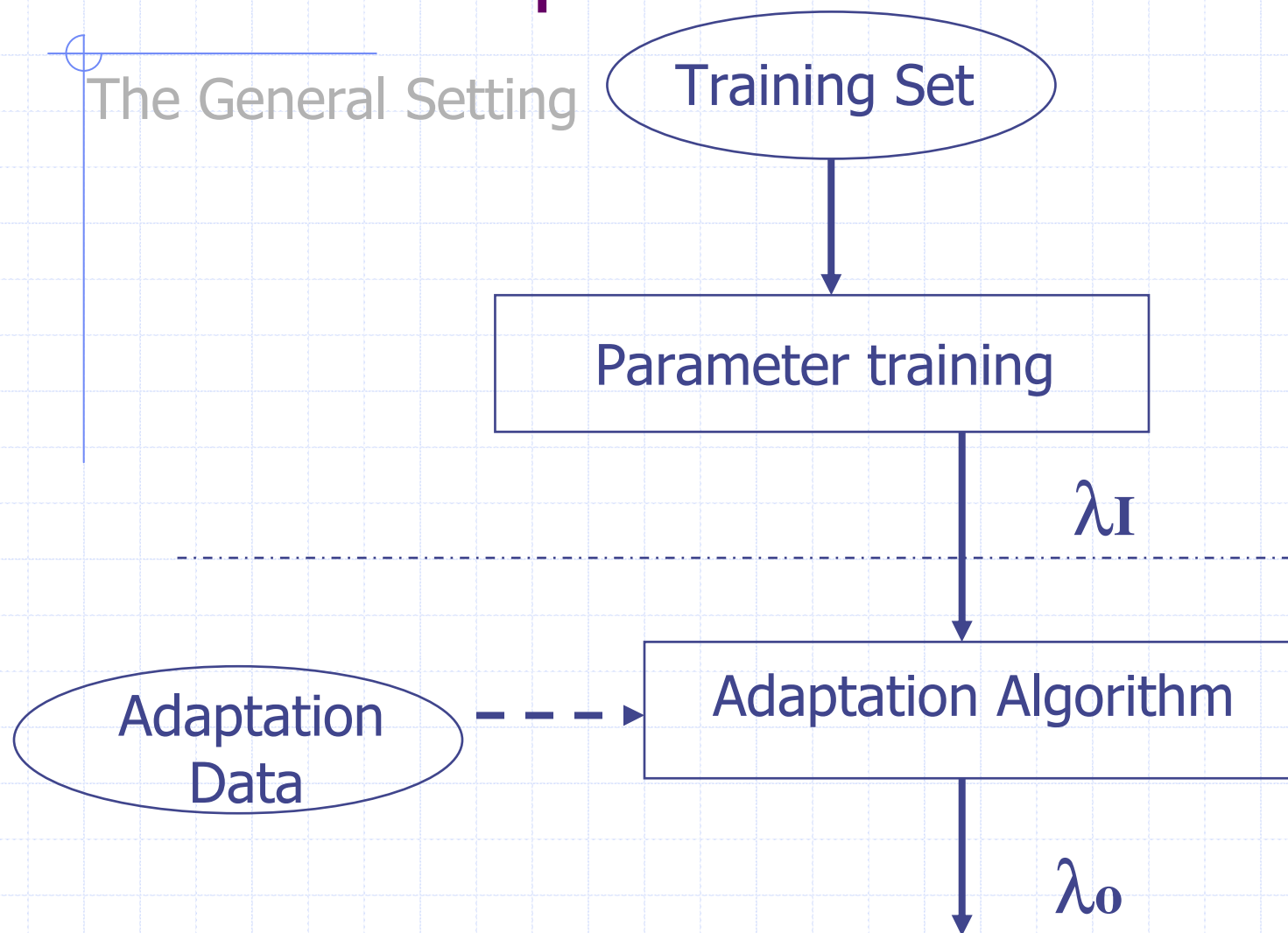
◆ Robustness to mismatched conditions, like variations in the:

- Microphone
- Environment noise
- Speaker
- Topic, etc.

e.g.: Speaker dependent versus speaker independent systems.

# Model Adaptation

The General Setting



# Adaptation Schemes

Example: Language Modeling

## ◆ Interpolated Model

$$P(w_i | h) = \alpha(h) P_I(w_i | h) + (1 - \alpha(h)) P_A(w_i | h)$$

## ◆ Cache Language Models

$$P_{cache}(w_i | w_{i-n+1} \dots w_{i-1}) = \lambda_c P_s(w_i | w_{i-n+1} \dots w_{i-1}) + (1 - \lambda_c) P_{cache}(w_i | w_{i-2} w_{i-1})$$

# Acoustic Model Adaptation

## ◆ Maximum a Posteriori (MAP)

- Consider also the prior distribution for the parameters of the model.

$$\hat{\Phi} = \arg \max_{\Phi} P(\Phi | W) = \arg \max_{\Phi} P(W | \Phi)P(\Phi)$$

- Useful when the adaptation data is limited.

## ◆ Maximum Likelihood Linear Regression (MLLR)

- A linear transformation of the model parameters are estimated.

# Language Model Adaptation

## ◆ Cache-based Language Models

$$P(w_i | w_{i-1}) = \lambda \times P_{cache}(w_i | w_{i-1}) + (1 - \lambda) \times P_{global}(w_i | w_{i-1})$$

- $P_{cache}(w_i/w_{i-1})$  is estimated from a cache, which contains the most recently dictated words.

## ◆ Topic Adaptation

- Build topic dependent language models from the topic clusters.
- Interpolate the topic dependent models.

## ◆ Dialog state dependent language models

- Build a state dependent model using the previous responses to the current” prompt.

# ASR - Evaluation

## ◆ Word Error Rate (WER)

$$\text{WER} = \frac{\# \text{ Ins} + \# \text{ Del} + \# \text{ Subs}}{\# \text{ Ref. Words}}$$

REF: i'd like to review my services that i have

HYP: i'd like to have a review the services i have

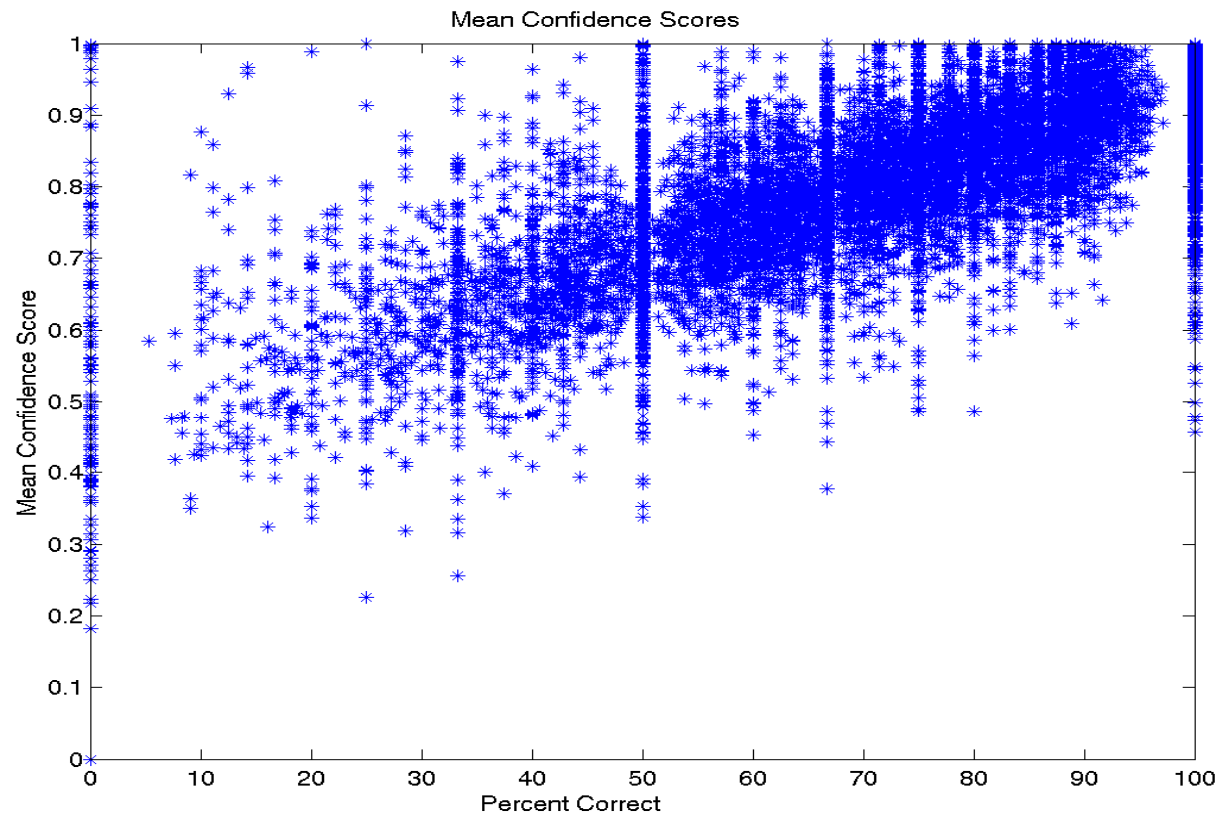
REF:	i'd	like	to	****	*	review	MY	services	THAT	i have
HYP:	i'd	like	to	HAVE	A	review	THE	services	****	i have
				Insertions	Insertions		Substitution		Deletion	

## ◆ Word Accuracy (WA)

$$\text{WA} = 1 - \text{WER}$$

# ASR Confidence Scores

- Probability of utterance  $u_i$  being correctly recognized by current model  $\lambda$





# ASR Confidence Scores

- ◆ Mark each phone/word/utterance with a score of confidence.
- ◆ ASR word confidence scores for
  - Selective Sampling for Active Learning
  - Probability Estimation for Unsupervised Learning
  - Selective Sampling for Unsupervised Learning
- ◆ Word confidence scores and word confusion networks (sausages) for improving
  - natural language understanding
  - machine translation
  - named entity extraction

# Likelihood Ratio Tests

- ◆ Likelihood ratio (LR) test (Lleida and Rose, 1996)

$$LR(A, \lambda^c, \lambda^a) = \frac{P(A | \lambda^c)}{P(A | \lambda^a)} \begin{matrix} > & H_0 \\ < & H_1 \end{matrix} \tau$$

- A: a sequence of feature vectors
- $\lambda^c$ : target model
- $\lambda^a$ : alternative model
- ◆ Word level confidence scores are obtained by combining LR scores.
- ◆ Requires training.

# Word Graph Based Approaches

- ◆ Word-Graph-based Approaches
  - Derived from the lattice output of ASR.
  - No need for training
- ◆ ASR lattices → Sausages (word confusion networks)
  - (Mangu, *et al.*, 2000)
  - Word posterior probability estimates on the sausages → word confidence scores
- ◆ (Hakkani-Tür and Riccardi, 2003)

# Hybrid Approaches

## ◆ Approaches that use:

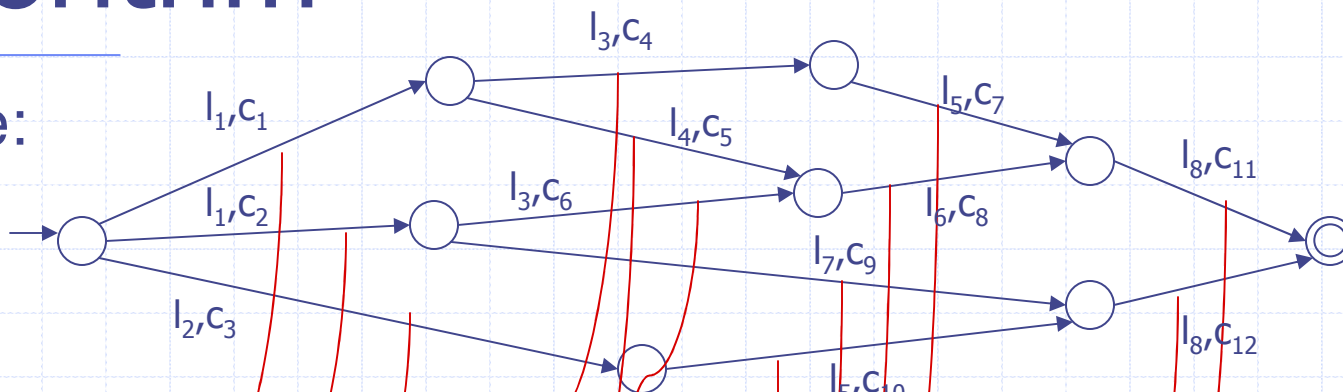
- Acoustic features
- Word lattice features
- Linguistically motivated features

to come up with word confidence scores  
(*eg.* Zhang and Rudnicky, 2001)

## ◆ Requires training.

# Algorithm

Lattice:



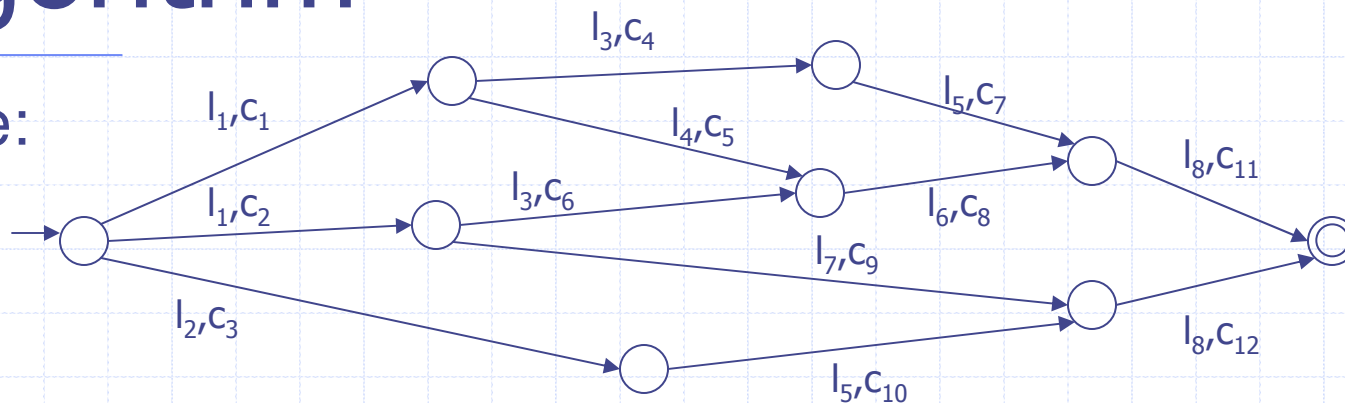
Pivot:



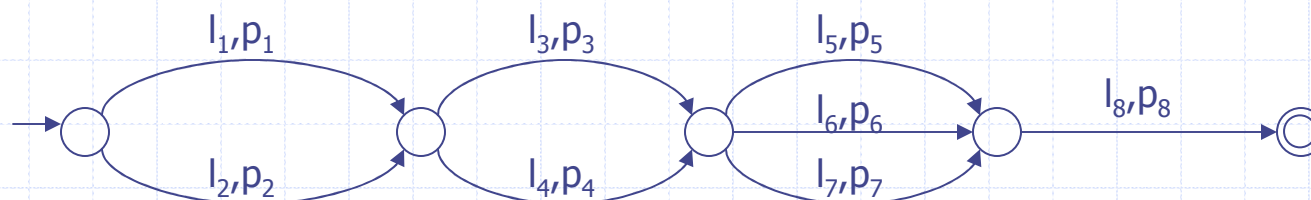
$l_i$  : labels  
 $c_i$  : costs  
 $p_i$  : posterior probabilities

# Algorithm

Lattice:



Pivot alignment:



$l_i$ : labels  
 $c_i$ : costs  
 $p_i$ : posterior probabilities

# Algorithm

**Compute** the posterior probabilities of all transitions on the lattice

**Select** a path as a baseline  
[random/best/longest path]

**For all transitions** in the lattice,

Find the most overlapping position (wrt start and ending state times) on the pivot/baseline

If a transition with same label already occurs there, increment its posterior

Otherwise, insert a new transition to the pivot/baseline

# Algorithm Details

- ◆ Time information is not necessary, but beneficial.
    - Time info is estimated as approximate state location.
  - ◆ The labels on arcs can be words, phones, semantic tags, etc.
    - E.g. slot confidence scores
  - ◆ Algorithmic complexity:  $O(N * M)$ 
    - MEMORY: smaller than word lattices (7% of lattices).
    - TIME: much faster than sausage computation of Mangu et al. (2000), which runs in  $O(N^3)$ .
- $N$ : Number of arcs in the lattice
- $M$ : Number of arcs on the best/longest/random path.



# Evaluation of Confidence Scores

- ◆ Test Set: 2,174 utterances (~31K words) from AT&T HMIHY?<sup>SM</sup> spoken dialog system test data.
- ◆ Baseline: Best Path
- ◆ Select a threshold, accept as correct recognition if confidence score is bigger than threshold.
- ◆ False Acceptance Rate (*FA*)

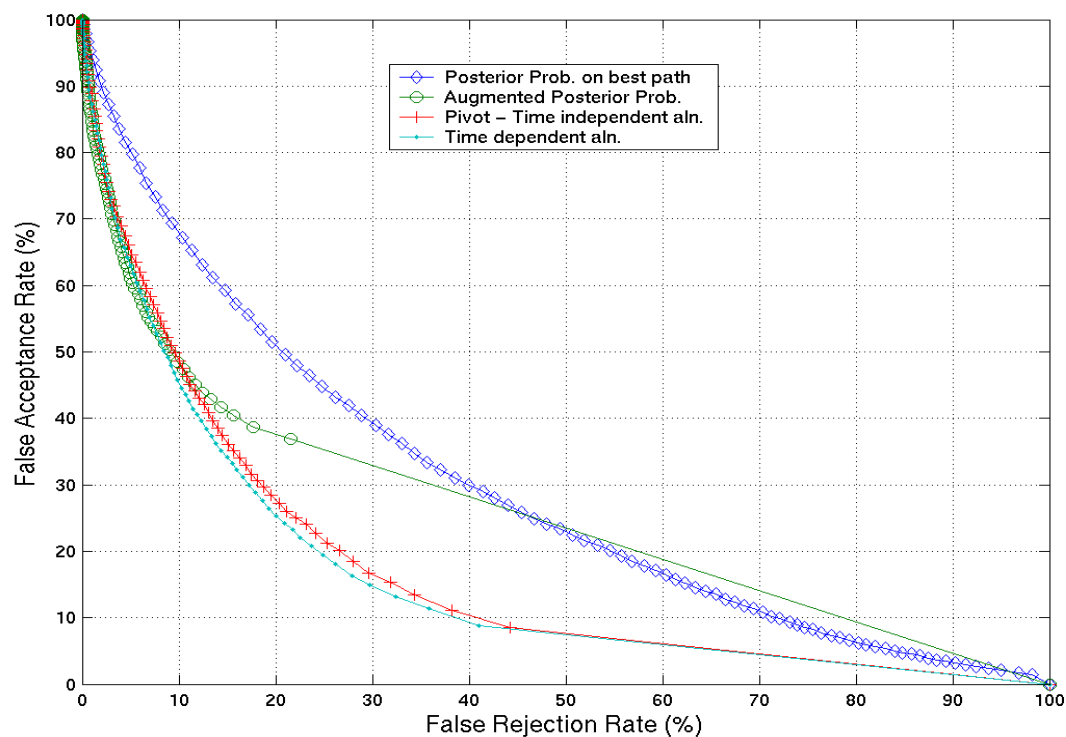
$$FA = \frac{\text{\# of misrecognized words that are accepted}}{\text{\# of words that are accepted}} \times 100\%$$

- ◆ False Rejection Rate (*FR*)

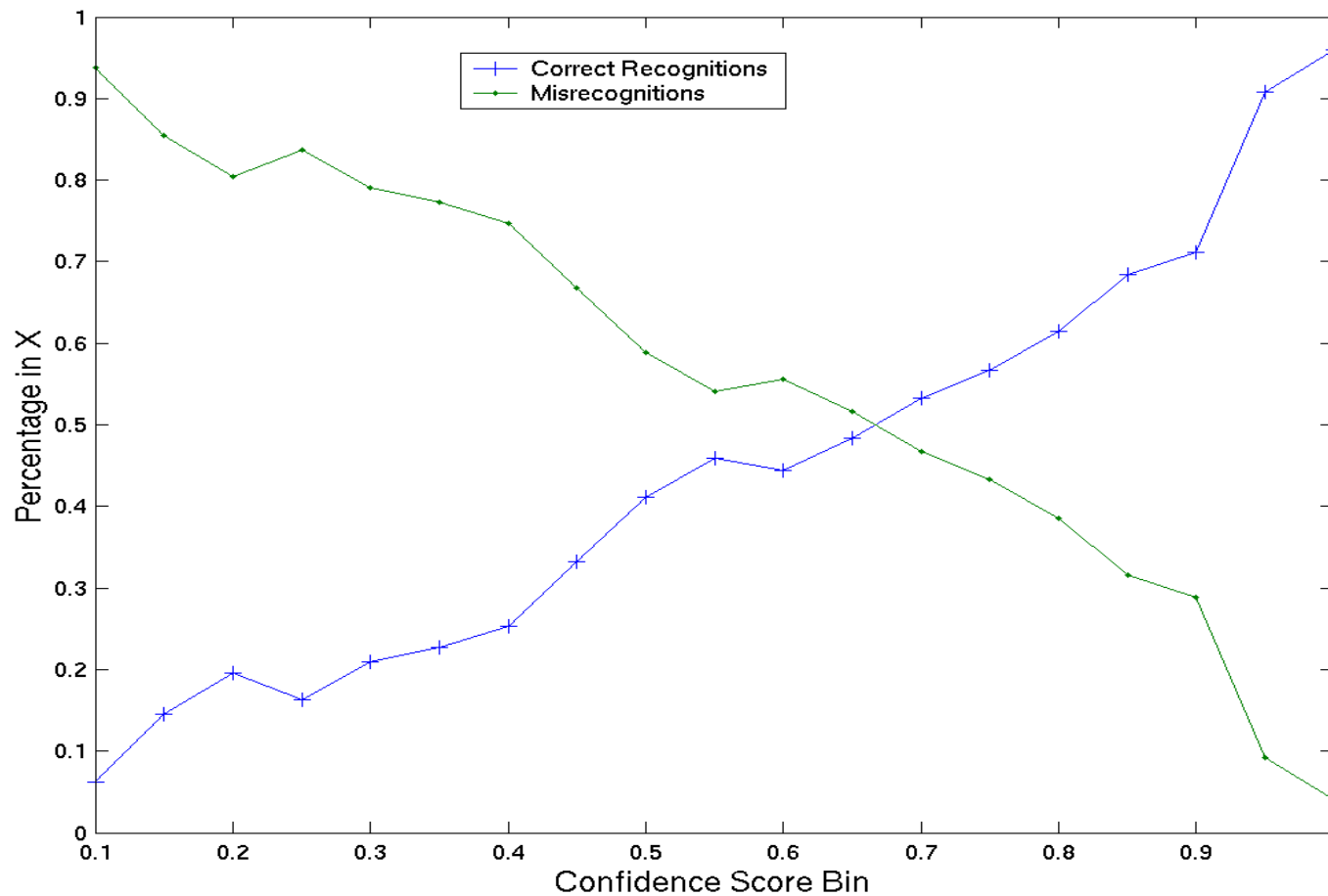
$$FR = \frac{\text{\# of correctly recognized words that are rejected}}{\text{\# of words that are rejected}} \times 100\%$$

# False Acceptance vs. False Rejection

- ASR 1-best posteriors
- Augmented ASR 1-best posteriors (using word lattices)
- Pivot alignments using time
- Pivot alignments without time



# Percent Correct/Misrecognition





# Active Learning for Automatic Speech Recognition

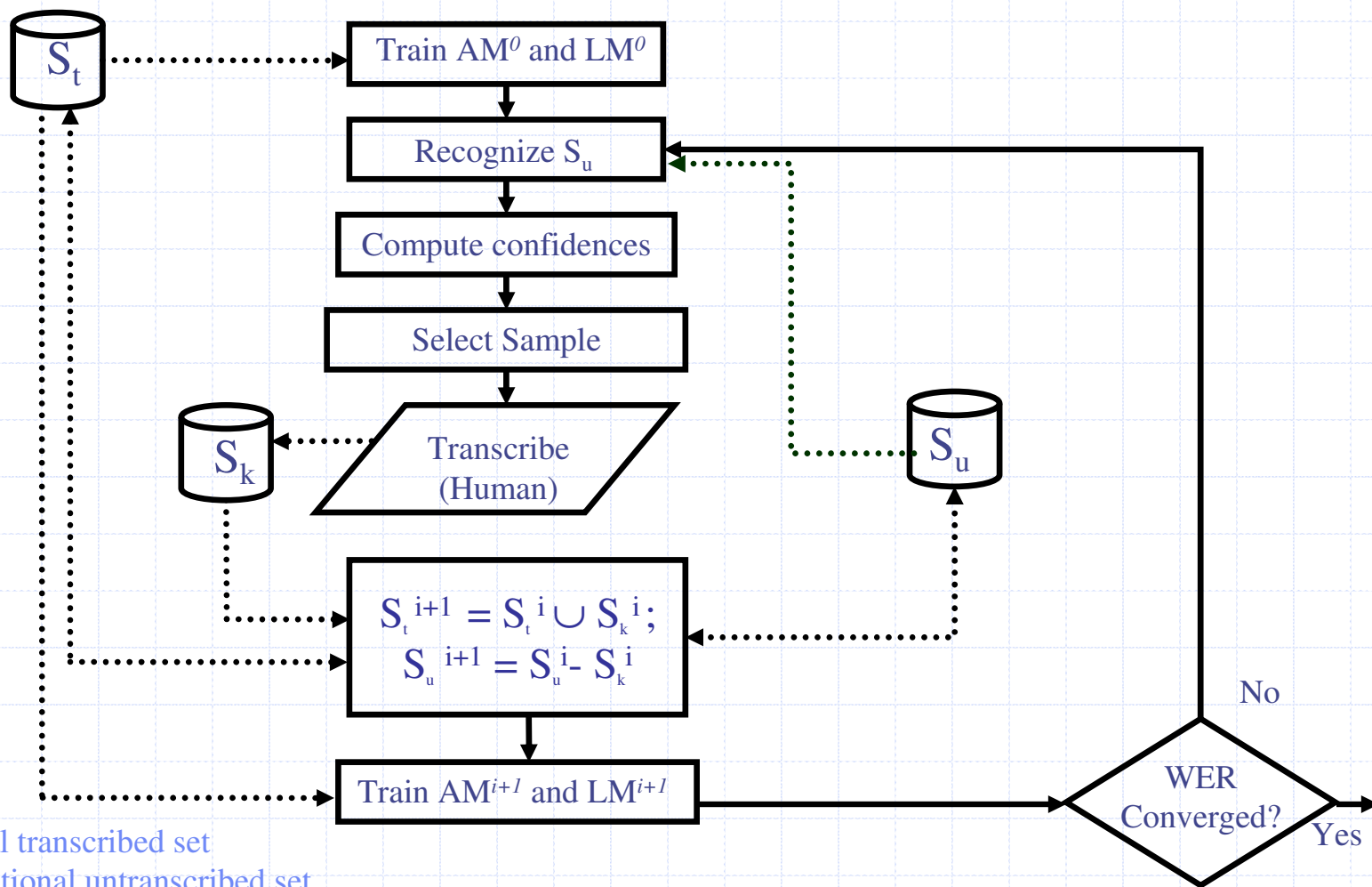
- ◆ (Hakkani-Tür et al., ICASSP 2002)
- ◆ (Kamm, Ph.D. Thesis, 2004)

# Active Learning for ASR

## ◆ Goals:

- Reduce the amount of transcribed data needed without reducing accuracy.
- Optimize the performance using a given set of transcribed data.

# Algorithm



$S_t$ : Initial transcribed set  
 $S_u$ : Additional untranscribed set  
 $S_k$ : Intermediate set to be transcribed

# Utterance Scores

- ◆ The algorithm is independent of the way utterance scores are computed, as long as they are good quality.
- ◆ We compute utterance scores, using word confidence scores.  $U = w_1, \dots, w_k$

- Mean confidence score

$$c(U) = \frac{1}{k} \sum_{i=1}^k c(w_i)$$

- Voting

$$c(U) = \frac{1}{k} \sum_{i=1}^k f(c(w_i)) \text{ where } f(c(w_i)) = \begin{cases} 1, & c(w_i) > \text{threshold} \\ 0, & \text{otherwise} \end{cases}$$

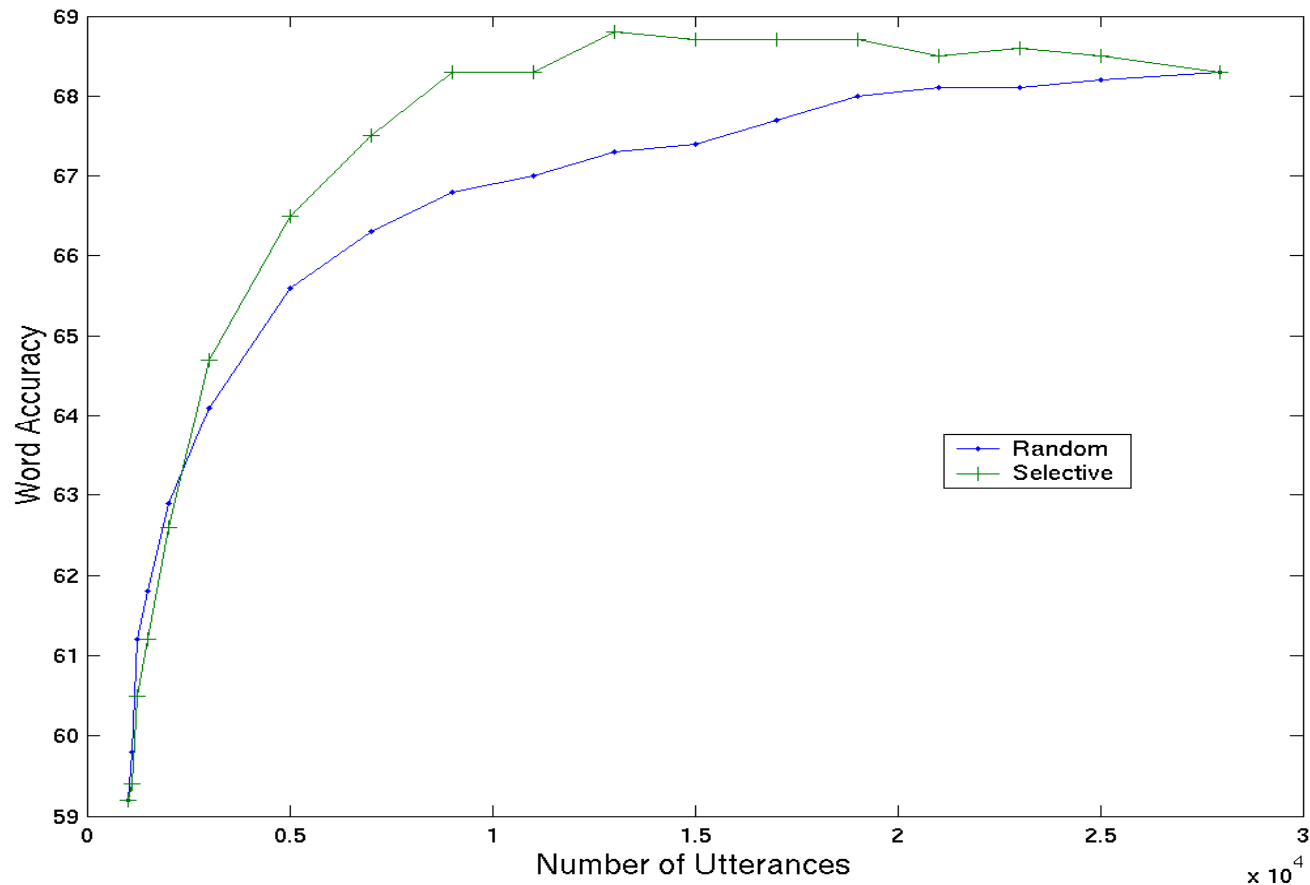
# Active Learning Expt(1)

- ◆ Data collected from HMIHY?<sup>SM</sup> field trials
  - ~100K utterances
- ◆ All utterance turns (80 prompts)
- ◆ Bootstrap data for LM and scoring
  - HM data collection
- ◆ Data is pooled and sampled
- ◆ No time ordering constraint

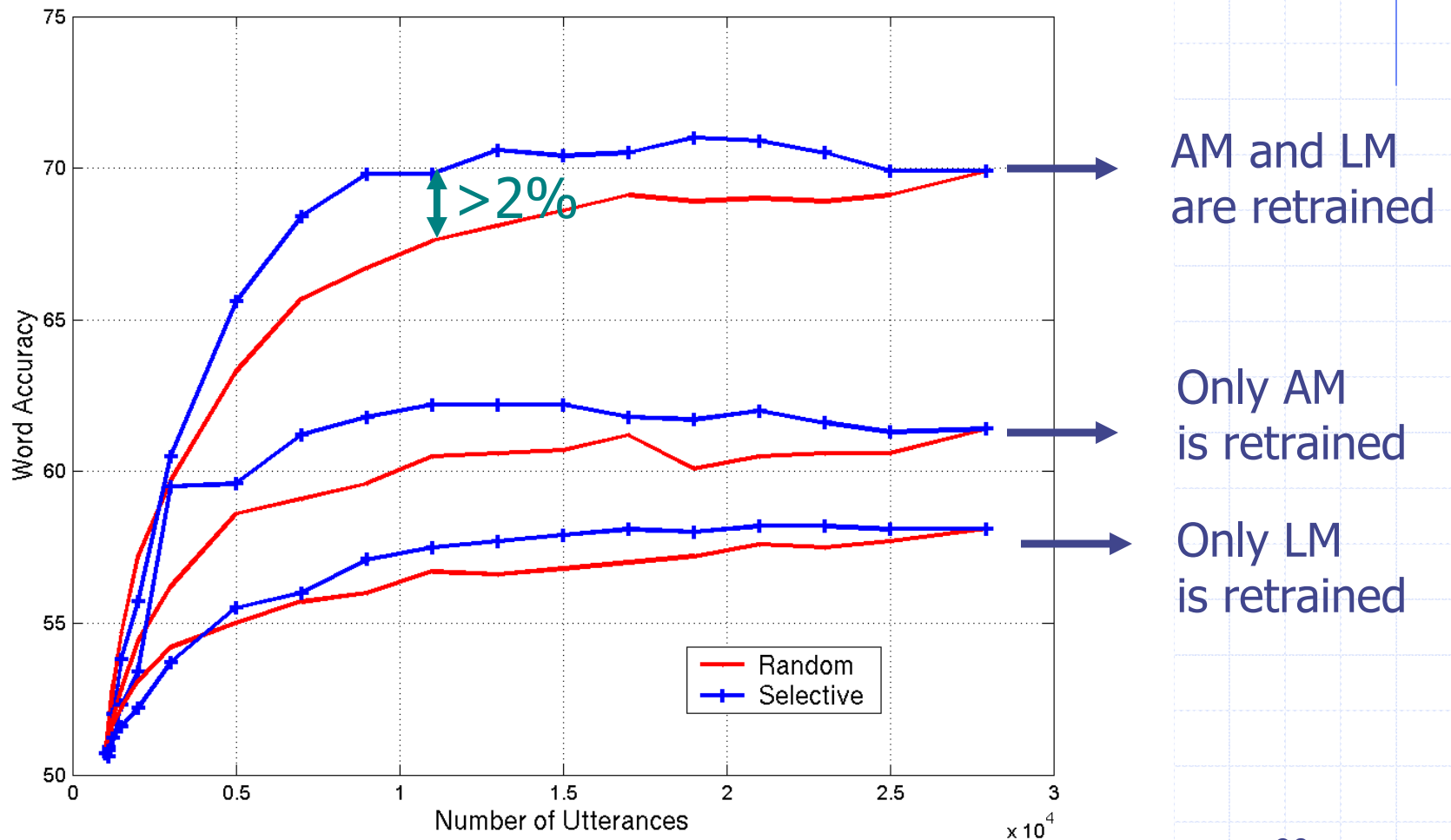


# Active Learning Expt(1)

- Halve data size requirement for a given  $\Phi$
- Improve over asymptotic performance

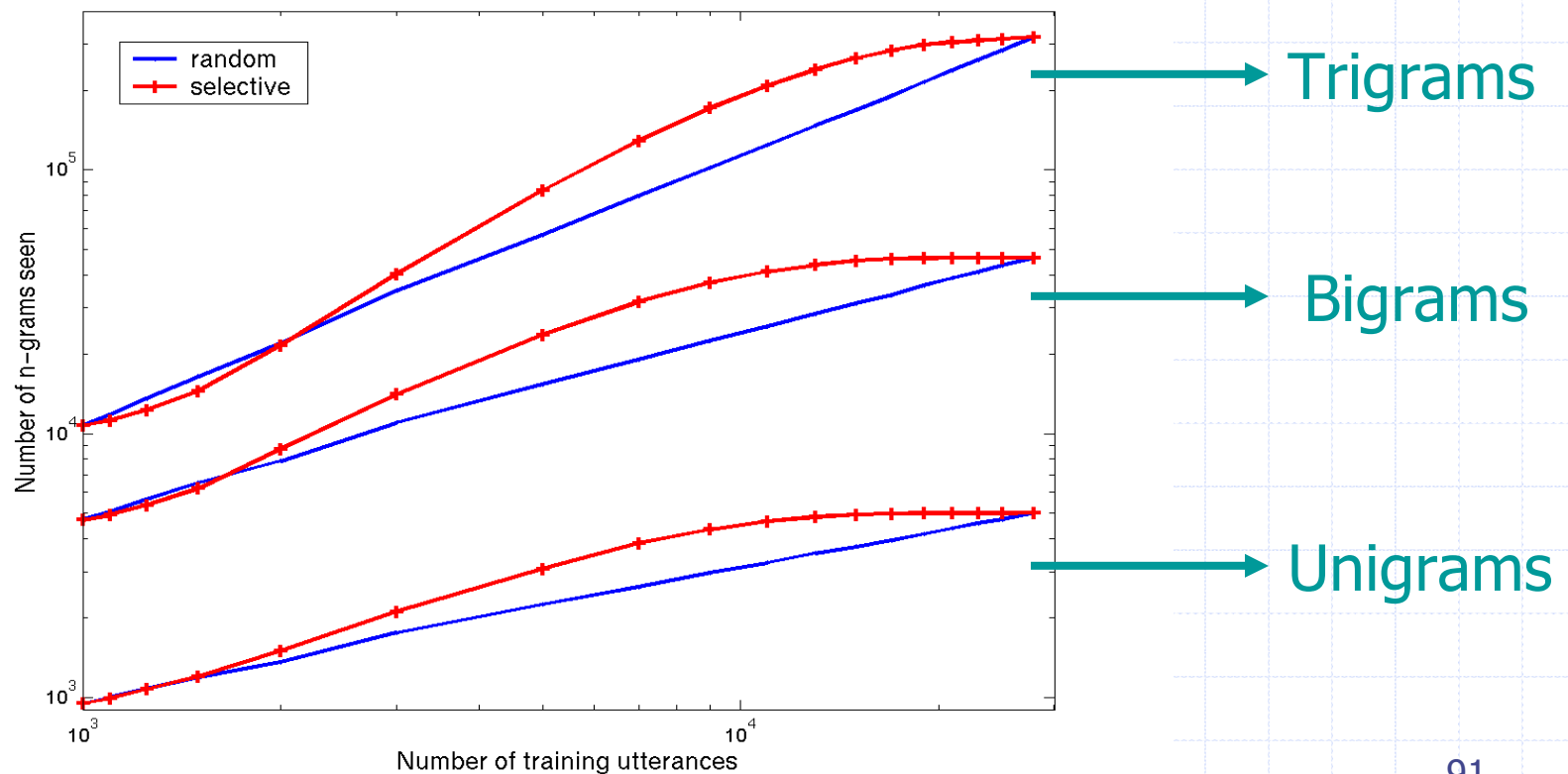


# Active Learning Expt (2)



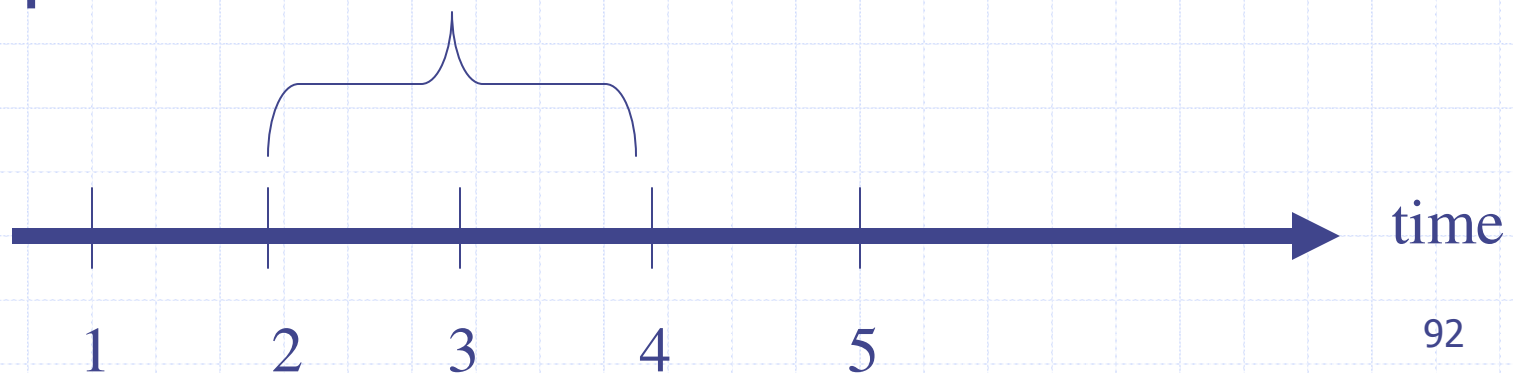
# Why does Active Learning work?

- Language modeling:
  - discover new words
  - discover new n-grams

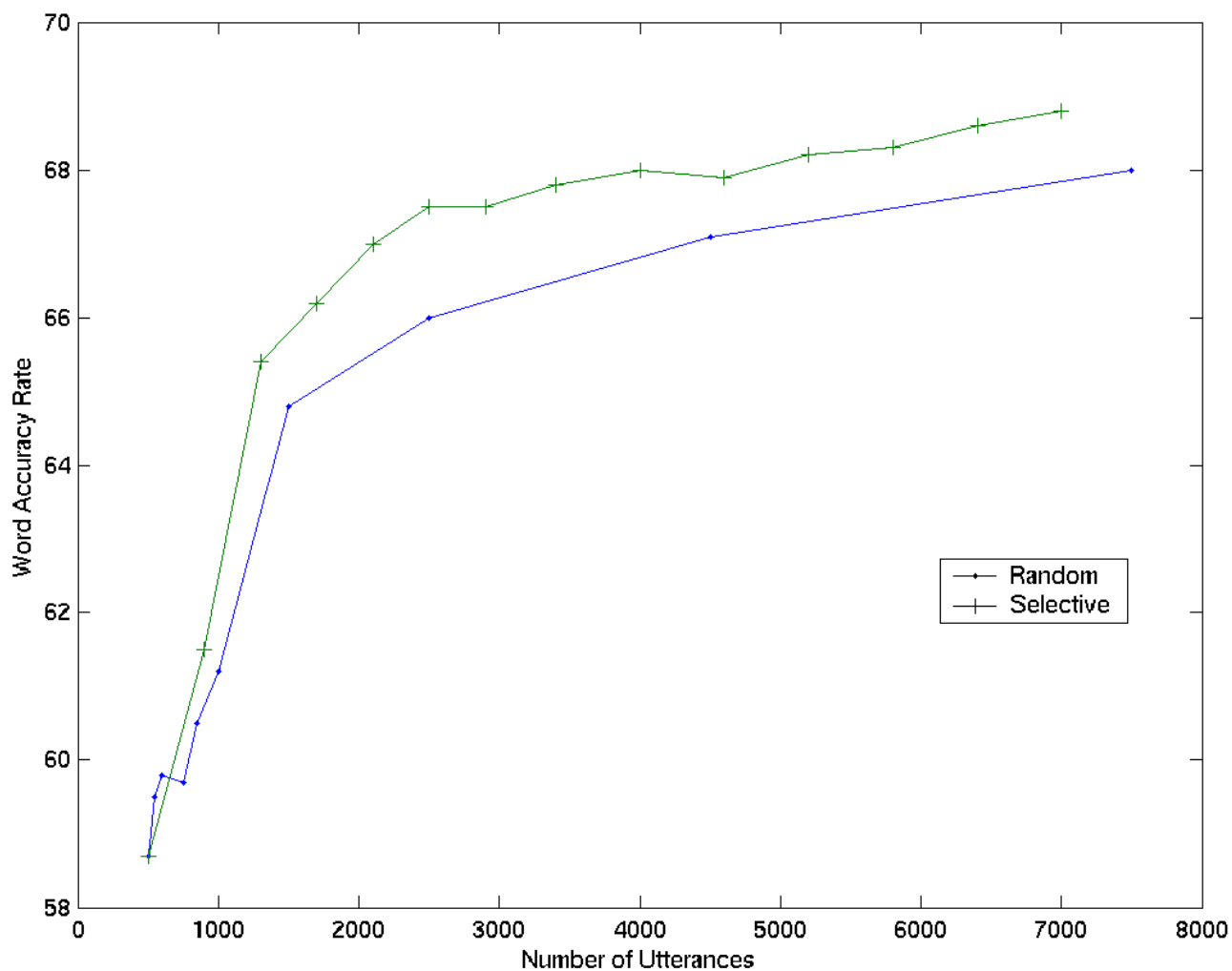


## Active Learning Expt(3)

- ◆ Data is time ordered and time-dependent data bin is used for selective sampling
- ◆ Time window for selective sampling
- ◆ Data is “forgotten” after n days
- ◆ Experiment close to operation modus operandi



# Active Learning Expt(3)



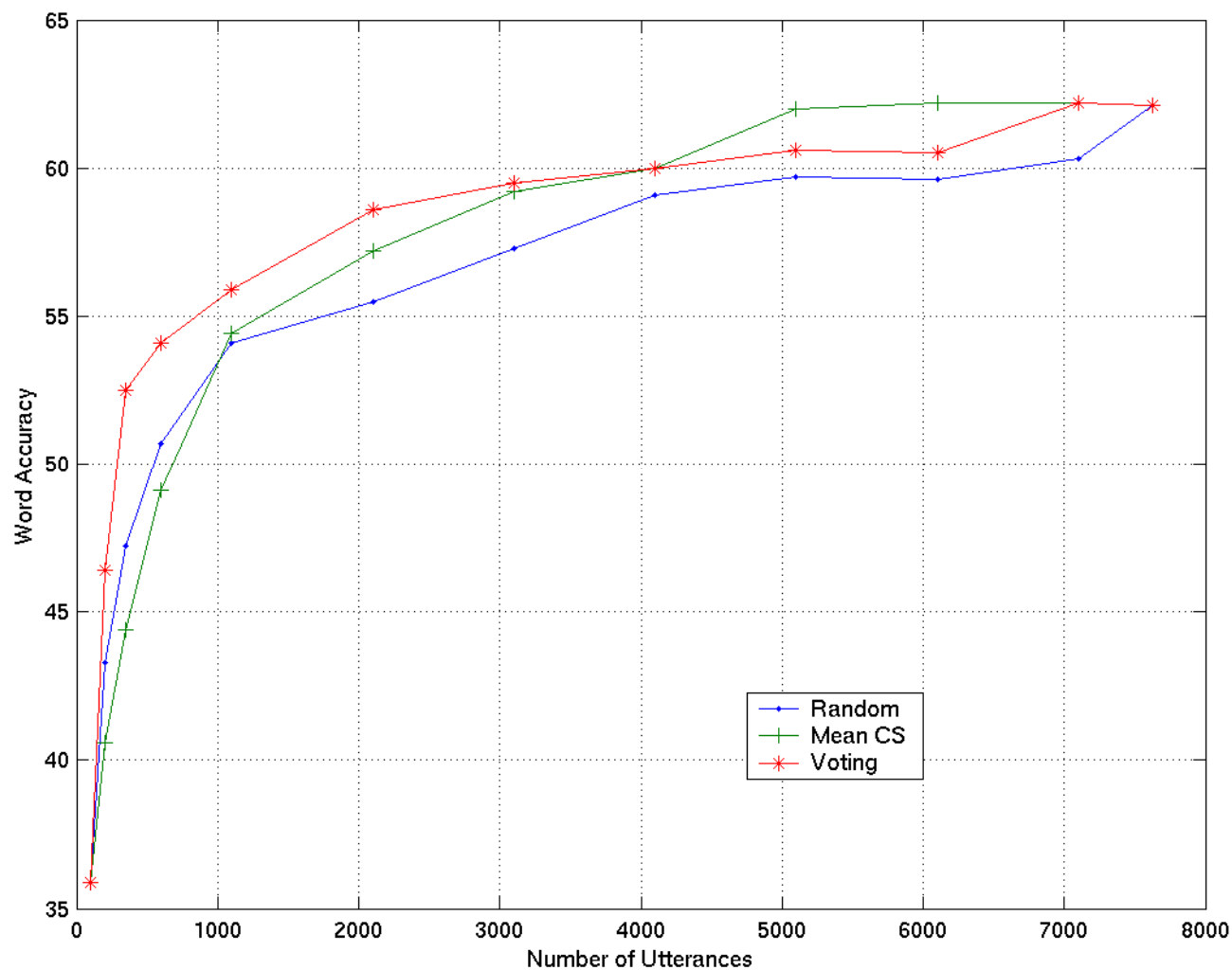
time

# Active Learning Expt(1)

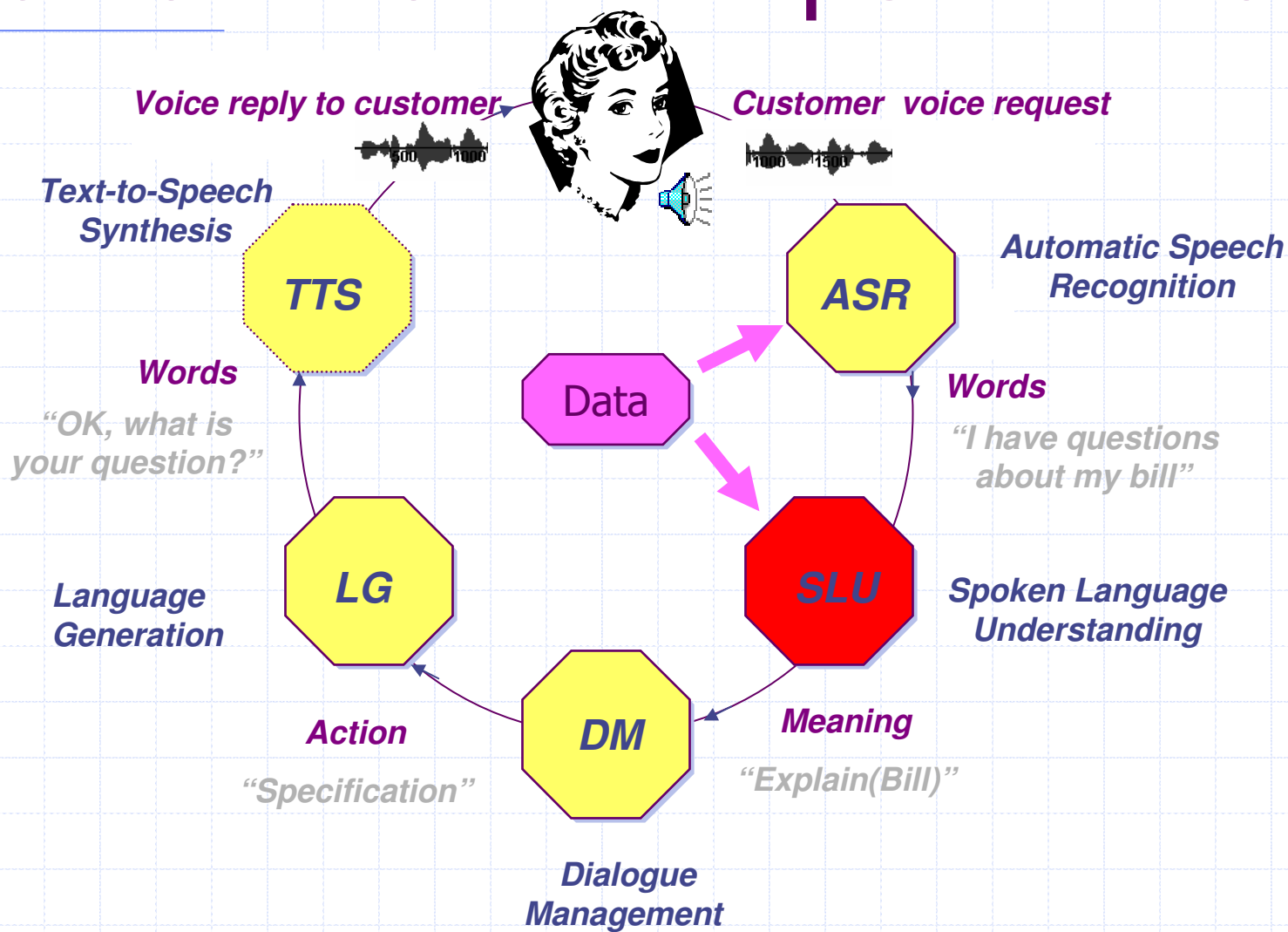
- ◆ Data collected from TTS Help Desk Trial
  - 8K utterances
  - Average length 5 words
  - Channel distortions (not matched AM)
- ◆ All utterance turns
- ◆ Bootstrap data for LM and scoring
  - Web-Mail data
- ◆ Data is pooled and sampled
- ◆ No time ordering constraint

# Active Learning Expt(2)

(TTS Help Desk)



# Human-Machine Spoken Dialog



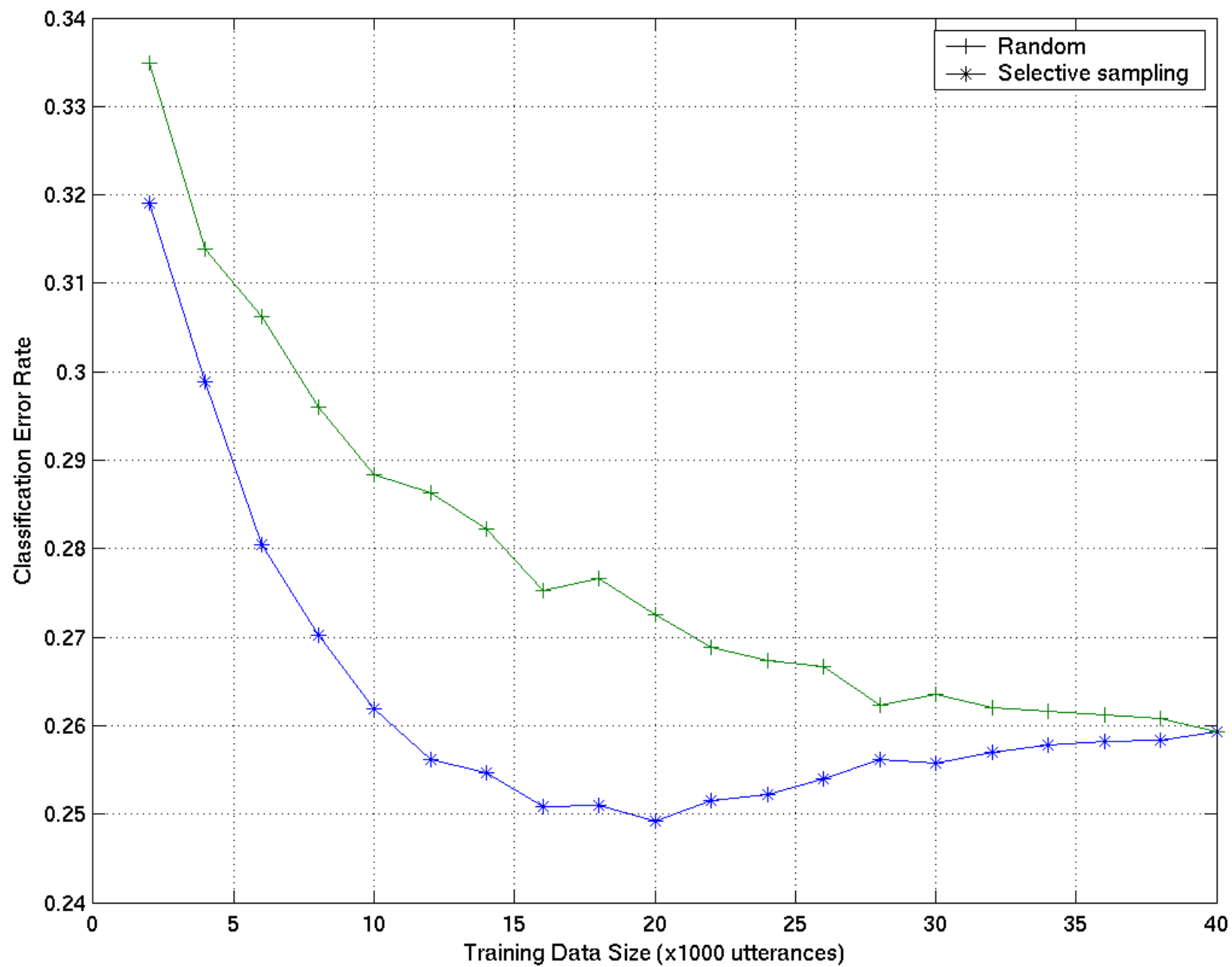


# Understanding User Intent

- ◆ **Greeting Prompt:** AT&T ... How may I help you?
- ◆ **User:** I have questions about my bill
  - **Call-type:** *Explain(Bill)*
- ◆ **Specification Prompt:** OK, what is your question?
- ◆ **User:** I have a couple of numbers I wanna check out
  - **Call-type:** *Explain(Bill\_UnrecognizedNumber)*
- ◆ **Confirmation Prompt:** Would you like to look up a number you don't recognize on your bill?
- ◆ **User:** Several of them
  - **Call-type:** *Yes*

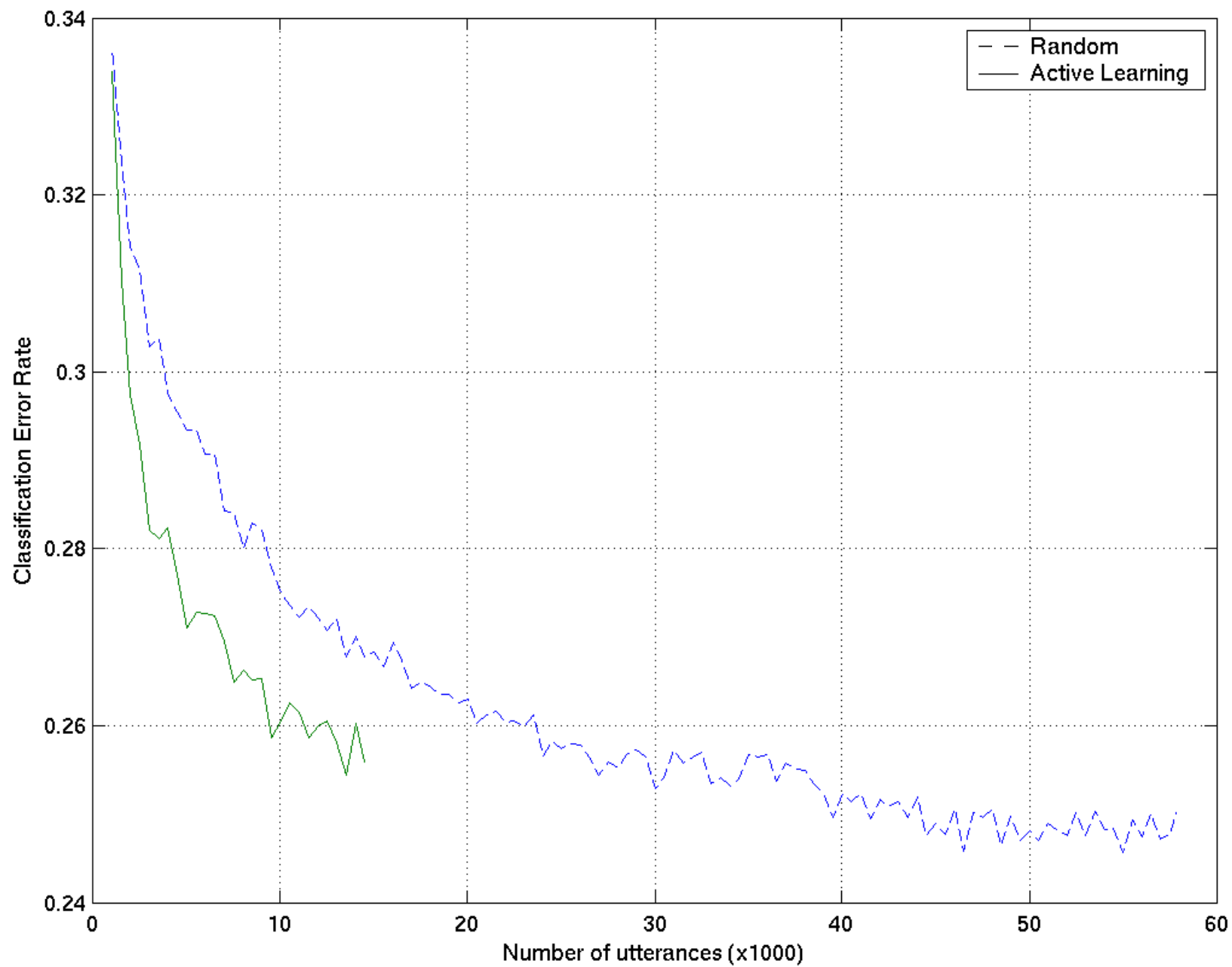
# Call Classification

- ◆ *Tur, Schapire, and Hakkani-Tür, ICASSP'03*
- ◆ 56 call types in total (0300)
- ◆ Classifier: Boosting
- ◆ Fixed pool

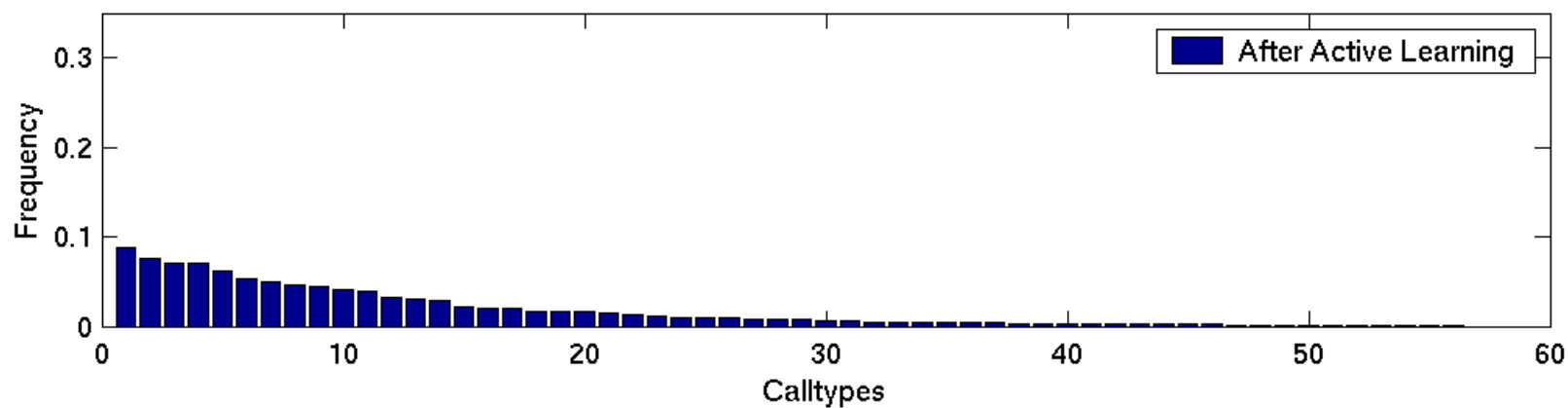
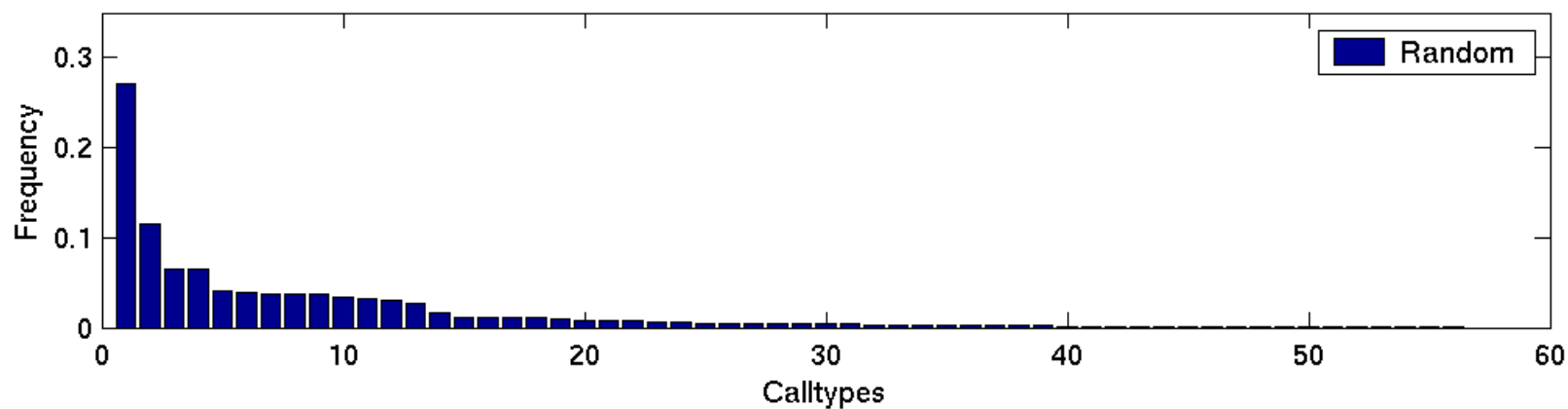


# Call Classification

- ◆ *Tur, Hakkani-Tür, and Schapire; ICASSP 2003*
- ◆ 56 call types in total (0300)
- ◆ Classifier: Boosting
- ◆ Dynamic Pool (1/4 of the candidate utterances selected at each iteration)



# Unbalanced Data Problem



# Unbalanced Data Problem

- ◆ Active learning changes the prior probabilities significantly.
- ◆ Halved the data from 10K to 5K by ignoring the utterances with calltypes occurring more frequent than a certain threshold.

<i>Training Set</i>	<i>Test Set Classification Error Rate</i>
Random 5K	29.12%
Biased 5K	30.81%

- ◆ Biasing distributions hurt the performance!

# One Solution

- ◆ This is not a paradox. If we can find a solution to this problem, active learning may perform better.
- ◆ *Lewis and Catlett, ICML'94* suggested:
  - Changing priors while training
  - Making false-positives more costly than false-negatives (C4.5 supports this)



# Outline

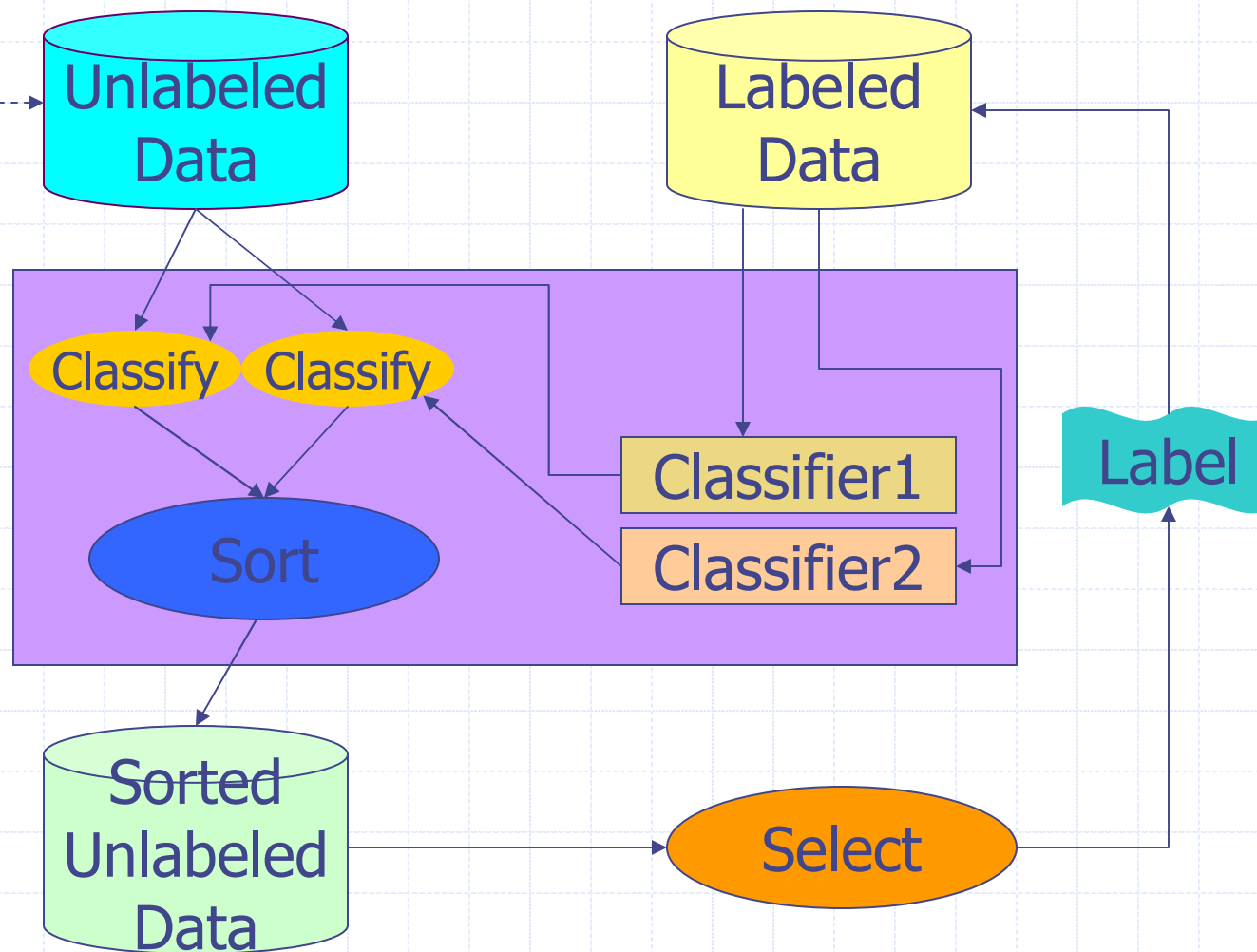
## ◆ Algorithm Dimension:

- Passive vs. Adaptive Learning
- Active Learning
  - ◆ Certainty-based
  - ◆ **Committee-based**
- Unsupervised Learning
- Combining Active and Unsupervised Learning

# Committee-based Active Learning

- ◆ Train multiple classifiers using initial training data
- ◆ While (labelers/data available) do
  - Label the data in the pool using all classifiers
  - Sort them according to **disagreement** between classifiers
  - Select the top  $k$  of them.
  - Label and add the selected ones to the training data
  - Re-train the classifier
  - Update the pool

# Committee-Based Active Learning



# Selected Bibliography for Committee-Based Active Learning

- ◆ Seung, Opper, Sompolinsky COLT'92
- ◆ Freund, Seung, Shamir, Tishby ML'97
- ◆ Liere and Tadepalli AAI'97 (Text Categorization)
- ◆ Engelson and Dagan JAIR'99 (POS Tagging)
- ◆ Tur, Schapire, and Hakkani-Tür ICASSP'03 (Call Classification)
- ◆ Osborne and Baldrige, EMNLP'03, NAACL'04 (Parsing)

# Part of Speech Tagging

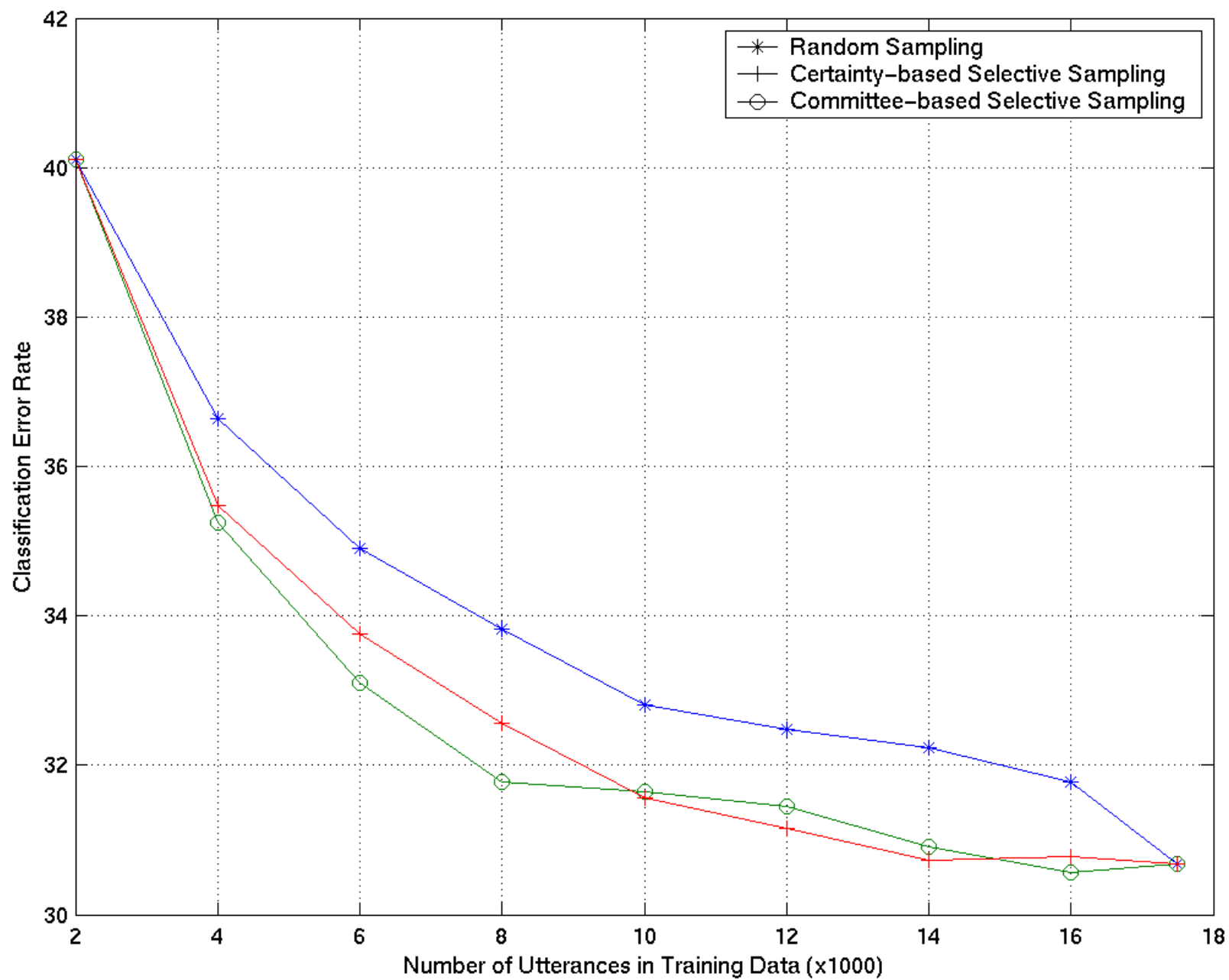
- ◆ *Engelson and Dagan JAIR'99*
- ◆ Part-of-speech tagging using HMMs
- ◆ Degree of disagreement for sample  $w$ :  
normalized entropy of committee classifications

$$D(w) = -\frac{1}{\log \min(k, |C|)} \sum_c \frac{V(c, w)}{k} \log \frac{V(c, w)}{k}$$

- ◆ Reduced the amount of human-labeled data needed by a factor of 4 using 10 committee members.

# Call Classification

- ◆ *Tur, Schapire, and Hakkani-Tür, ICASSP'03*
- ◆ 56 call types in total
- ◆ Fixed pool
- ◆ 2 committee members using 2 different classifiers: SVM and Boosting



# Parsing (HPSG)

- ◆ (Osborne and Baldrige, EMNLP'03, NAACL'04)
- ◆ A committee of parsers is trained using different and independent feature sets:
  - Configurational (e.g. parent, grandparent, sibling relationships)
  - $N$ -gram ( $n$ -grams over tree nodes)
  - Conglomerate (features from phrase structures)
- ◆ Cost of manual annotation is not equal to the number of utterances hand-labeled, but is proportional to the number of disambiguation decisions the labelers have to make.
- ◆ 73% reduction in the cost of annotation.



# Outline

## ◆ Algorithm Dimension:

- Passive vs. Adaptive Learning
- Active Learning
  - ◆ Certainty-based
  - ◆ Committee-based
- **Unsupervised Learning**
- Combining Active and Unsupervised Learning

# Unsupervised Learning

- ◆ **Goal:** to exploit the unlabeled utterances
  - to train better models
  - to train in a shorter time frame
  - to adapt fast to changes

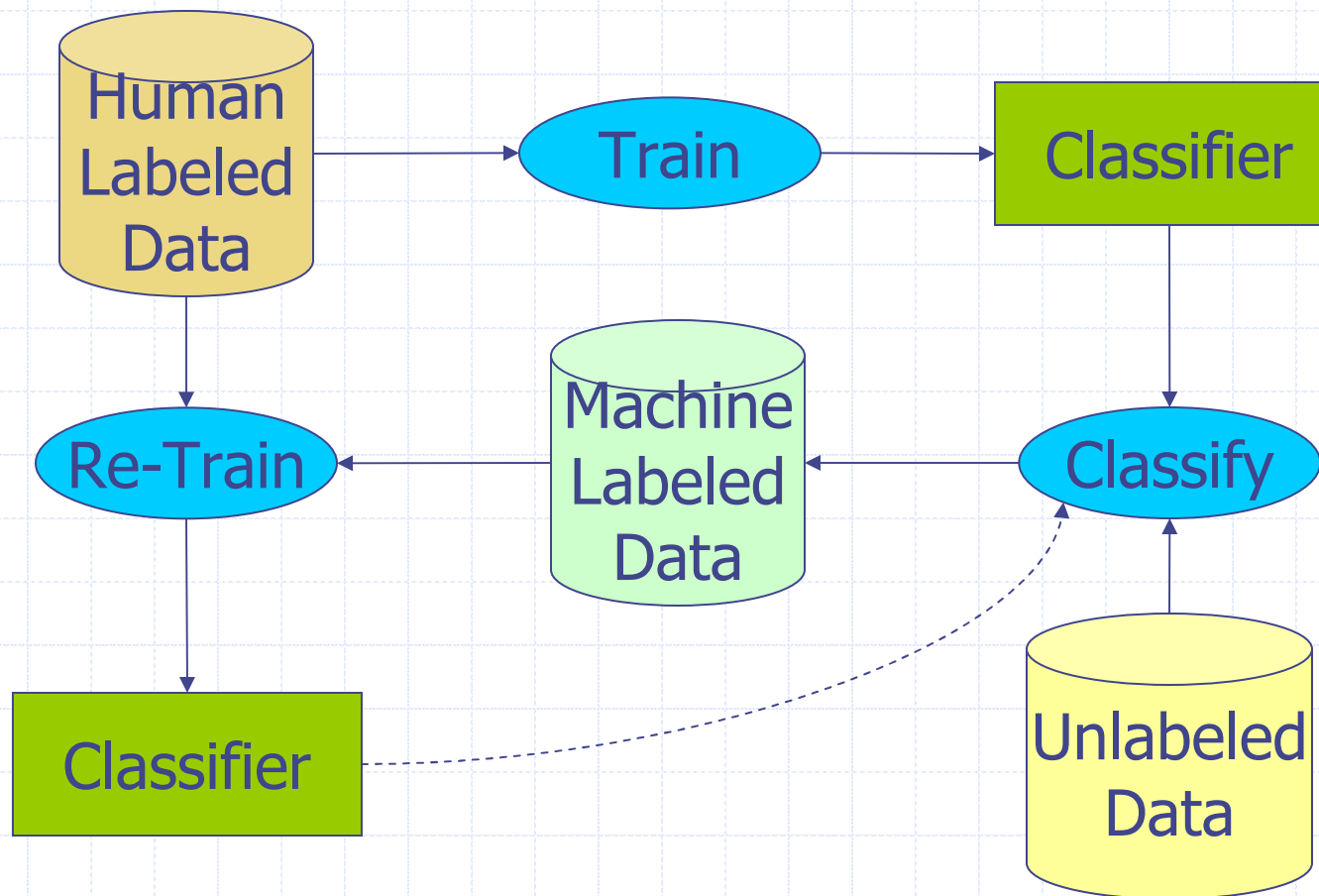
# Selected Bibliography for Unsupervised Learning

- ◆ Blum and Mitchell, COLT'98
- ◆ Nigam and Ghani, ICML'98
- ◆ Joachims, ICML'99
- ◆ Nigam, McCallum, Thron, and Mitchell, ML'00
- ◆ Nigam and Ghani, CIKM'00
- ◆ Ghani, ICML'02
- ◆ Tur and Hakkani-Tür, ES'03
- ◆ ...

## Using EM

- ◆ *Nigam, McCallum, Thron, and Mitchell, ML'00*
- ◆ Train a classifier using human-labeled data (call this prior model:  $\Pi$ )
- ◆ Add unlabeled utterances:
  - Classify the unlabeled utterances with  $\Pi$  (**Estimation**)
  - Add this machine-labeled data to the human-labeled data in a weighted manner and re-train the classifier (**Maximization**)
  - Iterate until model parameters converges
- ◆ 3-fold reduction in labeled data needed

# Unsupervised Learning



# Co-Training

- ◆ *Blum and Mitchell, COLT'98*
- ◆ Assume there are multiple views for classification
  - e.g. Task: Web-page classification
    1. Words in the web-page
    2. Words in the hyperlinks pointing to that web page
  - 1. Train multiple models using each view
  - 2. Classify unlabeled data
  - 3. Enlarge training set of the other using each classifier's predictions
  - 4. Goto Step 1
- ◆ Halved the classification error rate
- ◆ Nigam and Ghani later extended this to Co-EM so that it uses probabilistic labels (*CIKM'00*)

# Unsupervised Learning for ASR

- ◆ Goal: Exploit untranscribed data to improve performance.
- ◆ Use of the error signal to exploit the untranscribed data.
- ◆ Use of extra information, such as TV captions.
- ◆ Combining active and unsupervised learning.

# Previous Approaches

## ◆ AM

- TV captions (Kemp and Waibel, 1998, 1999).
- Accurate portions of the ASR output (Zavaliagos and Colthurst, 1998).
- ASR output (Lamel et al., 2002).

## ◆ LM

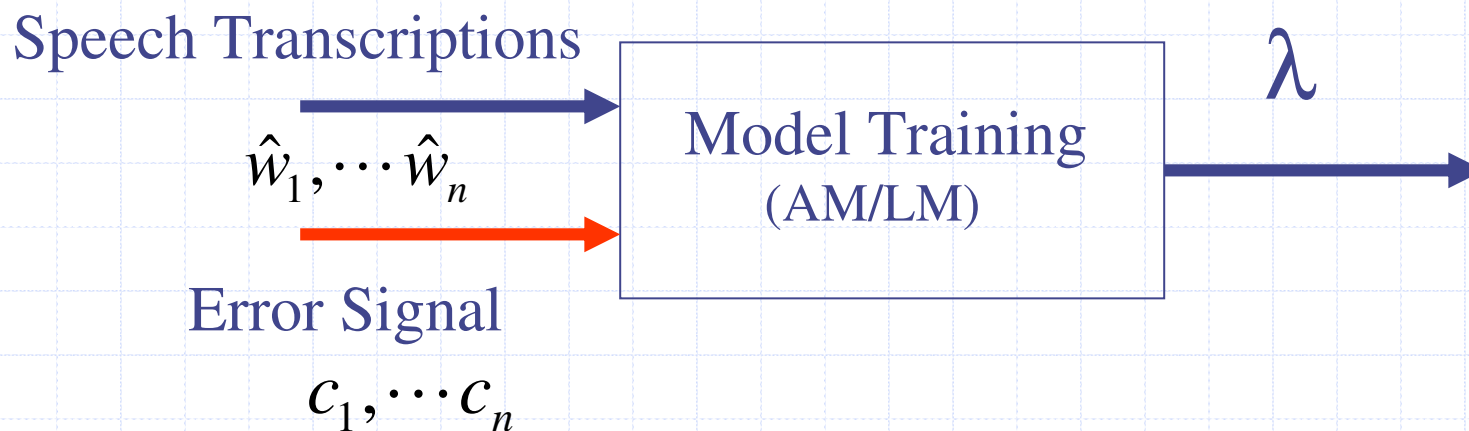
- Word confidence scores to extract the portions that are recognized correctly (Gretter and Riccardi, 2001).
- ASR output (Stolcke, 2002).
- ASR word lattices with posteriors (Roark and Bacchiani, 2003).

## ◆ Riccardi and Hakkani-Tür (Eurospeech, 2003).



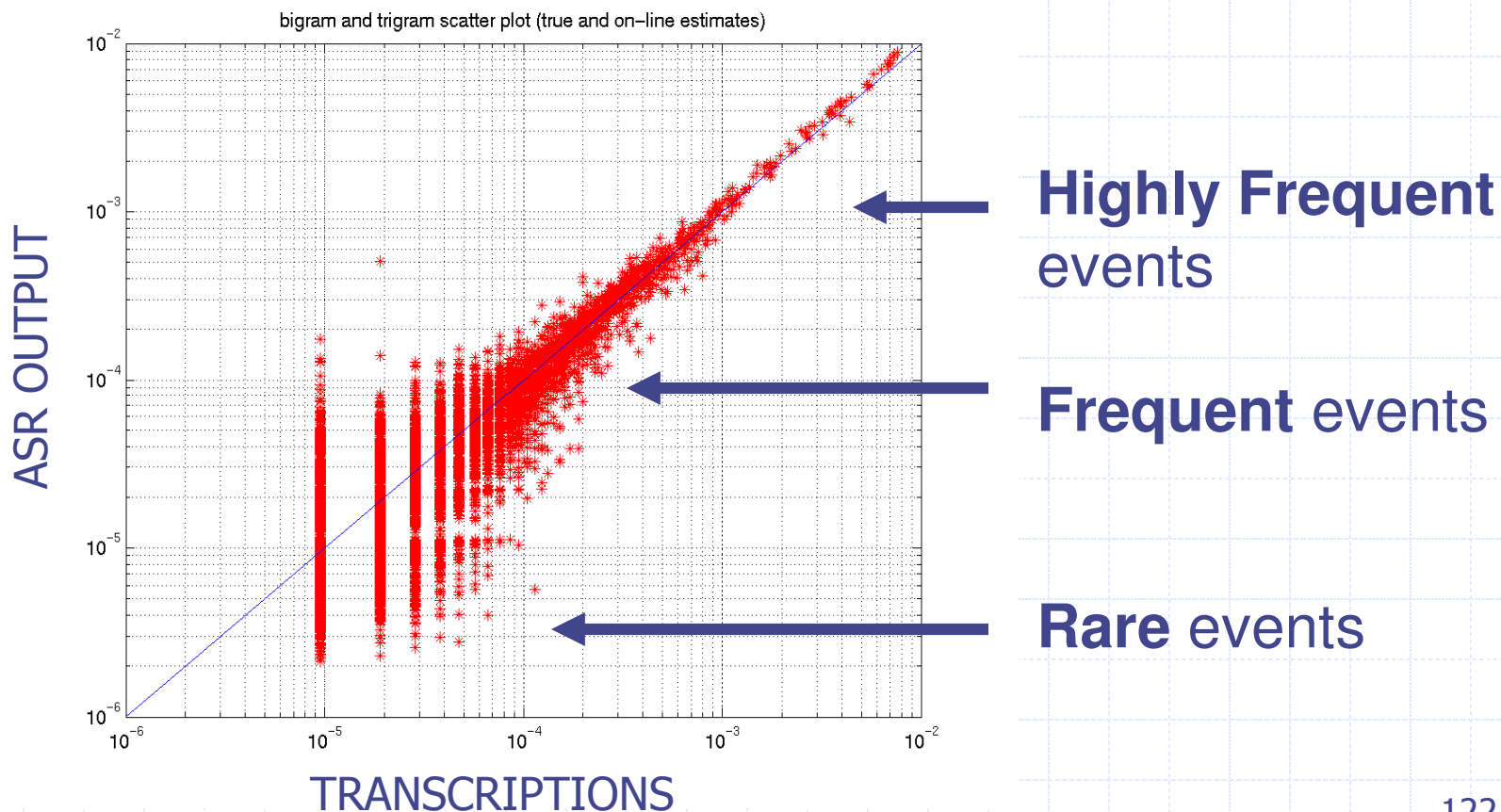
# Unsupervised Learning

$$C(w_i, w_{i+1}, w_{i+2}) = F(C(\hat{w}_i, \hat{w}_{i+1}, \hat{w}_{i+2}), c)$$



# Unsupervised Learning for ASR

- Estimate probabilities from ASR output.



# Results on 0300 Data

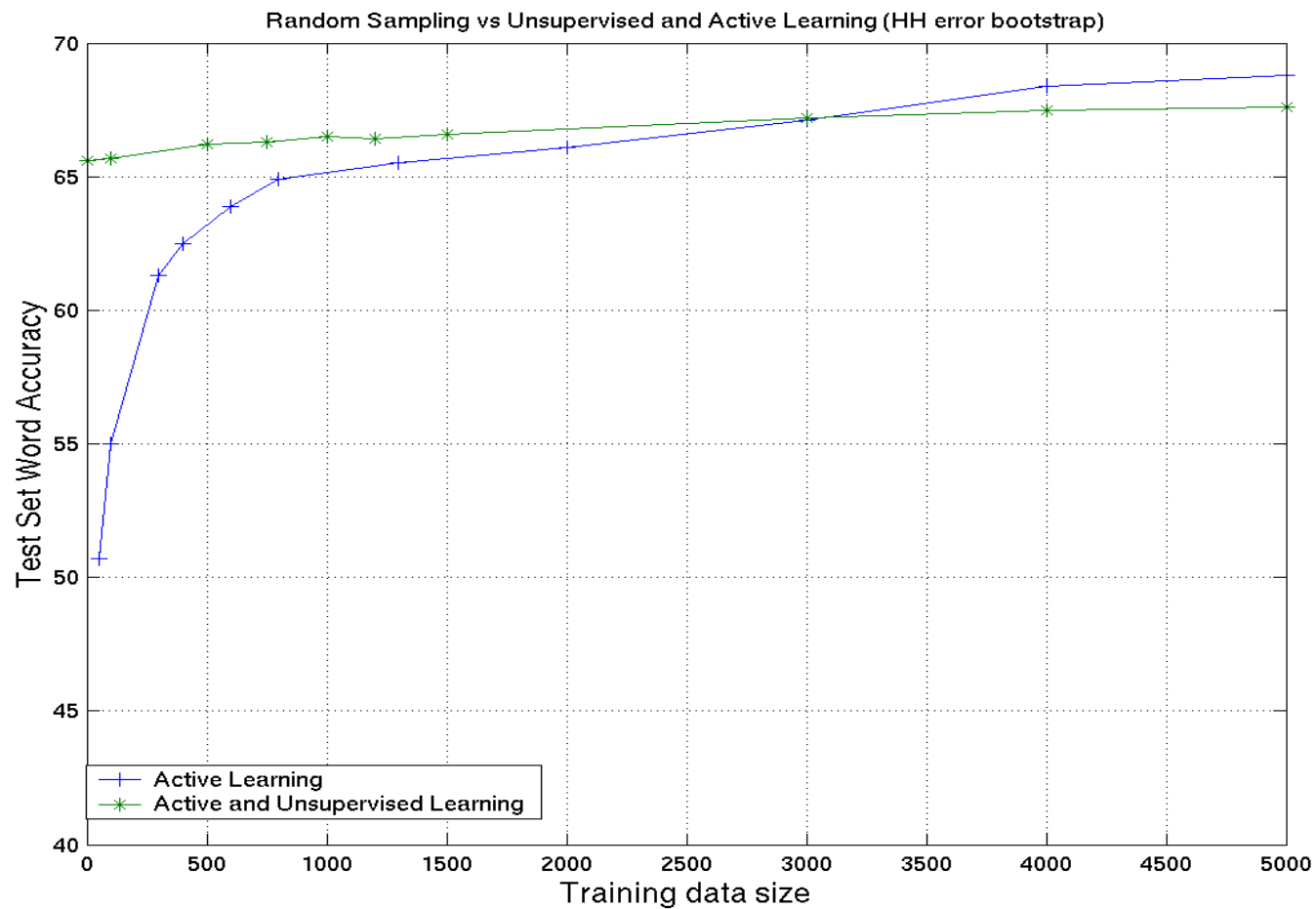
- ◆ Initial Set: random 1K H-M utterances (11K words)
- ◆ Additional Set: 27K H-M utterances
- ◆ Test Set: 1000 H-M utterances (~11K words)

Training Set	Word Accuracy
Initial Set	59.1%
ASR output of Additional Set	61.5%
ASR output of Additional Set, with confidence scores	62.1%

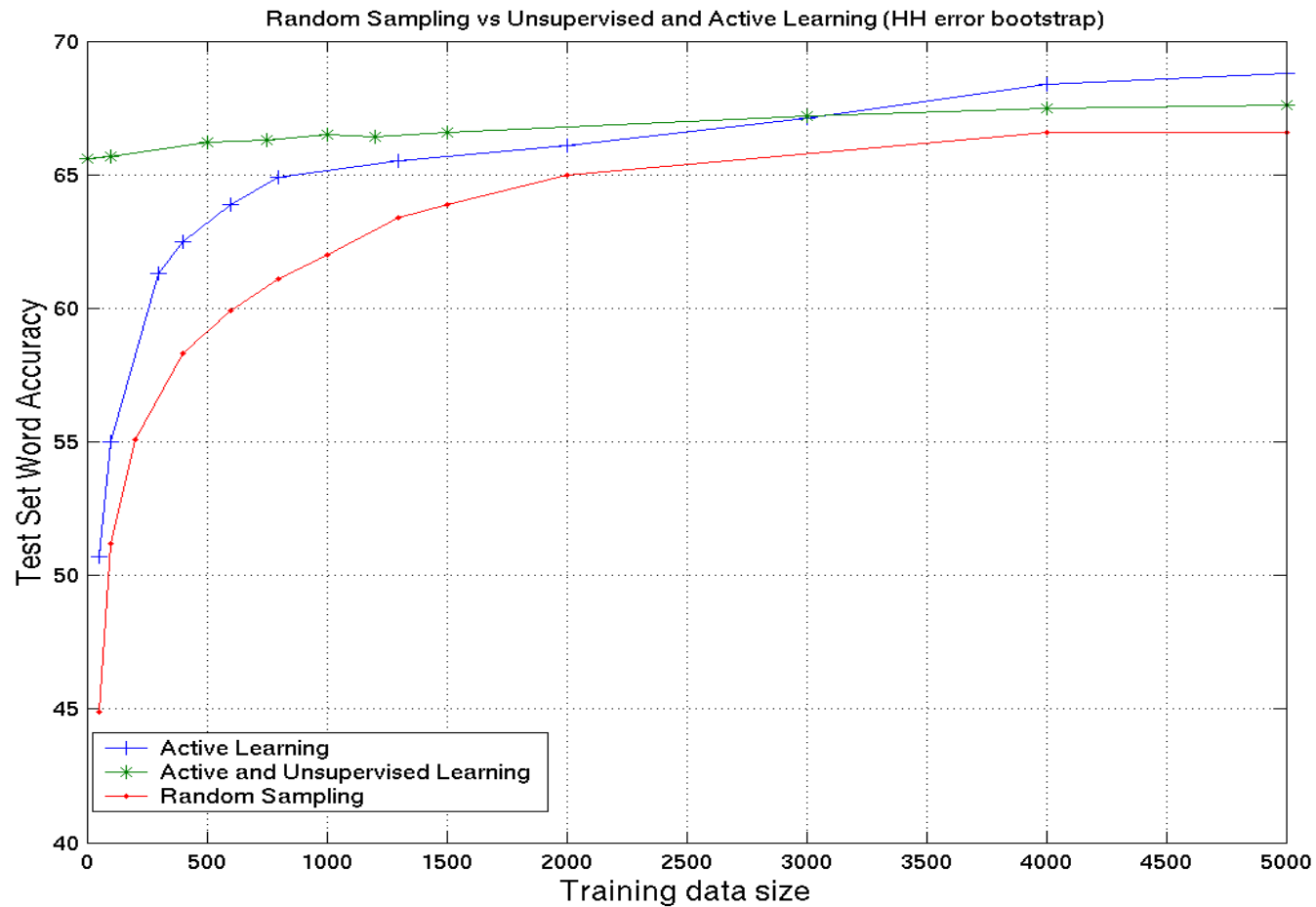
## Experiments with 0300 Data

- ◆ Initial Set: 8K H-H utterances
- ◆ Additional Set: 28K H-M utterances  
(~320K words)
- ◆ Test Set: 1000 H-M utterances (~11K words)

# Results on 0300 Data



# Results on 0300 Data



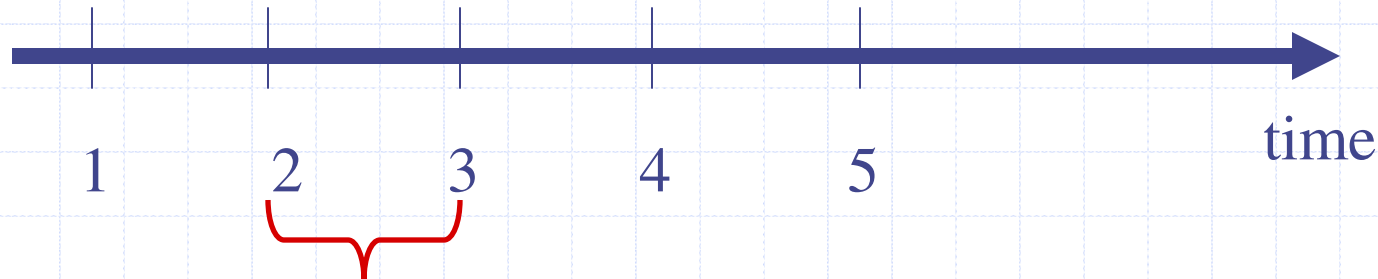
# Results on TTS Help Desk Data

- ◆ Initial Set: Web and e-mail data (~40 K words)
- ◆ Additional Set: 7,629 H-M utterances (~33K words)
- ◆ Test Set: 2,160 H-M utterances (~9.2K words)

<b>Training Set</b>	<b>Word Accuracy</b>
Initial Set	42.2%
Initial Set + ASR output of Additional Set	50.6%
Initial Set + Additional Set	61.8%

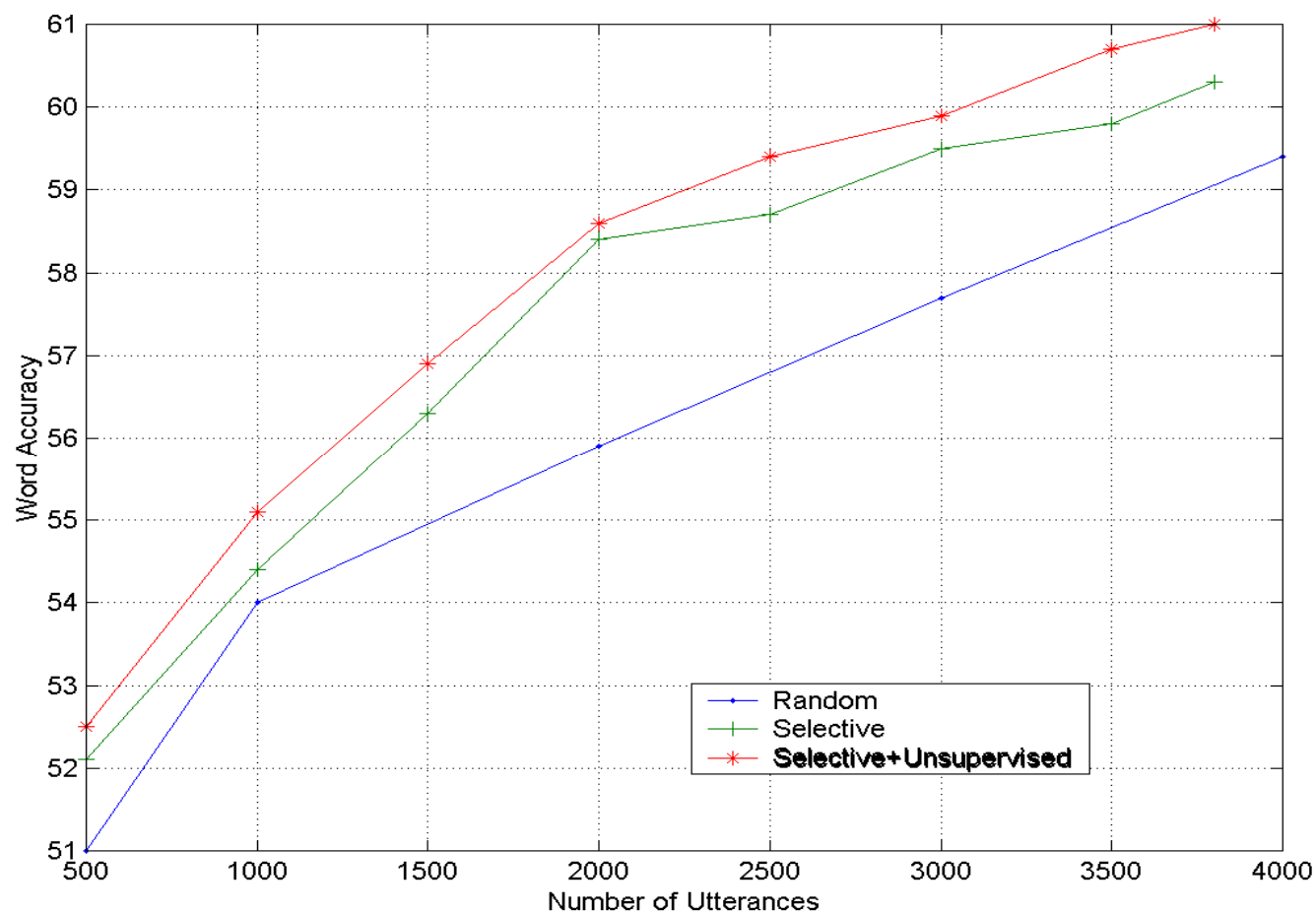
## Results on TTS Help Desk Data

- ◆ Data is time ordered and time-dependent data bin is used for selective sampling
- ◆ Time window for selective sampling
- ◆ Data is only used for unsupervised learning after n days.
- ◆ Experiment close to operation modus operandi





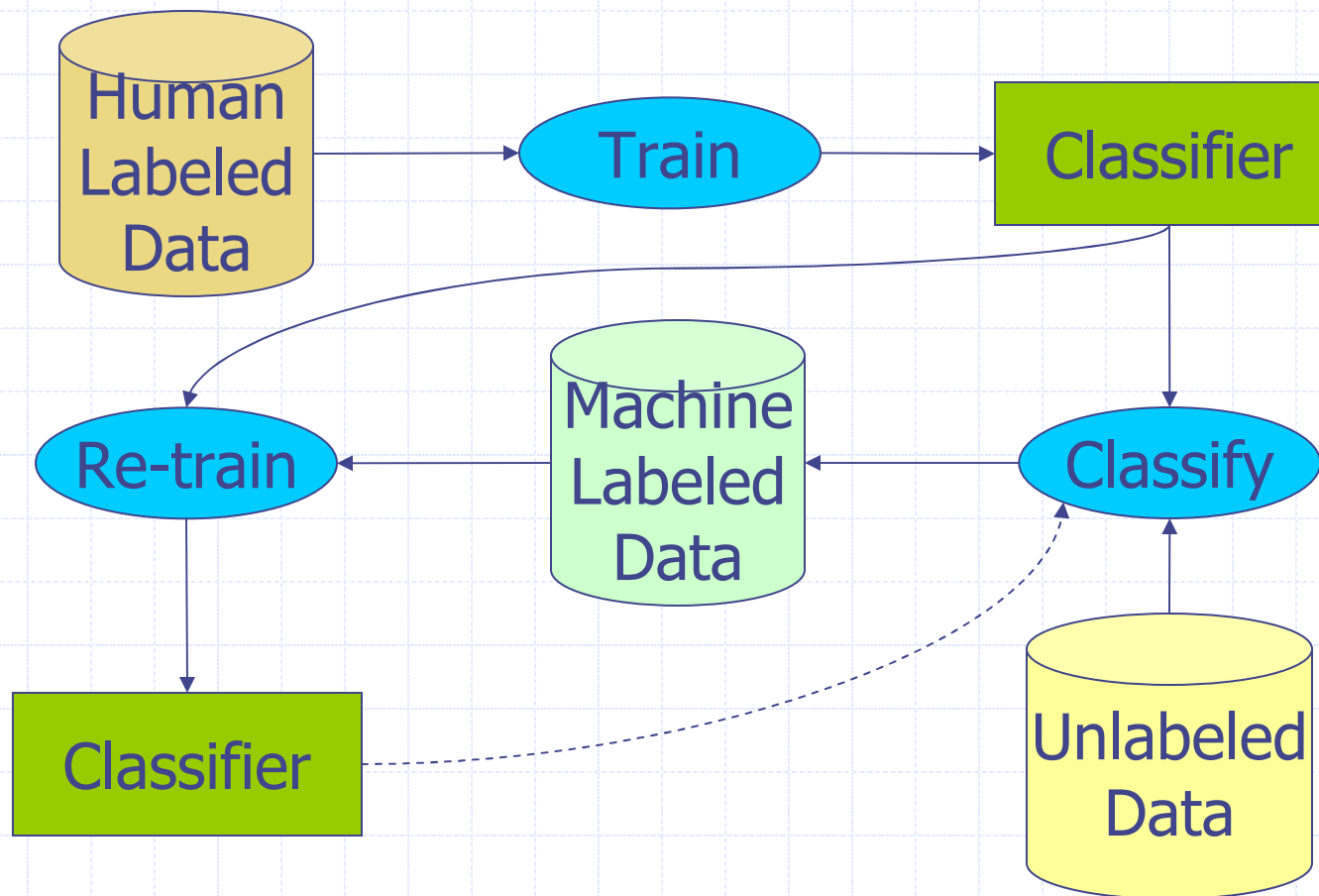
# Results on TTS Help Desk Data



# Unsupervised Learning in Boosting

- ◆ *Tur and Hakkani-Tür, Eurospeech'03*
- ◆ Train the Boosting classifier using human-labeled data (call this prior model:  $\Pi$ )
- ◆ Augment  $\Pi$  with unlabeled utterances
  - Classify the unlabeled utterances with  $\Pi$
  - Use the top calltype or calltypes exceeding some threshold as the label of that utterance
  - Augment the classifier using unlabeled data changing the loss function so that it fits both
    - ◆ the prior model,  $\Pi$ , and
    - ◆ the new unlabeled data

# Unsupervised Learning in Boosting



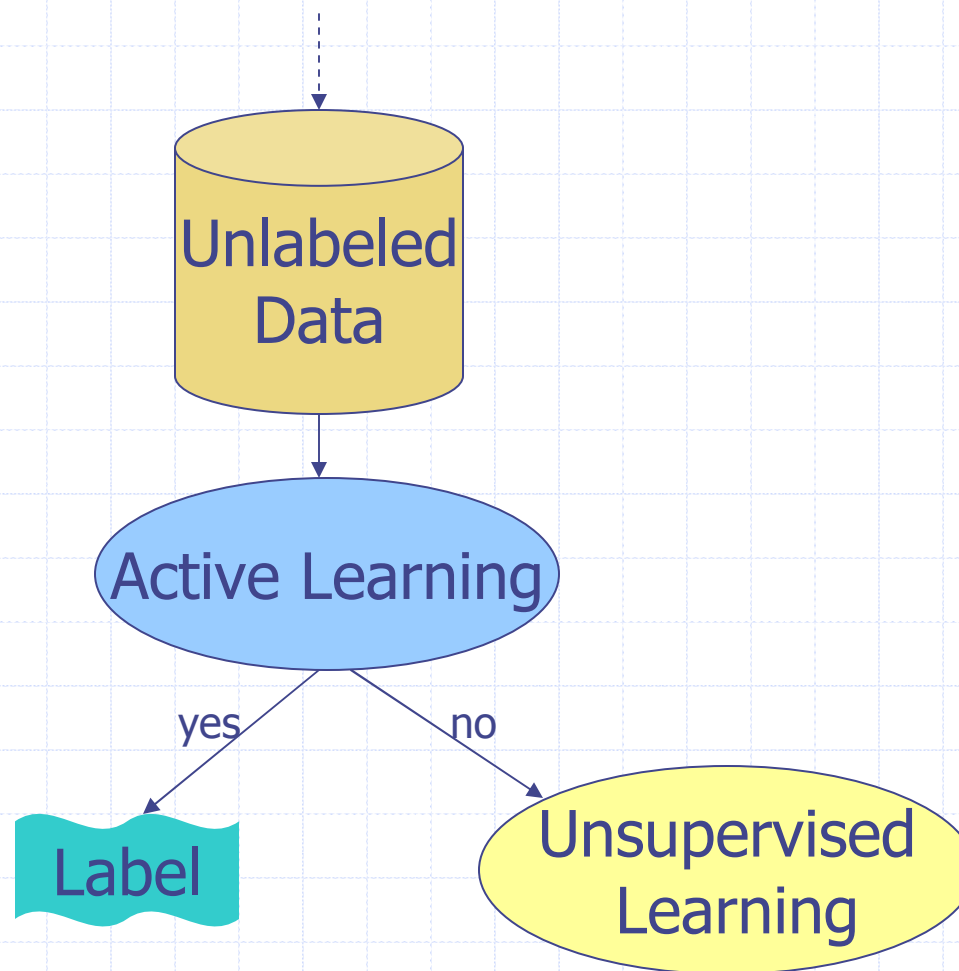
# Outline

- ◆ Algorithm Dimension:
  - Passive vs. Adaptive Learning
  - Active Learning
    - ◆ Certainty-based
    - ◆ Committee-based
  - Unsupervised Learning
  - Combining Active and Unsupervised Learning

# Combining Active and Unsupervised Learning

- ◆ Train a classifier using initial training data
- ◆ While (labelers/data available) do
  - Select  $k$  samples for labeling using ***active learning***
  - Label and add these selected ones to the training data and re-train the classifier.
  - Exploit the unselected data using ***unsupervised learning***
  - Update the pool.

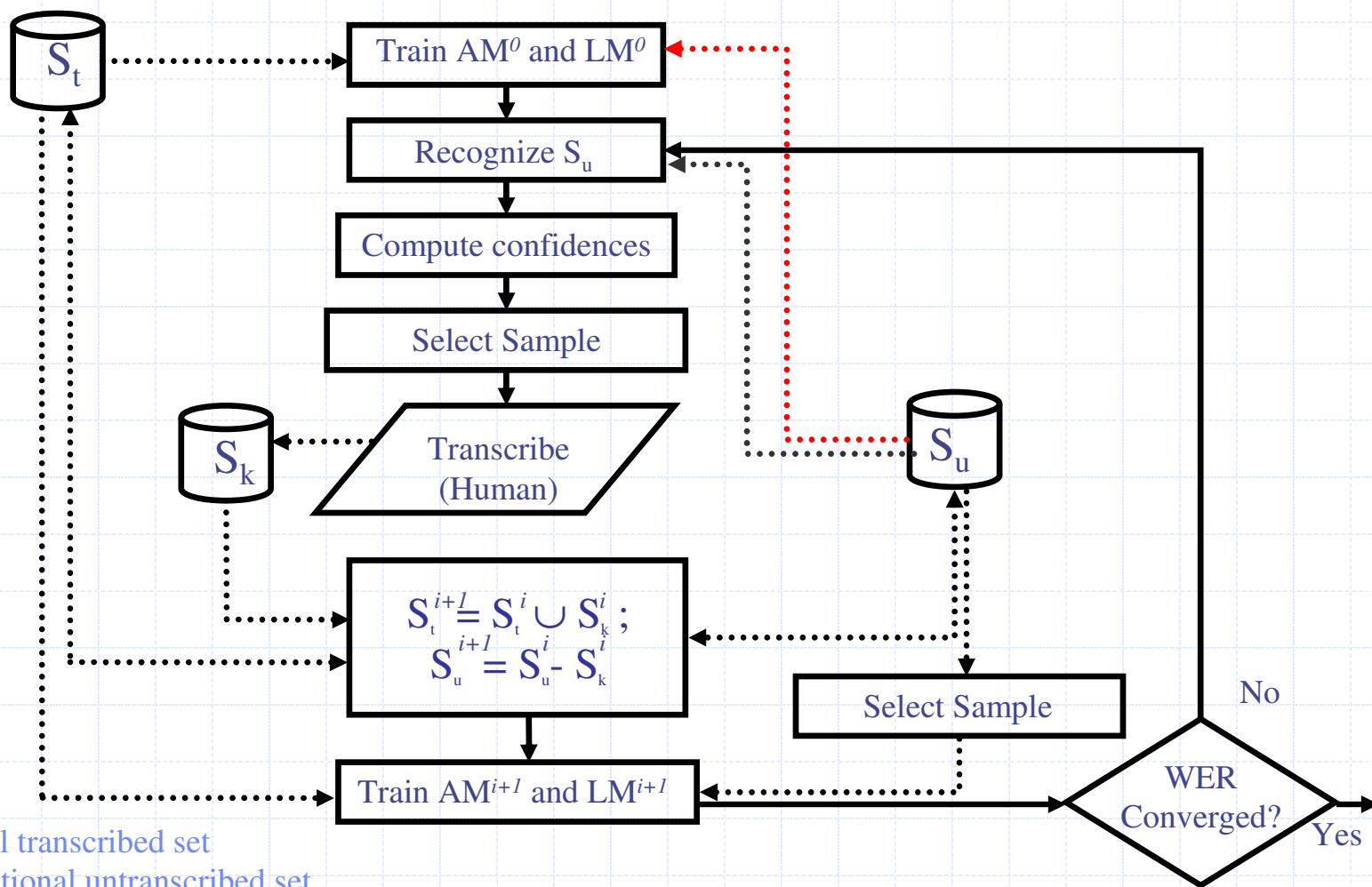
# Combining Active and Unsupervised Learning



## Selected Bibliography for Combining Active and Unsupervised Learning

- ◆ McCallum and Nigam, ICML'98
- ◆ Muslea, Minton, and Knoblock, ICML'02
- ◆ Fur, Hakkani-Für, and Schapire, not appeared yet

# Active and Unsupervised Learning for ASR



$S_t$ : Initial transcribed set  
 $S_u$ : Additional untranscribed set  
 $S_k$ : Intermediate set to be transcribed



# Exploiting Untranscribed Data

- ◆  $X$  is transcribed text,  $x$  and  $y$  are n-grams.

$$C(x) = \sum_{y \in X} \delta_x(y)$$

- ◆  $X$  is ASR output, where every n-gram  $y$  has a confidence score,  $c(y)$ ,

$$\begin{aligned} C_u(x) &= \sum_{y \in X} c(y) \times \delta_x(y) \\ &= \sum_{y \in X} (1 - e(y)) \times \delta_x(y) \\ &= C(x) - \sum_{y \in X} e(y) \times \delta_x(y) \end{aligned}$$

# N-gram Confidence Scores

- ◆ If we represent each n-gram  $X$  as  $x_1, \dots, x_n$  the confidence score of each n-gram can be:

$$c(X) = \sqrt[n]{\prod_{i=1}^n c(x_i)}$$

$$c(X) = c(x_n)$$

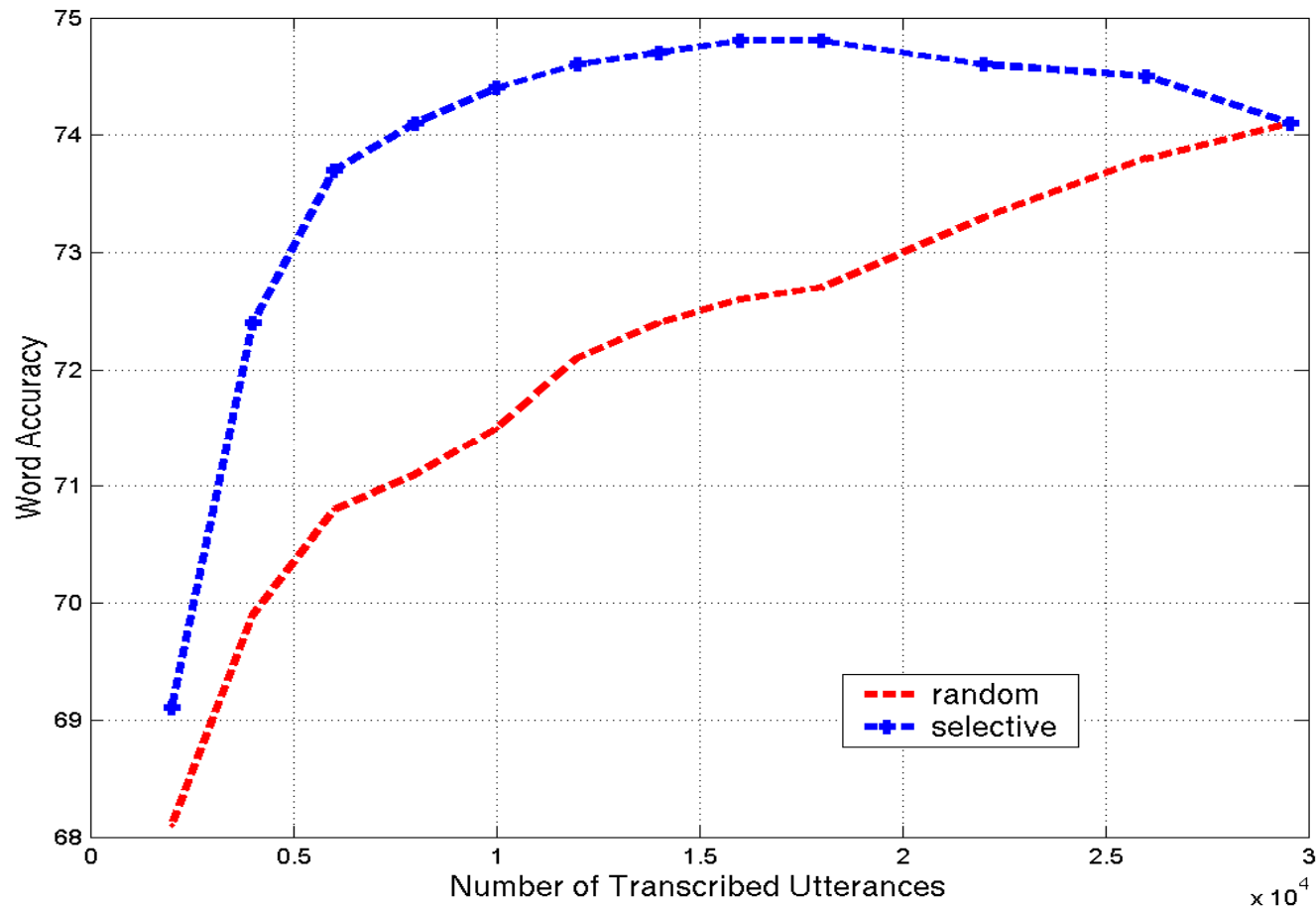
$$c(X) = \min_{x_i} c(x_i)$$

$$c(X) = \begin{cases} 1, & \text{if } c(x_i) > \text{threshold}, \\ 0, & \text{otherwise} \end{cases} \quad \forall x_i$$

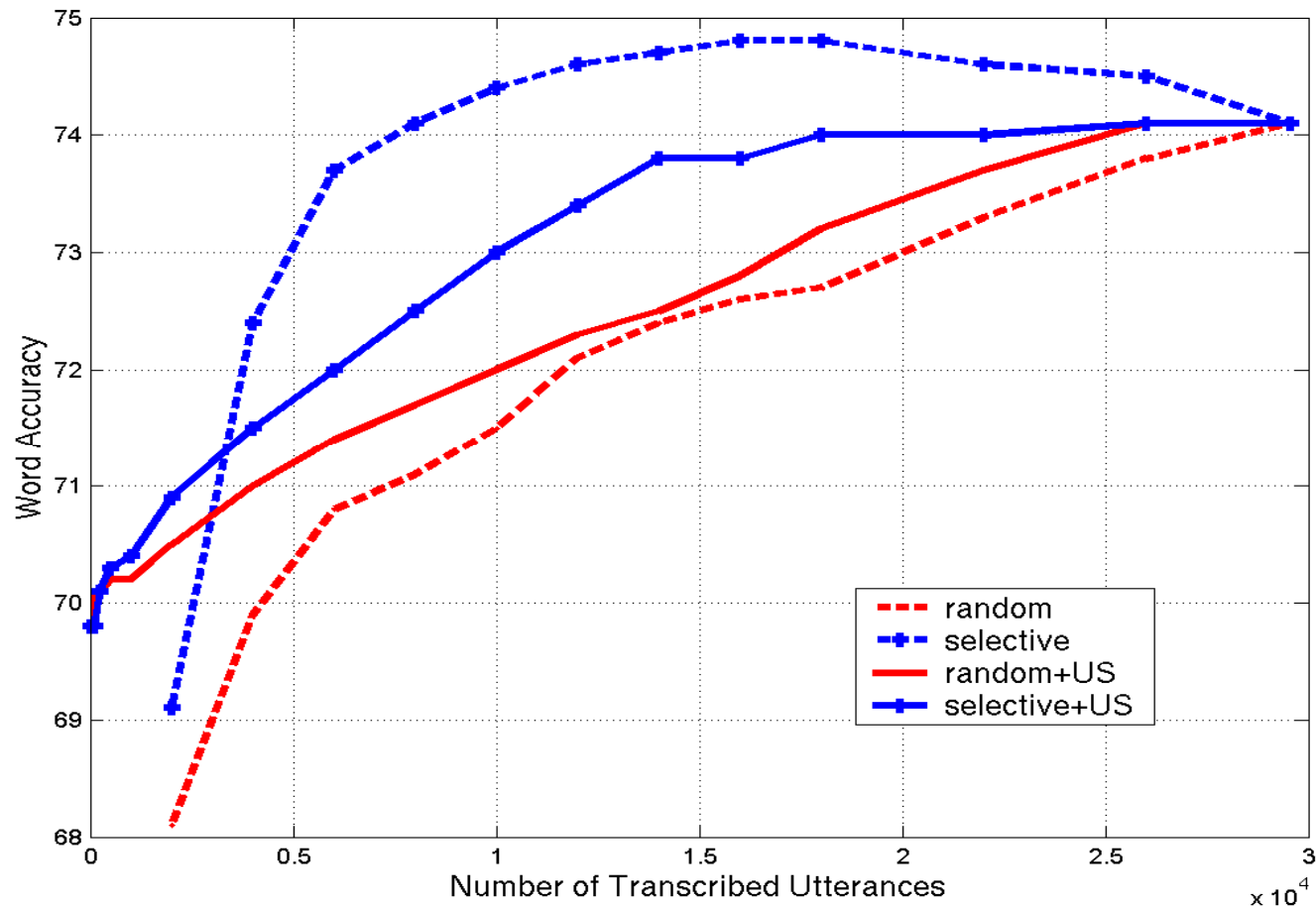
## Active and Unsupervised Learning Expt

- ◆ Initial Transcribed Data: Data collected from web, and Switchboard corpus.
- ◆ Additional Training Data: ~30K utterances from the HMIHY?<sup>SM</sup>
- ◆ Test Data: 5,171 utterances

# Active and Unsupervised Learning Expt

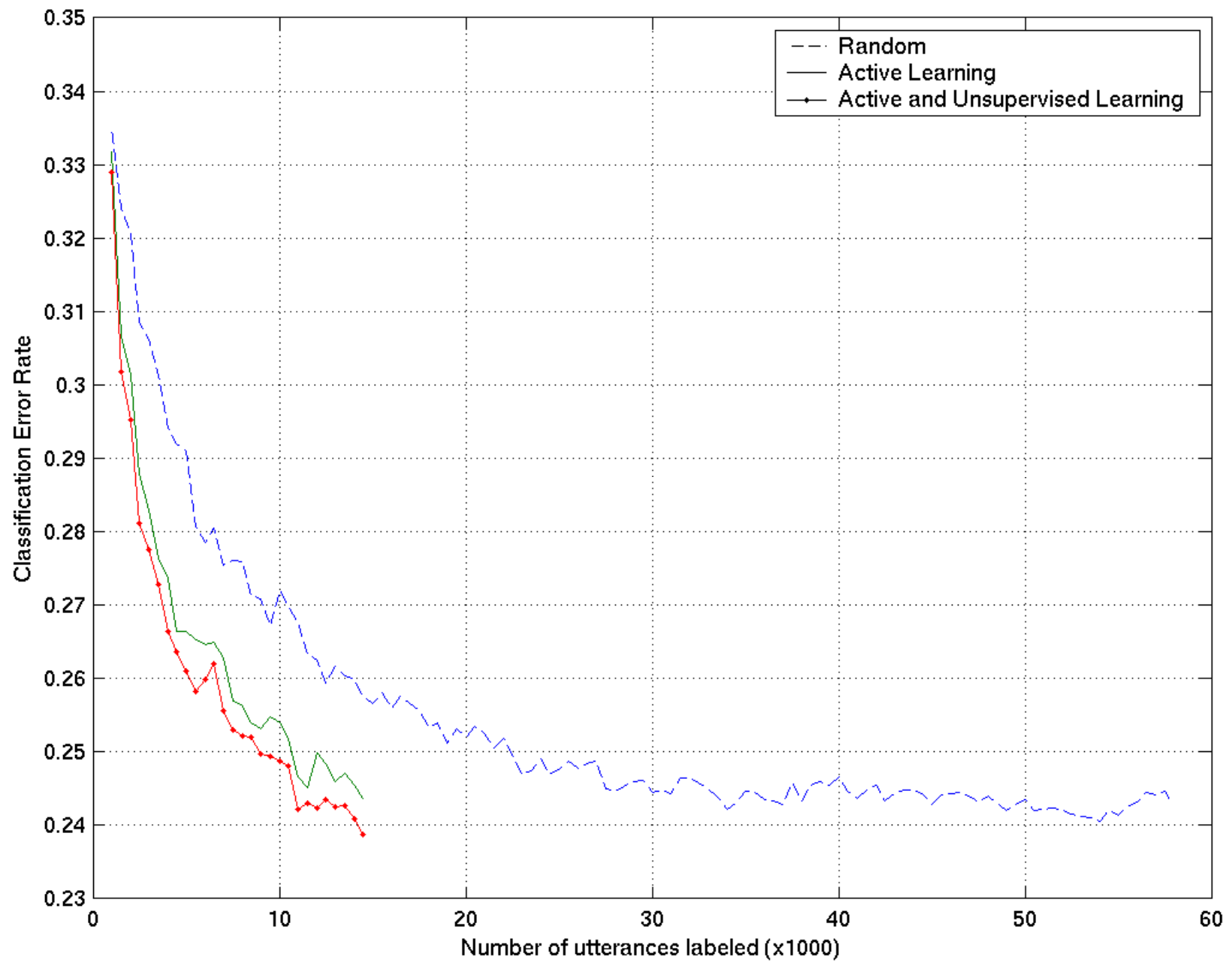


# Active and Unsupervised Learning Expt



# Call Classification

- ◆ *Tur, Hakkani-Tür, and Schapire, to appear.*
- ◆ 56 call types in total
- ◆ Dynamic Pool (1/4 of the candidate utterances selected at each iteration)
- ◆ Classifier: Boosting
- ◆ Combined Certainty-Based Active Learning with Unsupervised Learning



# Text Categorization

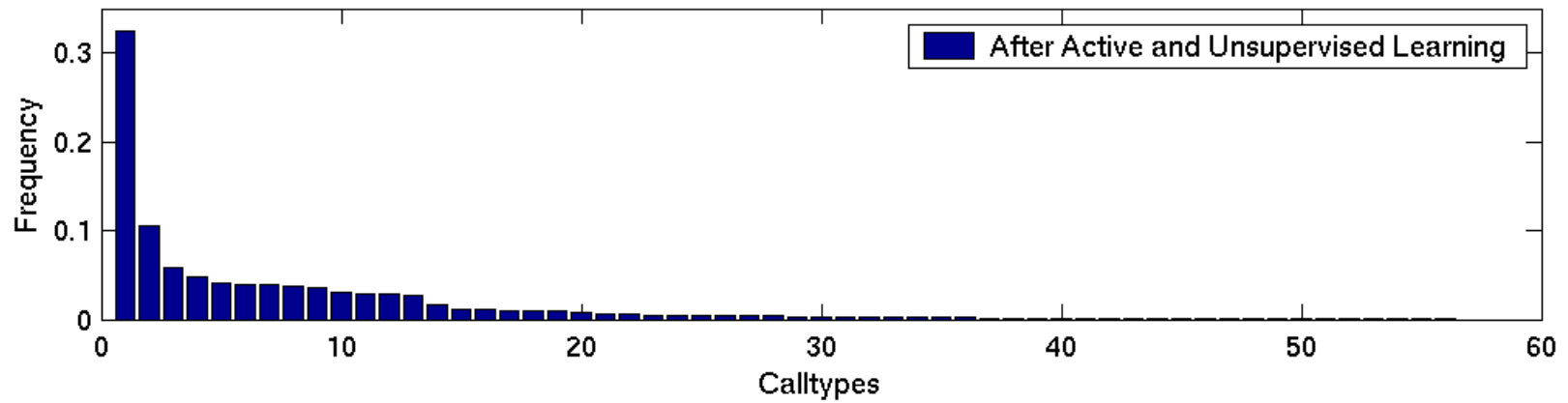
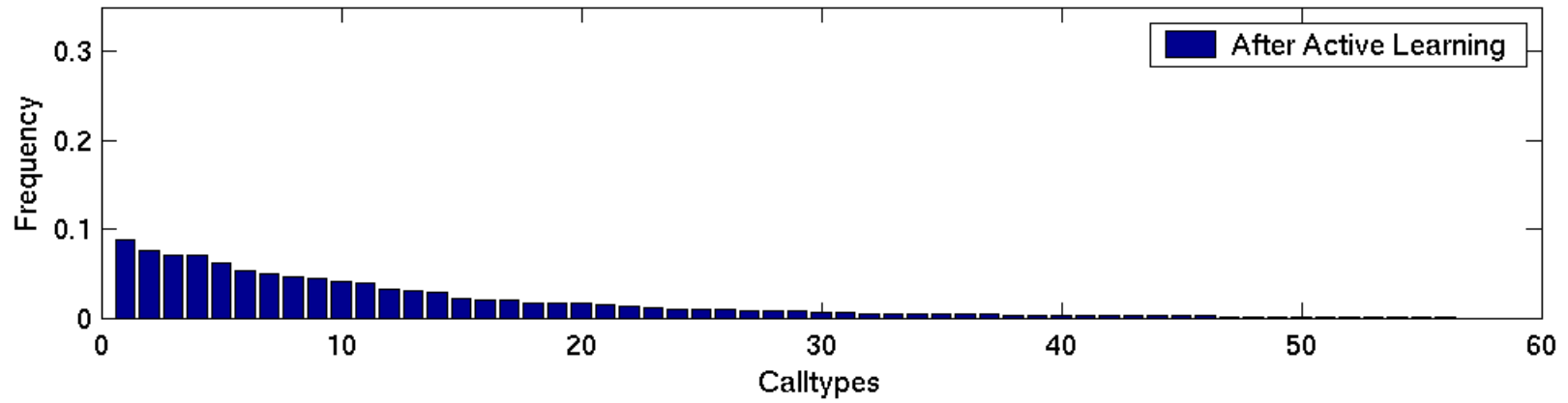
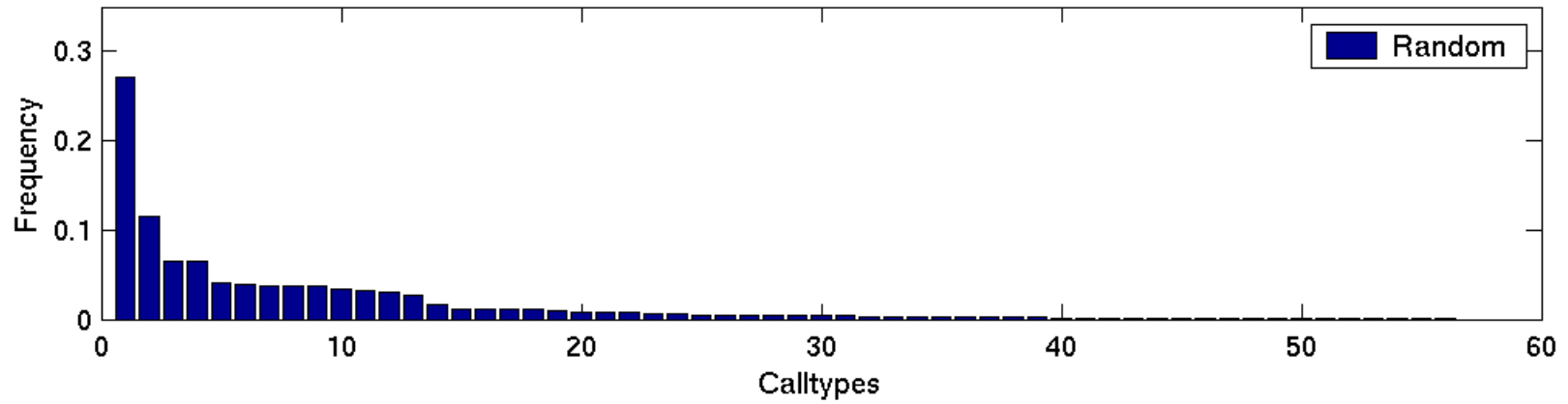
- ◆ *Muslea, Minton, and Knoblock, ICML'02*
- ◆ *Co-EMT algorithm:*
  - Repeat N times
    - Run like *Co-EM* to get multiple learners
    - Run like *Committee-Based Active Learning* to decide on next data to label
- ◆ Outperformed both methods applied individually



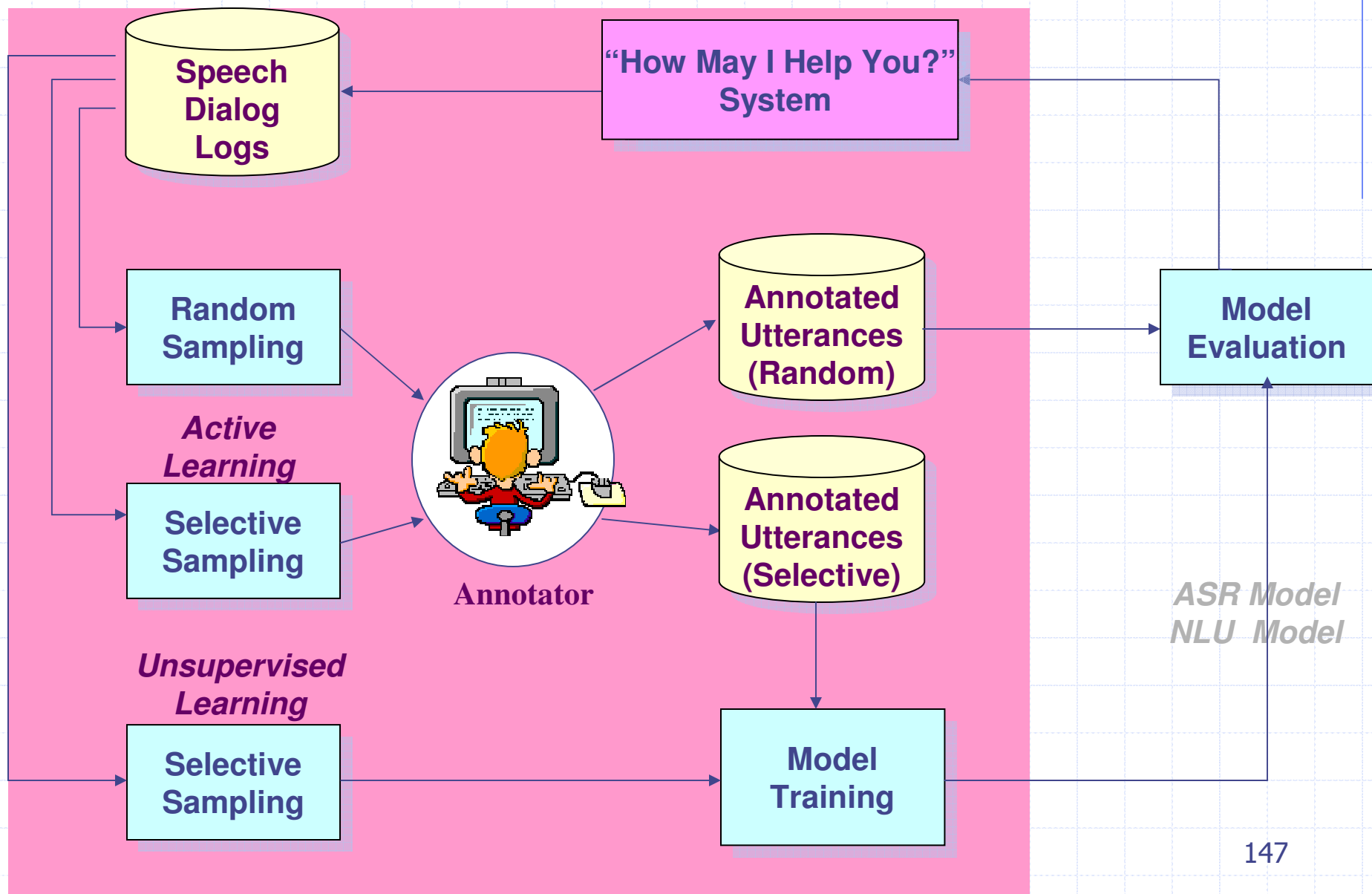
# Unbalanced Data Problem

- ◆ Unsupervised Learning changes the priors, too.
- ◆ Two issues may cancel each other, because:
  - Active Learning shaves more frequent classes
  - Unsupervised Learning do not favor infrequent classes
- ◆ Combining active and unsupervised learning may be a solution to both problems.

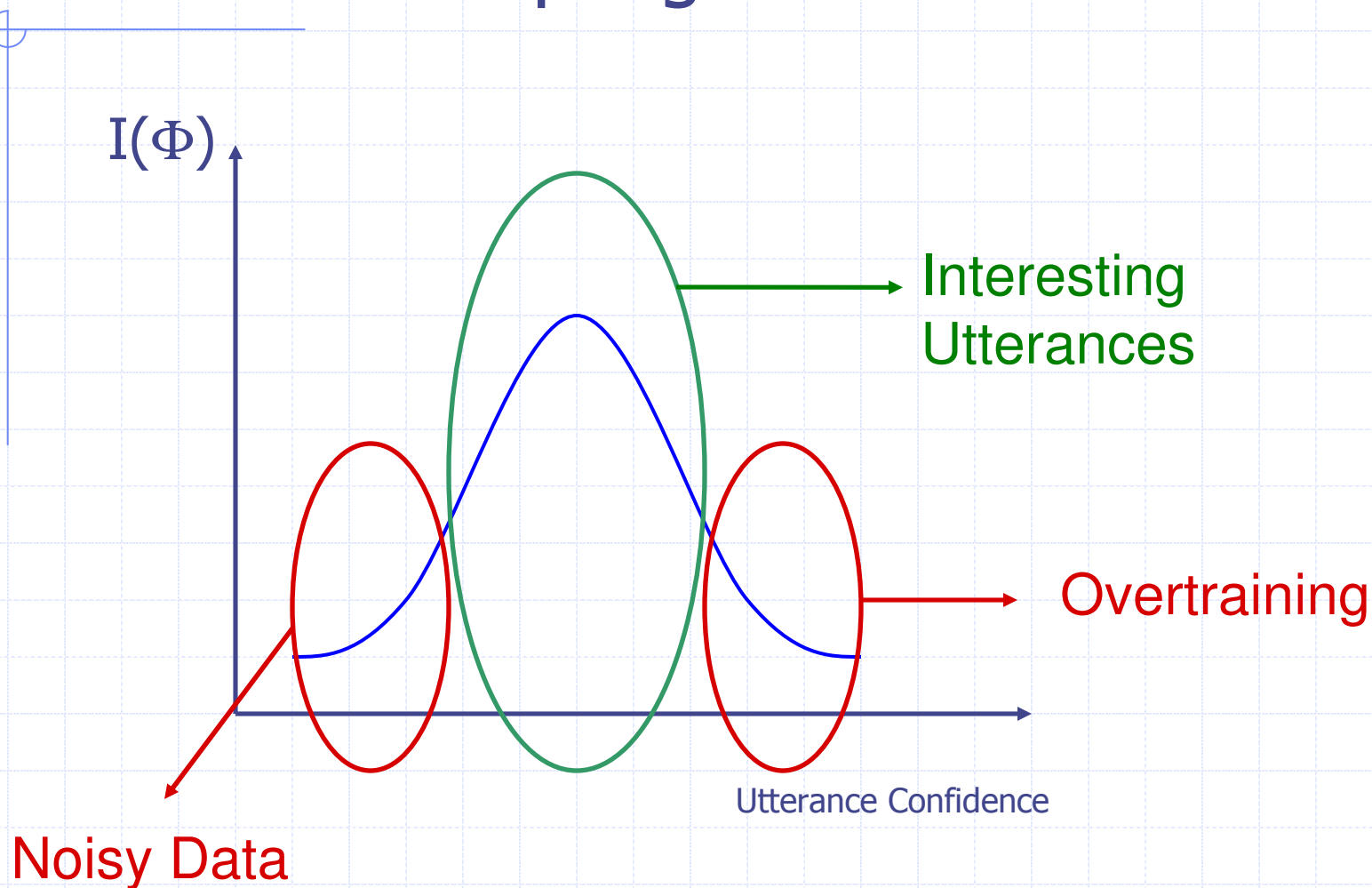
# UNBALANCED DATA PROBLEM



# Adaptive Learning in Practice



# Selective Sampling of Untranscribed Data



# Summary

- ◆ Adaptive Learning for Speech and Language Processing
  - Active Learning
    - ◆ Minimize human supervision by automatically selecting samples to be labeled
    - ◆ Optimize data for performance
  - Unsupervised Learning
    - ◆ Minimize human supervision by automatically labeling some of the data
    - ◆ Improve performance for free (finding unlabeled data is generally not an issue)
  - Combining active and unsupervised learning into a single and dynamic framework

# Open Research Issues

- ◆ Selective Sampling and Ranking algorithms
- ◆ Predict model error based on selected samples
- ◆ AL as optimization problem

# Bibliography

## Automatic Speech Recognition and Speech Understanding

- L. Rabiner and B.-H. Juang. *Fundamentals of Speech Recognition*. Prentice Hall. 1993.
- R. De Mori. *Spoken Dialogues with Computers*. Academic Press. 1998.
- F. Jelinek. *Statistical Methods for Speech Recognition*. MIT Press. 1997.
- T. Mitchell. *Machine Learning*. McGraw-Hill 1997.
- Duda and P. Hart *Pattern Classification and Scene Analysis*. John Wiley & Sons. 1973

## Machine Learning

- T. Hastie, R. Tibshirani and J. H. Friedman. *The Elements of Statistical Learning: Data Mining, Inference and Prediction*. Springer Verlag. 2001.
- Robert E. Schapire. *The boosting approach to machine learning: An overview*. Proceedings of the MSRI Workshop on Nonlinear Estimation and Classification, 2002.
- N. Cristianini, J. Shawe-Taylor. *An Introduction to Support Vector Machines and other kernel-based learning methods*. Cambridge University Press. 2000.

## Active Learning (General)

- D.D. Lewis and J. Catlett. *Heterogeneous Uncertainty Sampling for Supervised Learning*. Proc. of the 11th International Conference on Machine Learning. 1994.
- D. Cohn and L. Atlas and R. Ladner. *Improving Generalization with Active Learning*. Machine Learning. 1994.
- I. Dagan and S.P. Engelson. *Committee-Based Sampling for Training Probabilistic Classifiers*. Proc. of the 12th International Conference on Machine Learning. 1995.

# Bibliography

## Active Learning with Application to Automatic Speech Recognition

- Dilek Hakkani-Tür, Giuseppe Riccardi, Allen Gorin. *Active Learning for Automatic Speech Recognition*. In the Proceedings of International Conference on Acoustics, Speech and Signal Processing (ICASSP 2002). 2002.
- T.M. Kamm and G.G.L. Meyer. *Selective Sampling of Training Data for Speech Recognition*. Proceedings of Human Language Technology Conference. 2002.

## Active Learning with Application to Natural Language Understanding

- Gokhan Tur, Robert E. Schapire, and Dilek Hakkani-Tür. *Active Learning for Spoken Language Understanding*. Proceedings of International Conference on Acoustics, Speech and Signal Processing (ICASSP'03). 2003.
- R. Liere and P. Tadepalli. *The Use of Active Learning in Text Categorization*. Working Notes of the AAAI, Spring Symposium on Machine Learning in Information Access. 1996.

## Unsupervised Learning with Application to Automatic Speech Recognition

- R. Gretter and G. Riccardi. *On-line Learning of Language Models with Word Error Probability Distributions*. Proc. of the IEEE International Conference on Acoustics, Speech and Signal Processing. 2001.
- T. Kemp and A. Waibel. *Learning to Recognize Speech by Watching Television*. IEEE Intelligent Systems. 1999.
- A. Stolcke. *Error Modeling and Unsupervised Language Modeling*. Proceedings of the 2001 NIST Large Vocabulary Conversational Speech Recognition Workshop. 2001.
- G. Riccardi and D. Hakkani-Tür. *Active and Unsupervised Learning for Automatic Speech Recognition*. Submitted.



# Bibliography

## Unsupervised Learning with Application to Natural Language Understanding

- K. Nigam, A. McCallum, S. Thrun and T. Mitchell. *Text Classification from Labeled and Unlabeled Documents using EM*. Machine Learning. Volume 39. Pages: 103-134. 2000.
- R. Ghani. *Combining Labeled and Unlabeled Data for Multiclass Text Categorization*. Proceedings of the 19th International Conference on Machine Learning (ICML-02). 2002.
- A. Blum and T. Mitchell. *Combining Labeled and Unlabeled Data with Co-Training*. Proceedings of the Workshop on Computational Learning Theory (COLT). 1998.
- G. Tur and D. Hakkani-Tür. *Exploiting Unlabeled Utterances for Spoken Language Understanding*. Submitted.